



Calhoun: The NPS Institutional Archive

DSpace Repository

Theses and Dissertations

1. Thesis and Dissertation Collection, all items

1970-09

An evaluation of a modified binary search procedure for use with the Bruceton method in sensitivity testing

Hicks, Donald Lee

Monterey, California ; Naval Postgraduate School

https://hdl.handle.net/10945/14993

This publication is a work of the U.S. Government as defined in Title 17, United States Code, Section 101. Copyright protection is not available for this work in the United States.

Downloaded from NPS Archive: Calhoun



Calhoun is the Naval Postgraduate School's public access digital repository for research materials and institutional publications created by the NPS community. Calhoun is named for Professor of Mathematics Guy K. Calhoun, NPS's first appointed -- and published -- scholarly author.

> Dudley Knox Library / Naval Postgraduate School 411 Dyer Road / 1 University Circle Monterey, California USA 93943

http://www.nps.edu/library

AN EVALUATION OF A MODIFIED BINARY SEARCH PROCEDURE FOR USE WITH THE BRUCETON METHOD IN SENSITIVITY TESTING

by

Donald Lee Hicks



United States Naval Postgraduate School



THESIS

AN EVALUATION OF A MODIFIED BINARY SEARCH PROCEDURE FOR USE WITH THE BRUCETON METHOD IN SENSITIVITY TESTING

by

Donald Lee Hicks

September 1970

This document has been approved for public release and sale; its distribution is unlimited.

T135604



An Evaluation of a Modified Binary Search Procedure for use with the Bruceton Method in Sensitivity Testing

bу

Donald Lee Hicks Major, United States Marine Corps B.S., United States Naval Academy, 1957

Submitted in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE IN OPERATIONS RESEARCH

from the

NAVAL POSTGRADUATE SCHOOL September 1970 the H - 2601

ABSTRACT

Two methods of obtaining sensitivity data were simulated on an electronic computer for the purpose of comparing the accuracy of the estimates of the parameters of an underlying cumulative normal response function. The first method simulated the standard Bruceton procedure while the second used a modified binary search routine with a portion of the sample in order to obtain maximum likelihood estimates of the input parameters for use in a follow-on Bruceton test.

The results showed both methods to be effective in estimating the mean but with slightly more variability in the estimates obtained by the second procedure. Both methods underestimated the standard deviation again with more variability in the estimates obtained by the second procedure. When the prior parameter estimates were unknown and the applicable stimulus level bounded, the second method yielded estimates favorably comparable to those expected from the Bruceton procedure with suitable prior input estimates.

TABLE OF CONTENTS

.

I.	INT	RODU	CTION	Ι.	• •	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	7
II.	THE	MOD	EL .		• •	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•		•	9
III.	TES	TING	METH	IODS		•	•	٠	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	11
	Α.	BRU	CETON	METH	łOD	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	11
		1.	Desc	ripti	ion	•	•	•	•	•	•	•	•	•	•	•	•	•	•		•		•	•	•	•	11
		2.	Disc	ussic	on		•		•	•		•	•	•	•	•			•	•	•	•		•			12
	В.	BRU	CETON	METH	łod	PR	ECH	EDE	D	BY	S	EA	RC	н		•	•	•	•	•	•	•	•	•		•	13
		1.	Desc	ripti	lon	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•			•	13
		2.	Disc	ussid	on	•			•	•	•	•	•		•	•	•		•	•	•	•	•		•	•	19
IV.	SIM	ULAT	ION		• •			•	•	•			•		•			•		•	•	•	•	•	•	•	21
	Α.	DES	CRIPT	ION		•			•	•					•						•					•	21
	В.	MEAS	SURES	OF E	EFFE	CT	IVE	ENE	ss	1		•							•		•	•					22
	с.	DIS	CUSSI	ON							•		•			•	•	•	•	•		•	•	•	•	•	23
	D.	REST	ULTS			•						•									•	•			•		24
V.	CON	CLUS	IONS	AND F	RECO)MM	ENI)AT	IC	NS																	26
	Α.	CON	CLUSI	ONS		•					•						•	•					•			•	26
		1.	Esti	matic	on c	of	the	e M	lea	n											•				•		26
		2.		matic																							
		3	Exte																								
		5.		ence		. Li																					26
		4.	Use	of Se	earc	h '	Гес	hn	iq	ue			•	•	•	•	•	•		•	•	•	•	•	•	•	26
	В.	REC	OMMEN	DATIC	ONS	•	•	•	•	•	•	•		•	•	•	•	•	•	•	•	•	•	•	•	•	26
		1.	Redu	ctior	n of	E Sa	amp	ole	s S	iz	e		•	•	•	•	•	•	•	•		•	•	•	•	•	26
		2.	Rand	om Se	elec	ti	on	of	R	les	рс	ns	e	Fu	inc	ti	or	I	Par	an	net	er	s		•		27
COMPU	TER	PROG	RAM																								28

•

BIBLIOGRAPHY	• • • •	•	•	•	•	•	•	•	•	•	•	•	•	•		•	•	•	•	40
INITIAL DISTRIBUTION	LIST	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•			41
FORM DD 1473				•	•			•			•		•		•					43



LIST OF FIGURES AND TABLES

Figure		Page
1	Starting Sequence	15
2	S _U Sequence	16
3	S* Sequence	17
4	S _L Sequence	18
5	Response Sequences and Parameter Estimates	20
Table		Page

.

I	Table of Experimental Results	25
---	-------------------------------	----



I. INTRODUCTION

Frequently a statistician is faced with the problem of determining the level of a stimulus which critically affects the performance of a device. The nature of the testing to be discussed is such that once some positive level of the stimulus is applied to the device either a response or a non-response can be immediately observed and, in either case, the device is altered so that a bonafide result cannot be obtained from a second test. Tests of this type are known as sensitivity tests.

One of the many problems besetting those involved in explosives research is that of providing measures and specifying rules to provide for the safe handling and transportation of explosives. Many different types of sensitivity testing apparatus have been developed for laboratory use, the most common being those that subject some quantity of explosive to the impact load of a falling drop-weight from some controllable height. At least as late as October 1965 there remained two important physical problems to be solved; namely, that of establishing a measure of stimulus not highly apparatus-dependent and then that of translation of these results to safe handling rules [1]. These problems are not addressed in this paper but should be kept in mind when considering the overall problem.

In the early 1940's, a technique for obtaining sensitivity data was developed and used in explosives research at the Explosives Research Laboratory, Bruceton, Pennsylvania which has come to be called synonymously, the Bruceton, Staircase, or "Up and Down" Method.

The aim of this method of testing is to increase the accuracy with which certain critical values of the stimulus may be estimated, notably the median (or mean) and standard deviation. The accuracy of the method

depends in part on the stimulus level at which the first item is tested and the interval spacing for subsequent levels of testing [2].

When the stimulus levels mentioned above cannot be determined prior to testing or when little confidence is placed on the available estimates, a preliminary (or search) phase of testing may be desirable to obtain maximum likelihood estimates prior to employing the Bruceton Method with the remainder of the sample. A procedure to do this is offered as an alternative method.

The comparative accuracies of the two techniques were examined through the use of simulation conducted on a high-speed electronic computer. All parameters and estimates considered as inputs to the simulation were kept within ranges for which the Bruceton Method is considered to yield accurate results [2].

