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**NAVAL
POSTGRADUATE
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MONTEREY, CALIFORNIA

THESIS

**DYNAMIC RESPONSE OF SOLDERED ELECTRONIC
COMPONENTS UNDER IMPACT LOADING**

by

Andrew Calvin Wood

December 2011

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**DYNAMIC RESPONSE OF SOLDERED ELECTRONIC COMPONENTS
UNDER IMPACT LOADING**

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Submitted in partial fulfillment of the
requirements for the degree of

MASTER OF SCIENCE IN MECHANICAL ENGINEERING

from the

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ABSTRACT

The objective of this research was to analyze the effects of impact loading on electronic component failure. A standard fiberglass composite printed circuit board (PCB) card was used in two impact tests. The first test consisted of a PCB card with four adhered strain gauges, which were mounted inside an aluminum box fabricated for testing. Impact testing was conducted with weights ranging from 0 to 30 lb., and the corresponding strain values were recorded. For the second set of impact tests, a new circuit card was mounted inside the aluminum box. The new circuit card maintained the same dimensions, but no strain gauges were attached. Solder joints were placed at nine different locations on the card, and testing was conducted to determine the impact load at solder joint failure. Both visual and resistance inspections were conducted after each impact. After seven drop tests were conducted, no failure had been detected. This lack of failure was attributed to the rigidity and substantial nature of the aluminum box used in testing. Upon completion of both impact tests, two Finite Element Method (FEM) models were built. The first FEM model represented a scaled version of the PCB card, four solder joints, and a silicon computer chip. Strain data from the PCB card testing was input into the model, and a corresponding solder joint strain was calculated. The second FEM model was a full-scale version of the aluminum box and mounted circuit card. A force was applied to the box, and the various strains were recorded on the PCB card. The collection of this data has helped to establish a valuable relationship between the strains in PCB cards and solder joints, and it will increase the understanding of electronic component failure under impact loading conditions.

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LIST OF ACRONYMS AND ABBREVIATIONS

Ag	Element symbol for silver
Al	Element symbol for aluminum
BGA	Ball-Grid Array
CAD	Computer Aided Design
Cu	Element symbol for copper
ε	Strain (mm/mm)
$\mu\varepsilon$	Microstrain (mm/mm)
FEM	Finite Element Method
ft	Feet
kN	Kilonewton
IED	Improvised Explosive Device
in	Inches
kg	Kilogram
l	Length
lb.(s)	Pound(s)
MPa	Megapascal
mm	Millimeters
ms	Milliseconds
Pb	Element symbol for lead
PCB	Printed Circuit Board
PGA	Pin-Grid Array
s	Seconds
Si	Element symbol for silicon
Sn	Element symbol for tin

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I. INTRODUCTION

A. BACKGROUND

The vast majority of failures in electronic equipment are due to failures in the solder joint that connects the electronic component to the printed circuit board (PCB). With the increased use of improvised explosive devices (IED), we have seen failure of electronic components in many military applications [1]. Often, the boxes or cases holding these components withstood the blast impact without failure. However, the failure is found to be occurring at the solder joint interface between the component itself and PCB mounted inside the equipment box or case.

Similar results have been seen in Naval application when ships have impacted underwater obstructions or have been in close proximity to an underwater explosion. The integrity of the ship and its equipment housings remains intact, but the solder joints attaching the electronic components to the PCB cards are failing. Therefore, continued research on the effect of impact and shock loading on electronic component failure is beneficial to the design of electronic equipment and the formulation of a criterion for predicting failure of solder joints.

1. Ground Combat Application

The wars in Iraq and Afghanistan reveal vulnerabilities in U.S. Armed Forces defenses against IEDs. As a result, building and designing war fighting equipment to withstand IEDs has become a high priority. Military vehicles and equipment are now able to withstand much greater impact forces due to close range explosions caused by IEDs. However, failure is still occurring in the onboard electronic equipment due to the shock and impact forces resulting from the explosion [1]. More specifically, failure is occurring at the PCB card and solder joint interface of individual electronic components. The vehicles and the boxes holding the PCB cards are remaining intact, but the components themselves are breaking free from their soldered mounts.

2. Maritime Combat Application

Where ground forces face the challenge of overcoming IEDs and the damage they inflict on equipment and personnel, the Navy is exposed to an entirely different set of threatening devices. Underwater mines and torpedoes each have the ability to inflict catastrophic damage to a ship and its crew. In addition, uncharted sea mounts and shoal water present very real threats to the structural integrity of a war ship. To improve design and survivability, one ship from each class of war ship will normally undergo shock trials. The data gathered from each shock test provides valuable information to ship designers and engineers on how to improve the survivability of that vessel. However, despite the advancements made in structural integrity and survivability following an underwater explosion or impact, electronic components are still experiencing failure at the PCB card and solder joint interface.