II. THE MODEL

Let x be an applied stimulus level $(x_{\mathbb{C}}[o,\infty))$ and y = y(x) be the associated response $(y_{\mathbb{C}} \{ o, 1 \}$ where "o" denotes no response and "1" denotes response). At any given stimulus level consider y to be the realization of a Bernoulli random variable, Y, with response probability

$$p(x) = Prob (Y = 1 | x)$$

The function p(x) is called the response function and is further specified as

$p(\mathbf{x}) = 0$	x _€ [o,a]
0 < p(x) < 1	x _c (a,b)
p(x) ≅ 1	x∈[b,∞)

and

The intervals [o,a], (a,b) and $[b,\infty)$ are called the zero-response region, the mixed-response region, and the one-response region respectively. It is assumed that p(x) is a monotonely increasing function for stimulus values in the mixed-response region. Thus, p(x) can be considered as the cumulative distribution function for a random variable X such that

$$p(x) = Prob (X \le x), [3]$$

In this context the random variable X can be interpreted as a threshold stimulus level, thus

Prob (Y = 1 | x) = Prob (X < x) = p(x)

and

Prob (Y = 0 | x) = Prob (X > x) = 1 - p(x). [3]

It is assumed the X is distributed Normal (μ, σ^2) ; that is

$$p(\mathbf{x}) = \varphi(\mathbf{x} | \mu, \sigma^2)$$

where $\varphi(x | \mu, \sigma^2)$ represents the cumulative normal distribution with mean

 μ and variance $\sigma^2.~$ In particular

Prob $(x \le \mu) = p(\mu) = 0.5$. [3]

and the participant of the participant

The state of the second second

III. TESTING METHODS

A. BRUCETON METHOD

1. Description

Based on intuition or past experiments, the experimenter selects a priori estimates of μ and σ . Call these estimates μ_I and σ_I and let $d = \sigma_I$.

The experimenter tests the first item at or near μ_{I} . If there is a response the second item is tested at a level d units below μ_{I} , otherwise the second item is tested at a level d units above μ_{I} . In the same manner, each of the remaining items is tested at a level d units above or below the previous test level according as there was not or there was a response observed for the previous test. Thus the sample is concentrated about the mean and one would expect nearly equal numbers of responses and non-responses. In fact, the number of nonresponses at any level will not differ by more than one from the number of responses at the next higher level [2].

Let N denote the total number of observations of the less frequent event and $n_0, n_1, n_2, \cdots n_k$ denote the frequencies of this event at each level where n_0 corresponds to the lowest level and n_k the highest level at which the less frequent event occurs.

The final estimates of μ and σ are based on the first two moments of the stimulus levels. Since the intervals are equally spaced, these moments can be computed in terms of the sums

$$A = \sum_{i} i n_{i}$$
$$B = \sum_{i} i^{2} n_{i}.$$

and

Let $\stackrel{\wedge}{\mu}$ be the estimate of μ by this method. Then

$$\hat{\mu} = x' + d \left(\frac{A}{N} \pm \frac{1}{2}\right)$$

where x' represents the lowest level at which the less frequent event occurs [2]. The plus sign is used when the analysis is based on nonresponses, and the minus sign when it is based on responses [2].

If $(NB-A^2)/N^2 > .3$ the sample standard deviation is

s = 1.620 d
$$\left(\frac{\text{NB}-\text{A}^2}{\text{N}^2} + .029\right)$$

Otherwise, a more elaborate calculation must be employed and is described in Ref. 2.

To obtain confidence intervals, estimates of the standard deviations of the sample mean and sample standard deviation, say s and s respectively, are given by

$$s_m = \frac{Gs}{\sqrt{N}}$$

and

$$s_s = \frac{Hs}{\sqrt{N}}$$

where the factors G and H are dependent on the ratio $\frac{d}{s}$ and the position of the mean relative to the testing levels. Plots of these factors are available in Ref. 1.

2. Discussion

Only rarely is the threshold stimulus Z normally distributed. It is usually the case that some scale transformation of Z, say X, is made so that X is normally distributed in the vicinity of the mean. This transformation is done prior to testing to determine μ_{I} and σ_{I} . Only after all analysis is completed are the values scaled back to the original stimulus measure [2].

The size of the sample is critical to the accuracy of the estimation. Note that at most only half of the sample is used in the analysis so that, for example, if thirty items are tested the maximum possible value of N is fifteen. The analysis is based on large sample theory which in the case mentioned would be applied to a sample of size fifteen [2] [4].

Unless normality of the variate is assured this method does not yield accurate results for the small and large percentage points. This is unfortunate since in most applications one would be more interested in a small percentage point as a measure of safety and a large percentage point as a measure of reliability. At any rate, an estimate of a percentage point j is

$$j = \hat{\mu} + ks$$

where k is chosen from tables of the standard normal deviate to give the desired percentage [2]. One could then conduct tests in the vicinity of this value to refine the estimate.

B. BRUCETON METHOD PRECEDED BY SEARCH

1. Description

In the event that a priori estimates of μ and σ are not available some economic method of attaining these estimates is desired. A method proposed and described below is a modified binary search technique.

Again, the assumption is that the threshold stimulus (or some transformation of it) is normally distributed and p(x) can be represented by a cumulative normal distribution.

As noted from the model

Prob
$$(Y = 0 | x \le a) \approx 1$$

and

Prob
$$(Y = 1 | x \ge b) = 1$$
.

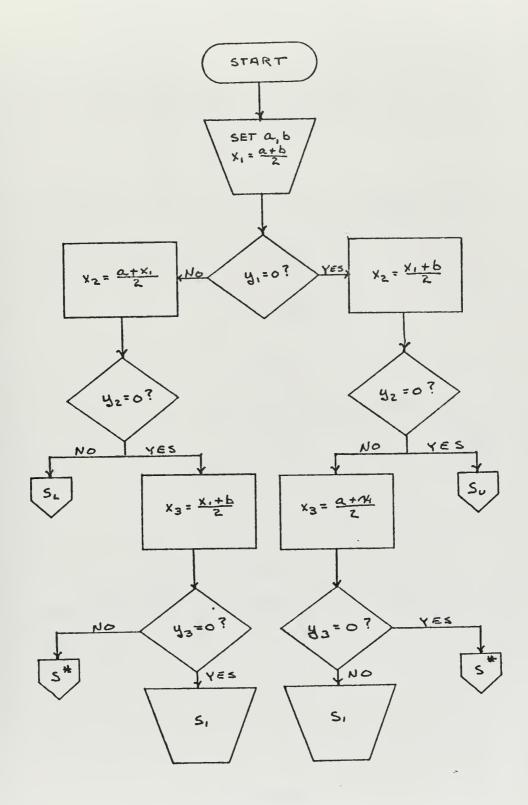
The first step in the procedure, then, is to select values for a and b. (In the case of complete uncertainty these could be the limiting values of the testing apparatus) and commence the binary search starting at

$$x = (a + b)/2$$
.

If p(x) were a step function, repetition of this method would locate the step in an interval of any desired length. In general, however, the mixed-response region has non-zero width and a non-response would merely indicate that the applied stimulus is in the mixed response region or below while a response would indicate that it was in the mixed response region or above.

If a test at x_1 yields a response and a test at x_2 yields a non-response while $x_1 < x_2$ it is certain that both x_1 and x_2 are in the mixed response region. This condition is called a response inversion and is the basic indicator for the modified binary search technique. The description of the procedure is best followed by referring to Figures 1 through 4.

Sequence S* is a cyclic one indicating that a reduction in step size should be taken. Test levels are selected attempting to reproduce this sequence. Failure to do this results in the basic inversion sequence S_0 . Tests are then made at the end of this sequence to result in one of three terminal situations S_1 , S_2 , or S_3 . In the event the mixed response region is relatively narrow and near a or b, several binary reductions may be necessary to reproduce S* or one of the terminal situations. These circumstances are represented by S_L and S_{II} [3].

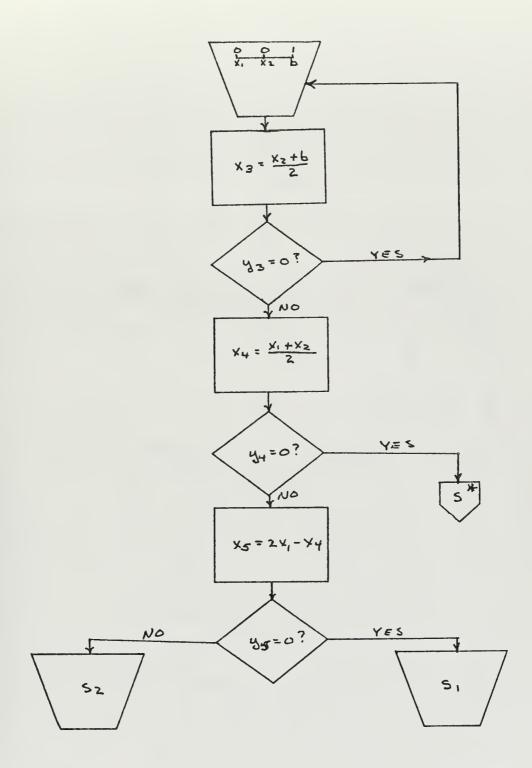


STARTING SEQUENCE

Figure 1

**





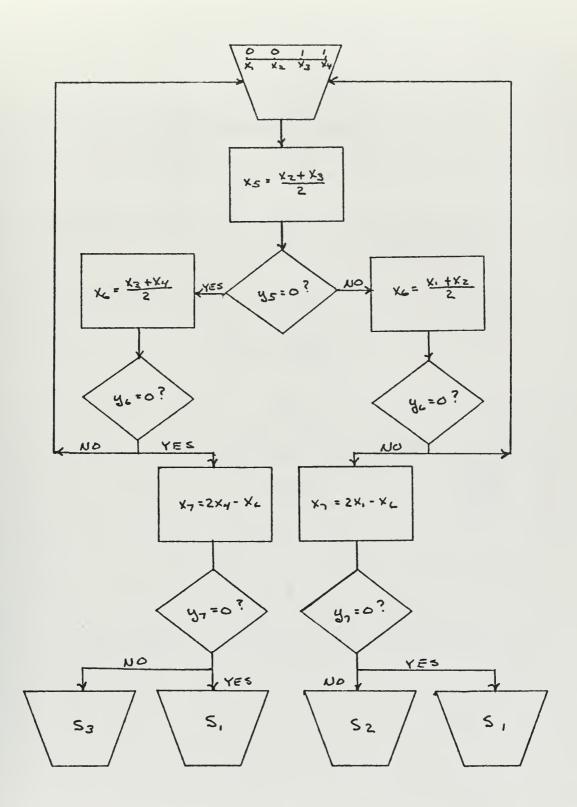
S_U SEQUENCE Figure 2

¢

-

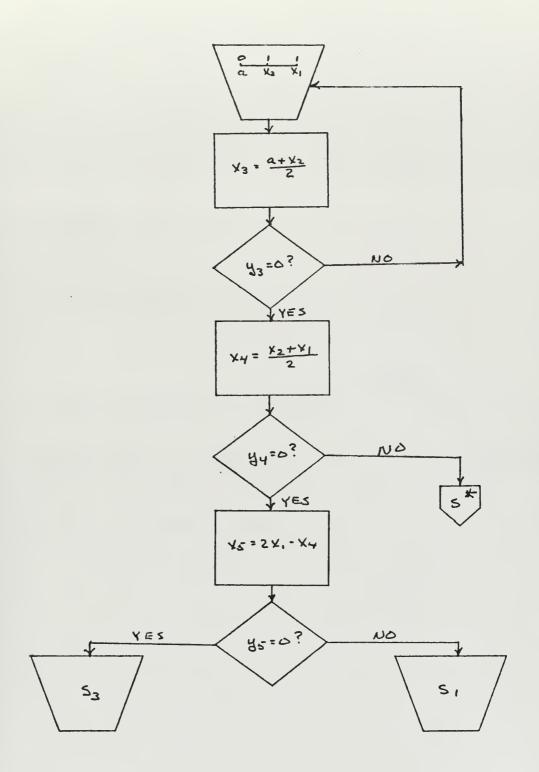


S* SEQUENCE



a





S_L SEQUENCE



e

Maximum likelihood estimates of μ and σ are available for sequences S₁, S₂, and S₃ and developed as described below [3].

2. Discussion

It is assumed that all trials are independent. Thus the probability of the sequence S_1 is

Prob (S₁) = Prob (Y₁=0, Y₂=0, Y₃=1, Y₄=0, Y₅=1, Y₆=1|X₁, X₂, X₃, X₄, X₅, X₆)

$$= \begin{array}{c} 6\\ \pi\\ i=1 \end{array} Prob (Yi = yi|xi)$$

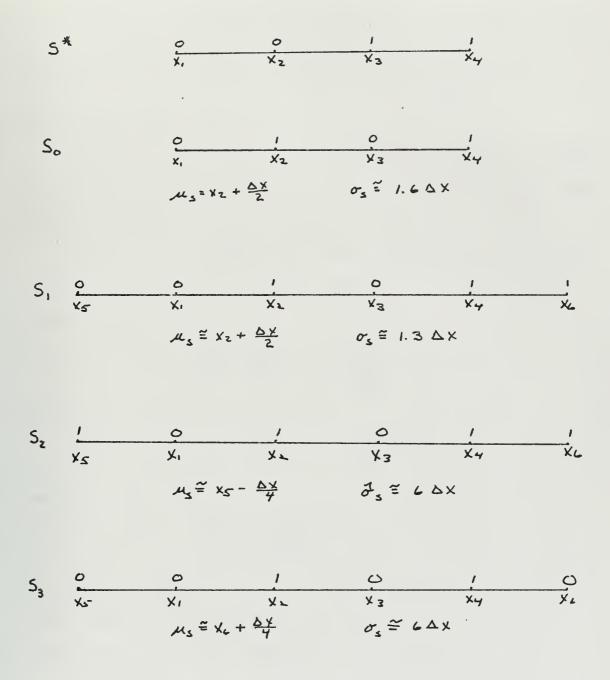
where

Prob
$$(Y_i = y_i | x_i) = \phi(x_i)$$
 if $y_i = 1$
= 1 - $\phi(x_i)$ if $y_i = 0$

and

$$\varphi(x_i) = \operatorname{Prob} (X_i \le x_i) = \int_{-\infty}^{x_i} \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{1}{2} \frac{(X-\mu)^2}{\sigma}} dx.$$

Maximum likelihood estimates for μ and σ can then be established using standard normal tables for each of the terminal situations. These estimates are indicated on Figure 5.



RESPONSE SEQUENCES AND PARAMETER ESTIMATES

Figure 5

IV. SIMULAT.ON

A. DESCRIPTION

All simulated experiments were conducted on an IBM 360/67 computer using the FORTRAN IV programming language. The basic program is attached. The response function p(x) used was cumulative normal with $\mu = 30$ and $\sigma = 3$.

The sample size was kept at seventy for each experiment to provide some assurance that the analytical sample would be suitable for large sample analysis.

The basic test procedure was to draw a random number on the unit interval and compare this to F(x), a function of a standard normal variate specified as

$$F(x) = \frac{1}{2} \left[1 - \operatorname{erf} \left(\frac{x}{\sqrt{2}} \right) \right] \quad \text{if } x < 0$$

and

$$F(x) = \frac{1}{2} \left[1 + \operatorname{erf} \left(\frac{x}{\sqrt{2}} \right) \right] \quad \text{if } x \ge 0$$

where

$$erf(v) = \frac{2}{\sqrt{\pi}} \int_{0}^{v} e^{-t^{2}} dt.$$

(The function subprogram erf is an IBM-supplied subprogram.) If the random number was less than or equal to $F(x_i)$ then a response was counted for the ith level; otherwise a non-response was counted.

Six different cases were tested using the straight Bruceton procedure (METHOD 1) with two different input estimates of μ and three different input estimates of σ . Case 1 considered exact estimates; i.e., $\mu_{I} = \mu$ and $\sigma_{I} = \sigma$. Case 2 considered $\mu_{I} = \mu$ -6 and $\sigma_{I} = \sigma$.

Cases 3 and 4 considered $\mu_{I} = \mu$ and $\sigma_{I} = \sigma/2$, 2σ respectively while Cases 5 and 6 repeated Cases 3 and 4 except $\mu_{I} = \mu$ -6. For each of the six cases 1000 experiments were conducted each utilizing a different sequence of random numbers.

The search procedure (METHOD 2) was then incorporated into each of the above six cases using the a prior estimates, μ_{I} and σ_{I} , to determine estimates for stimulus levels a and b and thereby the size of the binary reduction as indicated in Figure 1. The program then followed the flow shown in Figures 1 through 4 until either a terminal sequence was reached or the search was arbitrarily terminated as discussed in subparagraph C below. The Bruceton procedure was then used until the sample was exhausted.

The final case, Case 7, indicated complete lack of knowledge of μ and σ but considered the upper and lower stimulus level limits of the test apparatus to be 100 and 0 respectively.