B. LITERATURE SURVEY

1. Vibration Effects on Solder Joint Failure

Military environments expose war fighting equipment to numerous sources of harmful vibrations. Over time, these vibrations cause failure at the PCB card and solder joint interface. Though military grade equipment is often built to withstand these harsh conditions, many of the components used are commercial-off-the-shelf (COTS). Celik and Genc [1] state that the life expectancy of military grade electronics is 20 years, but COTS electronics will only last 7 to 10 years.

Attempts have been made to reduce the effects of these harmful vibrations by implementing vibration isolators. Though widely accepted as a solution to the problem of premature solder joint failures due to vibration, Celik and Genc [1] argue that these isolators have significant drawbacks. Their research suggests that the silicone used to isolate the component to the PCB card is not appropriate for high temperature environments. In addition, the adhesive will stiffen the component and cause excess flexural stresses. Lastly, manufacture and repair are often cost prohibitive.

Celik and Genc [1] conducted vibration testing on axial leaded capacitors. They found that the components could withstand more vibration as solder joint diameter

increased. Also, the length and width of the card had a direct effect on a components life span. As the width of the PCB card increased and the length decreased, the components saw a higher failure rate.

Celik and Genc [1] concluded that more computer simulation needs to be conducted on electronic components prior to their introduction into the fleet. Significant problems can be addressed through a computer modeling program long before it fails in combat application. COTS electronic components have a life expectancy that is half that of their military counterparts. However, sufficient simulation and testing is the first step in fixing the problems caused by premature solder joint failure due to vibration.

2. Varying Strain Rates and Solder Joint Failure

Luteran [2] focused his research in the area constant and varying strain rates and their effect on solder joint reliability. He conducted uniaxial testing to investigate the mechanical behaviors of a solder joint under single and varying strain rate loading. He determined that the elastic modulus of all test samples decreased as strain rate increased. Conversely, he found that yield and ultimate strengths increased as a result of an increased strain rate. It was also noted the fracture strains, ultimate strengths, and total strain energy densities had higher values when tested with a fast strain rate followed by a slow strain rate. A slow strain rate followed by a fast strain rate resulted in lower fracture strains, ultimate strengths, and total strain energy densities. Luteran's [2] research and experimentation led to the establishment of a failure criteria for lead free solder joints under varying strain rates.

Boyce et al. [3] studied the thermomechanical strain rate sensitivity of Sn-Pb solder over a wide range of strain rates. Failure rates occurred between 1 ms and 1 hr. They concluded that the standard Johnson-Cook constitutive model for strain rate sensitivity was insufficient for representing observed behavior. Boyce et al. [3] determined that a unified creep plasticity formulation offers an improved representation of the observed behavior. They also concluded that there was an absence of significant internal grain rotation, and that it consistent at all strain-rates.

3. Drop Impact Analysis on Sn-Ag-Cu Solder Joints

Pang and Che [4] discuss the complexities of drop test analysis and the dangers of over simplifying Sn-Ag-Cu solder joint deformation response. Solder joint failure is a combination of fatigue crack growth and brittle fracture of the intermetallic interfaces. Oversimplification can lead to a misunderstanding of the actual cause of failure due to drop impact testing. Pang and Che [4] use a split Hopkinson pressure bar (SHPB) test system to study the solder joint failure due to impact loading.

Pang and Che [4] argue that during drop testing, dynamic hardening will occur in the Sn-Ag-Cu solder joint. This hardening will cause the yield stress to rise several times higher than the nominal yield stress in the Sn-Ag-Cu solder joint. This increase in dynamic strength will cause strain cycling in the material and potentially lead to premature fatigue failure. Conversely, if the impact loading is excessive, impact failure strength of the intermetallic surface can lead to brittle failure.

Pang and Che [4] used multiple components in testing, and concluded that BGA components had the highest failure rate. They concluded that the strain rate effect had a large influence on the Sn-Ag-Cu solder joint reliability, and that lead free solder had a higher failure rate than the solder with lead.

C. OBJECTIVE OF STUDY

The objective of this study is to examine the strain in the PCB card and its solder joints, as a result of impact loading, in order to better understand failure in electronic components. Due to their small size and inaccessibility, it is impractical and cost prohibitive to directly mount strain gauges to many solder joints. Upon completion of impact testing for strain in the PCB card, this study will attempt to establish a relationship between the strains in the PCB card and the corresponding solder joint. A FEM model representing a small cutout of the PCB card, four solder joints, and mounted silicon processing chip will help to provide the data required to verify this relationship.