B. MEASURES OF EFFECTIVENESS

At the completion of all experiments for each case, several measures were obtained for comparison. First, average values of the parameters were determined to be

$$\bar{\hat{\mu}} = \sum_{i} \hat{\mu}_{i} / N$$

and

$$\overline{\hat{\sigma}} = \sum_{i} \hat{\sigma}_{i} / N$$

where $\hat{\mu}_{I}$ and $\hat{\sigma}_{I}$ are the a posteriori estimates of μ and σ for the ith experiment and n, the number of experiments used. Next, as measures of variability

$$s_{\hat{\mu}}^{2} = \sum_{i} (\hat{\mu}_{i} - \mu)^{2}/n-1$$

and

$$s_{\sigma}^{2} = \sum_{i} (\hat{\sigma}_{i} - \sigma)/n-1$$

were calculated. In addition, the program listed the maximum and minimum estimates of both μ and σ .

C. DISCUSSION

In Chapter III it was noted that sequences S*, S_U , and S_L are cyclic. In order to simplify the program it was necessary to artificially terminate these situations at some point and calculate the input values for the Bruceton test. The estimate of μ used was

$$\mu_{\rm s} = (x_1 + x_2)/2$$

where x_1 and x_2 are adjacent testing levels and $x_2 > x_1$ with $y_1 = 0$ and $y_2 = 1$. The estimate of σ used was

$$\sigma_{\rm s} = ({\rm x}_2 - {\rm x}_1)/2$$

for Cases 1 through 6 and

$$\sigma_{s} = (x_{2} - x_{1})/6$$

for Case 7. The former estimate of σ was chosen arbitrarily while the latter estimate was based on the estimate of the mixed response region being 6 σ . While the number of terminations of this type was insignificant for the first six search cases, in the final case over 600 experiments were thus terminated requiring the program to be expanded to permit more recycling. The point is that the artificial termination does not represent the search procedure. This problem would not arise in field experimentation until either the sample was exhausted or the step size reduction of stimulus level indicated was too narrow to be measured or controlled by the test apparatus.



Also in the interest of program simplification those experiments for which

$$\frac{NF - A^2}{N^2} \le .3$$

were not used for analyses. This limitation invalidated the measures of effectiveness for the Bruceton cases where $\sigma_T = 2\sigma$.

D. RESULTS

The results of the simulation are listed in Table I. It is questionable that the measures listed under Method 1 are valid for Cases 4 and 6 in that only .381 and .393 of the possible experiments were used. These two cases and Case 4 under Method 2 (where .661 of the possible experiments were used) are the only ones for which $\overline{\hat{\sigma}} > \sigma$.

In general the extreme estimates are more widely separated and the variability of $\hat{\sigma}$ is greater in Method 2.

Estimates of μ range from 27.8823 to 31.7647 for Method 1 and 27.937 to 31.91 for Method 2.

Estimates of σ range from .8741 to 6.5027 for Method 1 and .3498 to 9.8328 for Method 2.

The lowest average $\hat{\mu}$, 29.9113, was obtained under Method 1, Case 5, while the highest average $\hat{\mu}$, 30.1175, was obtained under Method 2, Case 3.

The lowest average $\hat{\sigma}$, 2.3748, was obtained under Method 2, Case 5, while the highest average $\hat{\sigma}$, 2.9474, was obtained under Method 1, Case 5. (Case 6 is not counted under Method 1 nor is Case 4 under both methods.)

24

TABLE OF EXPERIMENTAL RESULTS

		METHOD 1		METHOD 2	
		μ	σ	ĥ	σ
CASE	1				
$\mu_{T} = 30$	AVE	30.0067	2.8320	30.0117	2.8609
$\sigma_{T} = 3$	MAX	31.7647	5.7904	31.7813	5.9343
a = 18	MIN	28.5000	1.6089	28.2187	1.1241
b = 42 VAR		.2523	.4128	.2514	.5831
CASE	2				
$\mu_{I} = 24$	AVE	29.9641	2.9040	30.0317	2.8819
$\sigma_{I} = 3$	MAX	31.6765	5.8249	31.6875	9.1369
a = 12	MIN	28.3235	1.6250	28.1976	.9512
b = 36	VAR	.2656	.4225	.2666	.6336
CASE	3				
$\mu_{I} = 30$	AVE	30.0295	2.7216	30.1175	2.8615
$\sigma_{T} = 1.5$	MAX	31.6071	6.1197	31.9100	7.7997
a = 24	MIN	28.4118	.8741	28.5950	.8697
b = 36	VAR	.2046	.7409	.2693	.9081
CASE	4				
$\mu_{T} = 30$	AVE	29.9683	3.5424	29.9750	3.0721
$\sigma_{\rm I} = 6$	MAX	31.4571	6.0266	31.6875	6.3569
a = 6	MIN	28.0286		27.9370	1.6170
b = 54	VAR	.2574	.4639	.2619	.4522
CASE	5				
$\mu_{I} = 24$	AVE	29.9113	2.9474	29.9363	2.3748
$\sigma_{I} = 1.5$	MAX	31.4773	5.9257	31.4063	7.9507
a = 18	MIN	28.2353	.9452	28.1961	.3498
b = 30	VAR	.2220	.8748	.2184	1.4889
CASE	6				
$\mu_{I} = 24$	AVE	29.9493	3.5438	30.0247	2.8398
$\sigma = 6$	MAX	31.4118	6.5027	31.5756	6.4201
a = 0	MIN	27.8823		28.2552	1.1252
b = 48	VAR	.2639	. 4785	.2490	.6300
CASE	7				
	AVE			30.0123	2.7280
	MAX			31.8229	9.8328
a = 0	MIN			27.9541	.5082
b = 100	VAR			.2628	2.1041

V. CONCLUSIONS AND RECOMMENDATIONS

A. CONCLUSIONS

1. Estimation of the Mean

Both methods estimate the mean effectively.

2. Estimation of the Standard Deviation

Both methods tend to under-estimate the standard deviation with no predictable bias and are therefore unsuitable for use in safety or reliability statements. This conclusion agrees with the findings of Hampton [4] as it pertains to the Bruceton Method.

3. Extension of the Search Phase for the Starting Sequence

Termination of the search phase with sequence S_1 in the starting sequence (see Figure 1) may yield estimates of σ greater than twice the actual value. To avoid this it is advisable to extend the search phase as described in Ref. 3.

4. Use of Search Technique

The search procedure should be used in those cases where there is not independent evidence that the estimate of σ is within the range for which the Bruceton Method is recommended (i.e., $\sigma/2 < \sigma_T < 2\sigma$).

B. RECOMMENDATIONS

Further testing of Method 2 is recommended under the circumstances listed below.

1. <u>Reduction of Sample Size</u>

It would be of interest to reduce the sample size to the point where the effective sample is small, say 15, and compare the Bruceton procedure with the search procedure using the entire sample for the search.

26

2. Random Selection of Response Function Parameters

A more valid test of both methods would be achieved by randomally selecting values of μ and σ over some range and using the on-line computer facility to conduct the simulation.

- 5



THIS PROGRAM SIMULATES SENSITIVITY TESTING BY BOTH THE BRUC-ETON METHOD (WHEN IANY=0) AND THE BRUCETON METHOD PRECEDED BY THE MODIFIED BINARY SEARCH (WHEN IANY=1). THE UNDERLYING RESPONSE FUNTION IS CUMULATIVE NORMAL (30,3). THE INPUT EST-IMATES OF THE MEAN AND THE STANDARD DEVIATION ARE CALLED EXMU AND EXSIG RESPECTIVELY.

PRINCIPLE VAPIABLE NAMES ARE AS FOLLOWS... ACT IS THE STIMULUS VALUE AT THE UPPER LIMIT OF THE MIXED RESPONSE REGION. THE AACT IS BACT IS THE STIMULUS VALUE AT THE LOWER LIMIT OF THE MIXED RESPONSE REGION. A AND B ARE ESTIMATES OF AACT AND BACT RESPECTIVELY. X(J) IS THE STIMULUS LEVEL OF THE JTH. STIMULUS. IXO(J) IS THE CUMULATIVE COUNT OF NON-RESPONSES AT X IXX(J) IS THE CUMULATIVE COUNT OF RESPONSES AT X(J) THE JTH. STIMULUS. NON-RESPONSES AT X(J). IXO(J) IS IXX(J) IS IS IS THE NU IS THE SAMPLE SIZE. ENTRY NUMBER FOR THE RANDOM NUMBER GENERATOR, THE NU UNIF N COUNTS N COUNTS THE NUMBER OF EXPERIMENTS. RN IS THE RANDOM NUMBER ON (0,1) RETURNED BY UNIF. FOFX IS THE VALUE OF THE RESPONSE FUNCTION RETURNED BY SUBPROGRAMS XNCDF AND SNCDF. ISUMO IS THE TOTAL NUMBER OF NON-RESPONSES FOR ONE EXPER-INCLISE TOTAL NUMBER OF RESPONSES FOR ONE EXPERIMENT ISUMX IS THE TOTAL NUMBER OF RESPONSES FOR ONE EXPERIMENT NT IS THE MINIMUM OF ISUMO AND ISUMX. NS(J) IS THE FREQUENCY OF THE LESS FREQUENT EVENT AT X(J) NG(J) REARRANGES NS(J) SO THAT NG(1)=NS(I) WHERE X(I) IS THE LOWEST STIMULUS LEVEL AT WHICH THE LESS FREQUENT EVENT OCCURS. UWEST STINUEUS LETTE OCCURS. USED TO CALCULATE THE FIRST MOMENT,SUMAP. USED TO CALCULATE THE SECOND MOMENT,SUMBR. S THE LOWEST LEVEL AT WHICH THE LESS FREQUENT AR(J) IS YPRIME I ĨS XMUEST DEVEST IS THE FINAL ESTIMATE OF THE TRUE MEAN, XMU. IS THE FINAL ESTIMATE OF THE TRUE STANDARD DEVIAT-ION, XSIG. EMU(J) IS THE DIFFERENCE OF XMUEST AND XMU. EDEV(J) IS THE DIFFERENCE OF DEVEST AND XSIG. SAMAVM AND SAMAVD ARE THE SAMPLE AVERAGE FRRORS OF XMUEST FMU(J) EDEV(J) AND DEVEST RESPECTIVELY. SAMSOM AND SAMSOD ARE THE AVERAGE MEAN SQUARE ERRORS OF XMUEST AND DEVEST RESPECTIVELY. NOGO IS THE NUMBER OF EXPERIMENTS NOT USED IN THE FINAL ANALYSIS DIMENSION ARRAYS AND FORMAT SIMULATE BRUCETON FIRST THEN SEARCH IANY=069 THING=0.

INITIALIZE INTERNAL AND OUTPUT VARIABLES

SET EXPERIMENT COUNTER, SAMPLE SIZE COUNTER, AND NU.

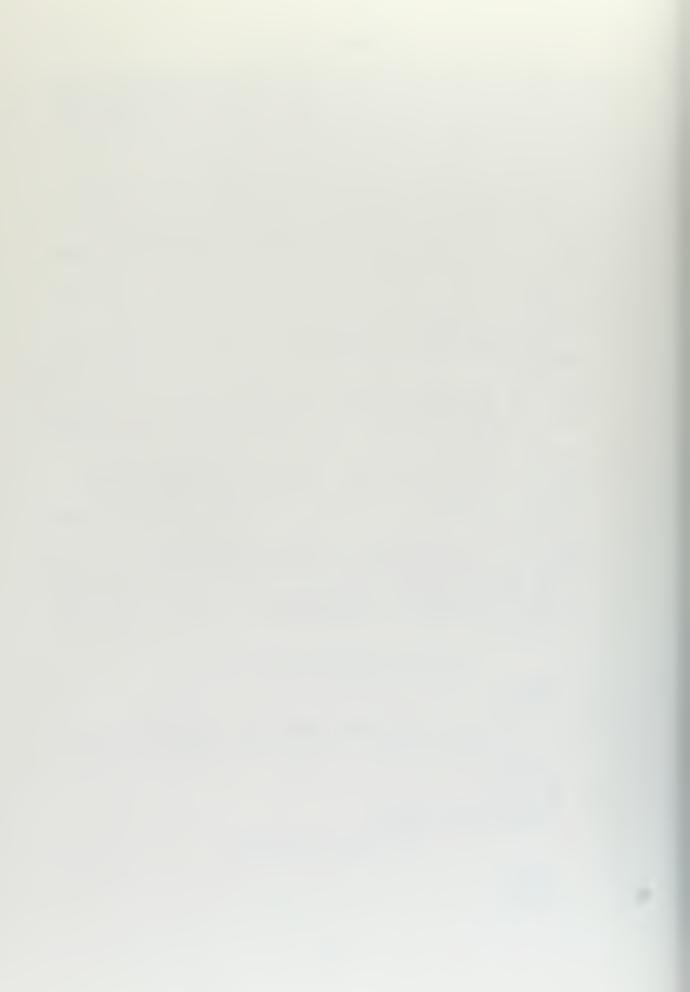
103

N=1 IF(IANY.EQ.0) NBR=0 IF(IANY.EQ.1) NBR=1

SET INPUT VARIABLES

XMU=30. XSIG=3. A=0. B=100. EXMU=50.

LCOUNT=1 NU=12371



EXSIG=12.5 A= EXMU-IQ*EXSIG B= EXMU+IQ*EXSIG X1 = (A+B)/2. IQ=4 INC = 0PROVIDE BRANCH TO STANDARD BRUCETON IF(NBR.EQ.0) GO TO 33 CONDUCT SEARCH CALL UNIF(RN, NU) FOFX=XNCDF(X1, XMU, XSIG) IF(RN.LE.FOFX) GD TD 9500 X2=(B+X1)/2. NBR=NBR+1 CALL UNIF(RN, MU) FOFX=XNCOF(X2,XMU,XSIG) IF(RN.LE.FOFX) GO TO 9250 X3=(B+X2)/2. NBR = NBR + 1CALL UNIF(RN,NU) FOFX=XNCDF(X3,XMU,XSIG) IF(RN.LE.FOFX) GO TO 9125 X4=(B+X3)/2. X4=(B+X5)/2. NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X4,XMU,XSIG) IF(RN,LF,FOFX) GO TO 9063 X5=(B+X4)/2. X5=(B+X4)/2. NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X5,XMU,XSIG) IF(RN.LE.FOFX) GO TO 1313 EXMU=(B+X5)/2. EXSIG=(X5-X4)/2. EXSIG=2.**XSIG EXSIG=EXSIG/6. GO TO 7000 EXMU=(X5+X4)/2. EXMU=(X5+X4)/2. EXSIG=(X5-X4)/2. EXSIG=2.*EXSIG EXSIG=EXSIG/6. 1313 EXSIG=EXSIG/6. GO TO 7C00 X5=(X3+X2)/2. NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X5,XMU,XSIG) IF(RN.LE.FOFX) GO TO 1314 X6=(X3+X4)/2. NBR=NBR+1 CALL UNIF(RN.NU) 9063 NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X6,XMU,XSIG) IF(RN.LE.FOFX) GO TO 1316 EXMU=(X6+X4)/2. EXSIG=(X6+X3)/2. EXSIG=2.*EXSIG EXSIG=5XSIG/6. GO TO 7000 EXMU=(X6+X3)/2. EXSIG=2.*EXSIG EXSIG=2.*EXSIG EXSIG=FXSIG/6. GO TO 7000 1316 GO TO 7000 X6=2.*X2-X5 NBR=NBR+1 1314 CALL UNIF(PN, NI) FOFX=XNCDF(X6,XMU,XSIG) IF(PN.LE.FOFX) GO TO 1315 XB = X5

DELX=X5-X2 EXMU=X8+DELX/2. EXSIG=1.3*DELX GO TO 7000 1315 XB = X6DELX=X2-X6 EXMU=XB-DELX/4. EXSIG=6*DELX GD TO 7000 9125 X4 = (X2 + X1)/2. NBR=NBR+1 CALL UNIF (RN, NU) FOFX=XNCDF(XA,XMU,XSIG) IF(PN.LE.FCFX) GO TO 9094 X5=(X2+X3)/2. NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X5,XMU,XSIG) IF(RN.LE.FOFX) GD TD 9047 $X_{5}=(B+X_{3})/2$. NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X6,XMU,XSIG) IF(RN,LE,FOFX) GO TO 9024 X7=2.*B-X5 NBR=NBR+1 CALL UNIF(RN, NU) FOFX=XNCDF(X7,XMU,XSIG) IF(RN.LE.FOFX) GO TO 9012 XB=X7 DELX=XB-B EXMU=XB+DELX/4. EXSIG=6.*DELX G0 T0 7000 9012 XB=X3 DELX=X6-XB EXMU=XB+DELX/2. EXSIG=1.3*DELX GO TO 7000 EXMU=(X3+X5)/2. EXSIG=(X3-X5)/2. EXSIG=2.*EXSIG EXSIG=FXSIG/6. GO TO 7000 Y6-(Y6+Y2)/2 9024 $X_{6}=(X_{4}+X_{2})/2$. 9047 NBR=NBR+1 NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X6,XMU,XSIG) IF(RN.LE.FOFX) GO TO 9011 EXMU=(X5+X2)/2. EXSIG=(X5-X2)/2. EXSIG=2.*EXSIG EXSIG=EXSIG/6. CO TO 7000 GO TO 7000 X7=2.*X4-X6 NBR=NBR+1 9011 CALL UNIF(RN,NU) FOFX=XNCDF(X7,XMU,XSIG) IF(RN.LE.FOFX) GO TO 9010 XB = X6DELX=X2-XB EXMU=XB+DELX/2. EXSIG=1.2*DELX GD TD 7000 9010 XB = X7DELX=X4-X7 EXMU=XB-DELX/4. EXSIG=6*DELX GO TO 7000 X5=2*X1-X4 9094 NBR = NBR + 1CALL UNIF(RN,NU)

FOFX=XNCDF(X5,XMU,XSIG) IF(RN.LE.FOFX) GD TD 9003 XB = X4DELX = X2 - X4EXMU=XB+DELX/2. EXSIG=1.3*DELX GD TO 7000 9003 XB = X5DELX=X1-X5 EXMU=XB-DELX/4. EXSIG=6.*DELX GD TD 7000 9250 X3 = (A + X1)/2.A3=(A+X1)/2. NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X3,XMU,XSIG) IF(RN.LE.FOFX) GO TO 9375 X4=(X1+X2)/2. NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X4,XMU,XSIG) IF(RN.LE.FOFX) GO TO 9004 X5=(B+X2)/2. NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X5,XMU,XSIG) IF(RN.LE.FOFX) GO TO 9005 X6=2*8-X5 NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X6,XMU,XSIG) IF(RN.LE.FOFX) GO TO 9006 XB = X6DELX=X6-B EXMU=XB+DELX/4. EXSIG=6*DELX GO TO 7000 9006 XB = X2DELX=X5-XB EXMU=XB+DELX/2. EXSIG=1.3*DELX GO TO 7000 EXMU=(X2+X4)/2. EXSIG=(X2-X4)/2. EXSIG=2.*EXSIG EXSIG=EXSIG/6. 9005 GO TO 7000 X5=(X1+X3)/2. 9004 NBR=NBR+1 NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X5,XMU,XSIG) IF(RN.LE.FOFX) GD TO 5555 EXMU=(X1+X4)/2. EXSIG=(X4-X1)/2. EXSIG=2.*EXSIG EXSIG=FXSIG/6. GD TO 7000 X6=2.*X3-X5 NBR=NBR+1 5555 NBR=NBR+1 CALL UNIF(RM,NU) FOFX=XNCDF(X6,XMU,XSIG) IF(RN.LE.FOFX) GD TD 9007 XB = X5DELX=X1-XR EXMU=XB+DELX/2. EXSIG=1.3*DELX GO TO 7000 9007 XB = X6DELX=X3-XB EXMUEXB-DELX/4. EXSIG=6*DELX GO TO 7000

9375 X4=2.*A-X3NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X4,XMU,XSIG) IF(RN.LE.FOFX) GO TO 9376 XB = X3DELX=X1-XB EXMU=XB+DELX/2. EXSIG=1.3*DELX GD_TD_7000 9376 XB = X4DELX=A-XB EXMU=XB-DELX/4. EXSIG=6*DELX GO TO 7000 9500 X2=(A+X1)/2. NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X2,XMU,XSIG) IF(RN.LE.FOFX) GO TO 9501 X3=(X1+B)/2. NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X3,XMU,XSIG) IF(RN.LE.FOFX) GO TO 5556 X4=2.*8-X3 NBR=NBR+1 CALL UNIF(RN,NU) FUFX=XNCDF(X4,XMU,XSIG) IF(RN.LE.FUFX) GO TO 5554 XB=X4 DELX=X4-XB EXMU=XB+DELX/4. EXSIG=6*DELX GO TO 7000 5554 XB=X1 DELX=X3-XB EXMU=XB+DELX/2. EXSIG=1.3*DELX GD TO 7000 5556 X4=(X1+X2)/2. NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X4,XMU,XSIG) IF(RN.LE.FOFX) GO TO 5557 X5=(X1+X3)/2. NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X5,XMU,XSIG) IF(RN.LE.FOFX) GO TO 5553 X6=2.*X3-X5 NBR=NBR+1 NBR=NBR+1 NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X6,XMU,XSIG) IF(RN.LE.FOFX) GD TD 5559 XB = X6DELX=XB-X3 EXMU=XB+DELX/4. EXSIG=6*DELX GO TO 7000 ĜÖ KB = X1
DELX = X5 - X1
EXMU = XB + DELX/2.
EXSIG=1.3*DELX
GO TO 7000
EVELX 5559 EXMU=(X4+X1)/2. EXSIG=(X1-X4)/2. EXSIG=EXSIG/3. GO TO 7000 5553 X5=(A+X2)/2. 5557 NBR=NBR+1 CALL UNIF (RN, NU)

.

FOFX=XNCDF(X5,XMU,XSIG) IF(RN.LE.FOFX) GO TO 5561 X6=(X2+X4)/2. NBR=NBR+1 CALL UNIF (RN, NII) FOFX=XNCDF(X6,XMU,XSIG) IF(RN.LE.FOFX) GO TO 121 X7=(X4+X1)/2. NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X7,XMU,XSIG) IF(RN.LE.FOFX) GO TO 122 X8=2.*X1-X7 NBR=NBR+1 CALL UNIF(RN,MU) FOFX=XNCDF(X8,XMU,XSIG) IF(RN.LE.FOFX) GO TO 123 FXMU=X8+(X8-X1)/4. 123 $x_{B}=(x_{6}+x_{4})/2$. 122 XD=(X0+X4)/2. NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X8,XMU,XSIG) IF(RN.LE.FOFX) GO TO 124 X9=(X4+X7)/2. NBR=NBR+1 NGR=NBR+1 CALL UNIF(RN,NU) FDFX=XNCDF(X9,XMU,XSIG) IF(RN.LE.FDFX) GO TO 125 EXMU=(X4+X9)/2. EXSIG=1.3*(X9-X4) GO TO 7000 EXMU=(X8+X4)/2. 125 EXSIG=(X4-X8)/6. GO TO 7000 X9=(X2+X6)/2. 124 NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X9,XMU,XSIG) IF(RN.LE.FOFX) GO TO 126 EXMU=(X6+X8)/2. EXSIG = (X8 - X6)/6.GO TO 7000 EXMU=(X9+X6)/2. EXSIG=1.3*(X5-X9) GO TO 7000 126 X7 = (X5 + X2)/2. 121 NR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X7,XMU,XSIG) IF(RN.LE.FOFX) GO TO 127 X8=(X6+X2)/2. NBR=NBR+1 NBRENDETT CALL UNIF(RN,NU) FOFX=XNCDF(X8,XMU,XSIG) IF(RN.LE.FOFX) GO TO 128 X9=(X6+X4)/2. NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X9,XMU,XSIG) IF(RN.LE.FOFX) GO TO 129 EXMU=(X6+X9)/2. EXSIG=1.3*(X9-X6) GO TO 7000 EXMU=(X8+X6)/2. 129 EXSIG=(X6-X8)/6.TO 7000 GO X9 = (X7 + X2)/2. 128

	NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X9,XMU,XSIG)
	IF(RN.LE.FOFX) GO TO 130 EXMU=(X2+X8)/2. EXSTG=(X8-X2)/6.
130	GD TD 7000 EXMU=(X9+X2)/2. EXSIG=1.3*(X2-X9) GD TD 7000
127	EXMIJ=(X7+X2)/2. EXSIG=1.3*(X2-X7)
5561	GO TO 7000 X6=2.*A-X5 NBR=NBR+1
	CALL UNIF(RN,NU) FOFX=XNCDF(X6,XMU,XSIG) IF(RN.LE.FOFX) GO TO 5560
	XB=X5 DEL X= X5-A E XMU= XB+DEL X/2.
5560	EXSIG=1.3*DELX GD TO 7000 XB=X5
2200	DELX=A-X6 EXMU=XB-DELX/4.
9501	EXSIG=6*DELX GU TO 7000 X3=(A+X2)/2.
	NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X3,XMU,XSIG)
	IF(RN.LE.FOFX) GO TO 9503 X4=(X1+X2)/2. NBR=NBR+1
	CALL UNIF(RN, NU) FOFX=XNCDF(X4,XMH,XSIG) IF(RN.LE.FOFX) GO TO 9504
	X5=2.*X1-X4 NBR=NBR+1
	CALL UNIF(RN,NU) FOFX=XNCDF(X5,XMU,XSIG) IF(RN.LE.FOFX) GO TO 9080
	XB=X5 DELX=XB-X1 EXMU=XB+DELX/4.
9080	EXSIG=6*DELX GD TO 7000 XB=X2
9080	DELX=X4-X2 EXMU=XB+DELX/2.
9504	
	NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X5,XMU,XSIG)
	IF(RN.LE.FOFX) GO TO 9081 X6=(X2+X4)/2. NBR=NBR+1
	CALL UNIF(RN,NU) FOFX=XNCDF(X6,XMU,XSIG) IF(RN.LE.FOFX) GO TO 9082
	X7=2.*X4-X5 NBR=N3R+1
	CALL UNIF(RN,NU) FOFX=XNCDF(X7,XMU,XSIG) IF(RN.LE.FOFX) GO TO 9083
	XB=X7 DELX=X7-X4 EXMU=XB+DELX/4.
	EXSIG=6*DELX

9033	DELX = X6 - X2
9032	EXMU=XB+DELX/2. EXSIG=1.3*DELX GD TD 7000 EXMU=(X5+X2)/2.
9081	EXSIG=(X2-X5)/6. GO TO 7000 X6=(X3+A)/2. NBR=NBR+1
	CALL UNIF(RN,NU) FOFX=XNCDF(X6,XMU,XSIG) IF(RN.LE.FDFX) GO TO 9084 EXMU=(X3+X5)/2. EXSIG=(X5-X3)/6.
9094	GD TO 7000 X7=2.*A-X6 NBR=NBR+1
	CALL UNIF(RN,NU) FOFX=XNCDF(X7,XMU,XSIG) IF(RN.LE.FOFX) GO TO 9085 XB=X6 DELX=X3-X6
9085	EXMU=XB+DELX/2. EXSIG=1.3*DELX GD TO 7000 XB=X7
0.5.00	DELX=A-X7 EXMU=XB-DELX/4. EXSIG=6*DELX GD_T0_7000
9503	X4=(X3+A)/2. NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X4,XMU,XSIG)
	IF(RN.LE.FOFX) GD TO 9507 X5=(X2+X3)/2. NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X5,XMU,XSIG)
	IF(RN.LE.FOFX) GO TO 9509 X6=2.*X2-X5 NBR=NBR+1 CALL UNIF(RN,NU)
	FOFX=XNCDF(X6,XMU,XSIG) IF(RN.LE.FOFX) GO TO 9510 XB=X6 DELX=X6-X2
9510	EXMU=XB+DELX/4. EXSIG=6*DELX GD TO 7000 XB=X3
	DELX=X5-X3 EXMU=XB+DELX/2. EXSIG=1.3*DELX GD TO 7000
9509	X6=(X3+X4)/2. NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X6,XMU,XSIG)
	IF(RN.LE.FDFX) GO TO 9511 FXMU=(X6+X3)/2. EXSIG=(X3-X6)/2. EXSIG=2.*FXSIG
9511	EXSIG=EXSIG/6. GD TD 7000 EXMU=(X4+X6)/2. EXSIG=(X6-X4)/2.
	EXSIG=2.*EXSIG EXSIG=EXSIG/6. GD TO 7000

-

9507	X5=(X4+A)/2. NBR=NBR+1 CALL UNIF(RN,NU) FOFX=XNCDF(X5,XMU,XSIG) IF(RN.LE.FOFX) GO TO 9508 EXMU=(X4+X5)/2. EXSIG=(X4-X5)/2. EXSIG=2.*EXSIG EXSIG=EXSIG/6.
9508	GD TD 7000 EXMU=(X5+A)/2. EXSIG=(X4-X5)/2. EXSIG=2.*EXSIG EXSIG=EXSIG/6. GD TD 7000
7000	XB=0. DEL X=0. WR ITE(6,1004) FXMU,EXSIG IF(EXSIG.LT.0.) EXSIG=-EXSIG OP T=0. DIF=0. XINC=0. OP T=EXMU-4.*EXSIG IF(OPT.LT.4) GO TO 1003 XINC=(OPT-A)/EXSIG INC=XINC/1 DIF=XINC-INC IF(DIF.GE.5) INC=INC+1 IF(DIF.LT.5) INC=INC
1003	GO TO 1001 A=OPT
1001 33	INC=0 M=IQ+INC+1 IS=70-NBR
	M=IQ+INC+1
	M=IQ+INC+1 CONDUCT BRUCETON TEST
	CONDUCT BRUCETON TEST ARRAYS DD 10 I=1,200 X(I)=0. IXD(I)=0 IXX(I)=0 NS(I)=0 NG(I)=0 SUMAR=0. SUMBR=0. AR(I)=0. BR(I)=0.
10	CONDUCT BRUCETON TEST ARRAYS DO 10 I=1,200 X(I)=0. IXD(I)=0 IXX(I)=0 NS(I)=0 NG(I)=0 SUMAR=0. SUMBR=0. AR(I)=0. BR(I)=0. CONTINUE
10	CONDUCT BRUCETON TEST ARRAYS DD 10 I=1,200 X(I)=0. IXD(I)=0 IXX(I)=0 NS(I)=0 NG(I)=0 SUMAR=0. SUMBR=0. AR(I)=0. BR(I)=0.
10 LOAD X 20	CONDUCT BRUCETON TEST ARRAYS DO 10 I=1,200 X(I)=0. IXD(I)=0 IXX(I)=0 NS(I)=0 NG(I)=0 SUMAR=0. SUMBR=0. AR(I)=0. CONTINUE ARRAY DO 20 J=1,200 X(J)=A+(J-1)*EXSIG

PERFORM BRUCETON ANALYSIS

RESPONSES AND NON-RESPONSES COUNT ISUMX=060 ISUM0=0 DO 14 J=1,200 ISUMX=ISUMX+IXX(J) ISUMO=ISUMO+IXO(J) NS(J) = 0AR(J) = 0. BR(J)=0. NG(J)=0 CONTINUE 14 DETERMINE LESS FREQUENT EVENT AND IF(ISUMX.LE.ISUMO) GO TO 15 LOAD NS NT=ISUMO IFLAG=0 DD 21 J=1,200 NS(J)=IXO(J) CONTINUE 21 GO TO 16 NT=ISUMX 15 IFLAG=1 DD 22 J=1,200 NS(J)=IXX(J) CONTINUE 22 DETERMINE FIRST AND SECOND MOMENTS 16 JCOUNT=1 IF(NS(JCOUNT).GT.O) GO TO 18 JCOUNT=JCOUNT+1 IF(JCOUNT.GF.200) GD TO 104 GO TO 17 17 MCOUNT=200-JCOUNT 18 DO 19 J=1, MC OUN'T NG(J)=NS(JCOUNT+J-1) AR(J)=(J-1)*NG(J) SUMAR = SUMAR + AR(J) BR(J) = ((J-1) **2) *NG(J) SUMPR = SUMAR + BR(J) CONTINUE 19 YPRIME=X(JCOUNT) ATE ESTIMATES OF MEAN AND STANDARD DEVIATION IF(IFLAG.FQ.O)XMUEST=YPRIME+EXSIG*((SUMAR/NT)+(1./2.)) IF(.NOT.IFLAG.EQ.O)XMUEST=YPRIME+EXSIG*((SUMAR/NT)-(1. SIGFAC=((NT*SUMBR)-(SUMAR**2))/(NT**2) IF(SIGFAC.GT..3) GO TO 1000 EMU(LCOUNT)=0. CALCULATE EDEV(LCOUNT)=0. NOGO=NOGO+1 GO TO 104 1000 DEVEST=1.62*EXSIG*(SIGFAC+.029) LOAD EMU AND EDEV EMU(LCOUNT) = XMUEST - XMU EDEV(LCOUNT)=DEVEST-XSIG ADDMU=ADDMU+EMU(LCOUNT) ADDSIG=ADDSIG+EDEV(LCOUNT) ADDMUQ=ADDMUQ+EMU(LCOUNT)**2 ADDSDQ=ADDSDQ+EDEV(LCOUNT)**2 IF(EMU(LCOUNT).LT.O.) GO TO 91 IF(EMU(LCOUNT).FQ.O.) GO TO 92 IMUHI=IMUHI+1 IF(EMU(LCOUNT).GT.HIMU) HIMU=EMU(LCOUNT) IF(.NOT.EMU(LCOUNT).GT.HIMU) HIMU=HIMU GO_TO_93 92 NOMU=NOMU+1 GO TO 93 91 IMULD=IMULO+1 IF(EMU(LCOUNT).LT.SMLO) SMLO=EMU(LCOUNT)

IF(.NOT.EMU(LCOUNT).LT.SMLO) SMLD=SMLO IF(EDEV(LCOUNT).LT.O.) GO TO 94 IF(EDEV(LCOUNT).EO.O.) GO TO 95 IDEVHI=IDEVHI+1 IF(EDEV(LCOUNT).GT.DEVHI) DEVHI=EDEV(LCOUNT) IF(.NOT.EDEV(LCOUNT).GT.DEVHI) DEVHI=DEVHI GO TO 104 93 95 NODEV=NODEV+1 GO TO 104 IDEVLO=IDEVLO+1 94 IF(CDEV(LCOUNT).LT.DEVLO) DEVLO=EDEV(LCOUNT) IF(.NOT.EDEV(LCOUNT).LT.DEVLO) DEVLO=DEVLO 104 JCOUNT=0 SIGFAC=0. XMUFST=0. DEVEST=0. SUMAR=0. SUMBR=0. LCOUNT=LCOUNT+1 HAVE 1000 EXPERIMENTS BEEN CONDUCTED ? IF(LCOUNT.LT.1001) GO TO 103 IF EXPERIMENTS COMPLETED CALCULATE AND WRITE PESULTS EXNOGO=NOGO SAMAVM=ADDMU/(1000.-EXNOGO) SAMAVD=ADDSIG/(1000.-EXNOGO) SAMSQM=ADDMUQ/(929.-EXNOGO) SAMSOD=ADDSOQ/(999.-EXNOGD) IF(IANY.EQ.1) GD TO 35 IANY=IANY+1 GD TO 69 35 STOP END SUBROUTINE UNIF(RN, NU) SUBROUTINE RETURNS RANDOM NUMBER UNIFORM ON (0,1). REAL MOD MOD= 2**31 NR=129*NU+1 RN=NR/MOD IF(RN.LT.0.0) RM=-RN NU=NP RETURN END

FUNCTION XNCDF(V,XMU,SX)

FUNCTION SUBPROGRAM CALCULATES CUMULATIVE NORMAL. X IS AN R.V. WITH MEAN, XMU, AND STANDARD DEVIATION, SX. ARG=(V-XMU)/SX XNCDF=SNCDF(ARG) RETURN END

FUNCTION SNODE(X)

FUNCTION SUBPROGRAM CALCULATES STANDARD CUMULATIVE NORMAL. DATA TEST/0.0/ IF(TEST.NE.0.0) GO TO 100 SR2= SORT(2.0) TEST=1. 100 SNCDF=(1.0+ERF(X/SR2))/2.0 RCTURN END

.

-

BIBLIOGRAPHY

- 1. Boyars, C. and Levine, D., "Drop-Weight Sensitivity Testing of Explosives", Pyrodynamics, v. 6, p. 54, 1968.
- Dixon, W. J., and Mood, A. M., "A Method for Obtaining and Analyzing Sensitivity Data", <u>Journal of the American Statistical</u> Association, v. 43, p. 109-126, 1948.
- Tysver, J. B., <u>A Binary Search Procedure for Use in Sensitivity</u> <u>Testing</u>, submitted to a technical journal for publication, U. S. N. Postgraduate School, Monterey, California, July 1970.
- Naval Ordnance Laboratory Technical Report 66-117, Monte Carlo Investigations of Small Sample Bruceton Tests, by L. D. Hampton, p. 3.

INITIAL DISTRIBUTION LIST

		No. (Copies
1.	Defense Documentation Center Cameron Station Alexandria, Virginia 22314		2
2.	Library, Code 0212 Naval Postgraduate School Monterey, California 93940		2
3.	Associate Professor J. B. Tysver, Code 55Ty Department of Operations Analysis Naval Postgraduate School Monterey, California 93940		1
4.	Major Donald L. Hicks, USMC 20 Mesa Vista Drive Boise, Idaho 83705		1
5.	Library, Department of Operations Analysis Naval Postgraduate School Monterey, California 93940		1

42 ·

Δ.

e



Security Classification

DOCUMENT CONTROL DATA - R & D

(Security classification of title, body of abstract and indexing annotation must be entered when the overall report is classified)
IGINATING ACTIVITY (Corporate author)
28. REPORT SECURITY CLASSIFICATION

Naval Postgraduate School Monterey, California 93940

Unclassified 26. GROUP

3 REPORT TITLE

An Evaluation of a Modified Binary Search Procedure for Use with the Bruceton Method in Sensitivity Testing

4. DESCRIPTIVE NOTES (Type of report and inclusive dates)

Master's Thesis; September 1970

5. AUTHOR(S) (First name, middle initial, last name)

Donald Lee Hicks

6. REPORT DATE	78. TOTAL NO. OF PAGES	76. NO. OF REFS
September 1970	42	4
BE. CONTRACT OR GRANT NO.	98. ORIGINATOR'S REPORT NU	JMBER(S)
b. PROJECT NO.		
с.	96. OTHER REPORT NO(S) (Any this report)	y other numbers that may be assigned
d.		
10. DISTRIBUTION STATEMENT		

This document has been approved for public release and sale; its distribution is unlimited.

11. SUPPLEMENTARY NOTES	12. SPONSORING MILITARY ACTIVITY	
	Naval Postgraduate School	
13. ABSTRACT	Monterey, California 93940	

Two methods of obtaining sensitivity data were simulated on an electronic computer for the purpose of comparing the accuracy of the estimates of the parameters of an underlying cumulative normal response function. The first method simulated the standard Bruceton procedure while the second used a modified binary search routine with a portion of the sample in order to obtain maximum likelihood estimates of the input parameters for use in a follow-on Bruceton test.

The results showed both methods to be effective in estimating the mean but with slightly more variability in the estimates obtained by the second procedure. Both methods underestimated the standard deviation again with more variability in the estimates obtained by the second procedure. When the prior parameter estimates were unknown and the applicable stimulus level bounded, the second method yielded estimates favorably comparable to those expected from the Bruceton procedure with suitable prior input estimates.

43

Security Classification

.

.

KEY WORDS	LIN			кв	LIN	ĸ c
	 ROLE	ΨT	ROLE	wτ	ROLE	ΨT
Sensitivity testing						
Bruceton method						
Maximum likelihood estimates						
Computer simulation						
			-			
FORM 1473 (BACK)	 -					

Th Thesis H52687 Hicks c.1

not ic

121710

An evaluation of a modified binary search procedure for use with the Bruceton method in sensitivity testing.

Thesis H52687 c.1

H

52

c.

121710

23456

Hicks An evaluation of a modified binary search procedure for use with the Bruceton method in sensitivity testing.