In addition, this study will use further impact testing to establish a relationship between impact loading and solder joint failure. A second FEM model, a full-scale representation of the aluminum (Al) box and mounted circuit card, will be used to verify

failure results. Once a relationship is established, this model will provide researchers with an efficient means of modifying the box design. Quick and efficient modifications to the computer model will help to determine how dimensional changes to the box affect solder joint reliability.

Chapter II of this thesis describes the experimental impact testing for both strain and solder joint failure. Chapter III introduces two FEM models representing a section of the PCB card, solder joint and silicon chip, as well as the full-scale model of the Al box and mounted PCB card. Chapter IV addresses the behaviors of both lateral and longitudinal strain in the PCB card in addition to providing an analysis of both FEM models. Chapter IV will also explore the relationship between the stresses in both the PCB card and its corresponding solder joints. Chapter V will consist of both conclusions and any furthering research recommendations.

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II. EXPERIMENTAL

A. IMPACT TESTING FOR STRAIN

1. Drop Weight Vertical Impact Test Apparatus

The impact test platform used for both experimental studies was a Drop Weight Vertical Impact Test Apparatus pictured in Figure 1. The test rig consisted of a drop weight with a 7.6 x 7.6 cm steel base, approximately 1.9 cm thick. The drop weight allowed up to 30 lb. of added weight to be bolted to the apparatus. The drop weight was raised to a height of 91.4 cm above the Al box. Upon release, the drop weight would fall vertically and impact the Al box. Four guide rods with linear bearings insured a uniaxial loading of the Al box upon impact. The test rig frame was constructed from an Al alloy.

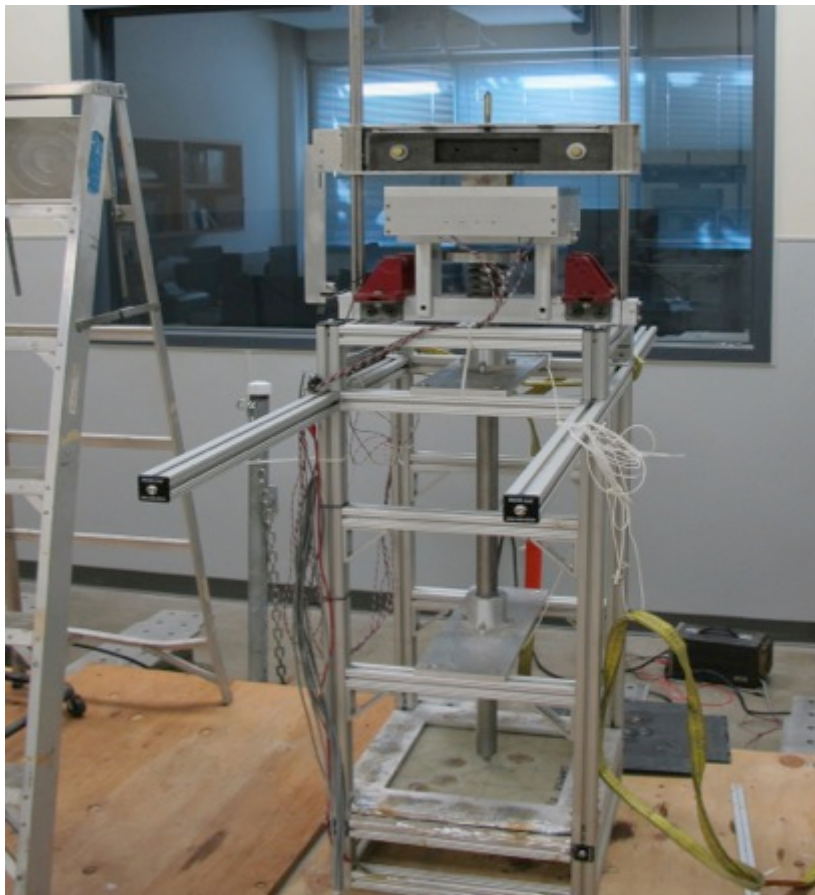


Figure 1. Drop weight vertical impact test apparatus.

The Al box was designed and built to withstand repeated impacts without failure. The box top dimensions are 27.9 x 27.9 cm with a thickness of 1.9 cm. The sides are all 10.2 cm tall with a thickness of 1.3 cm. The box is mounted to the test rig by way of two vertical supports and four set screws. The drop weight is designed to impact the exact center of the box top.

2. Data Collection

Data collection for all impact testing was conducted using LabVIEW™. Prior to impact, a vertical trigger mechanism passes through a sensor and starts a data recorder. 1,000 samples of strain data are recorded over a 0.1 s time period. The software is set to record at 10,000 Hz. Figure 2 and Figure 3 show the vertical trigger mechanism and the sensor.

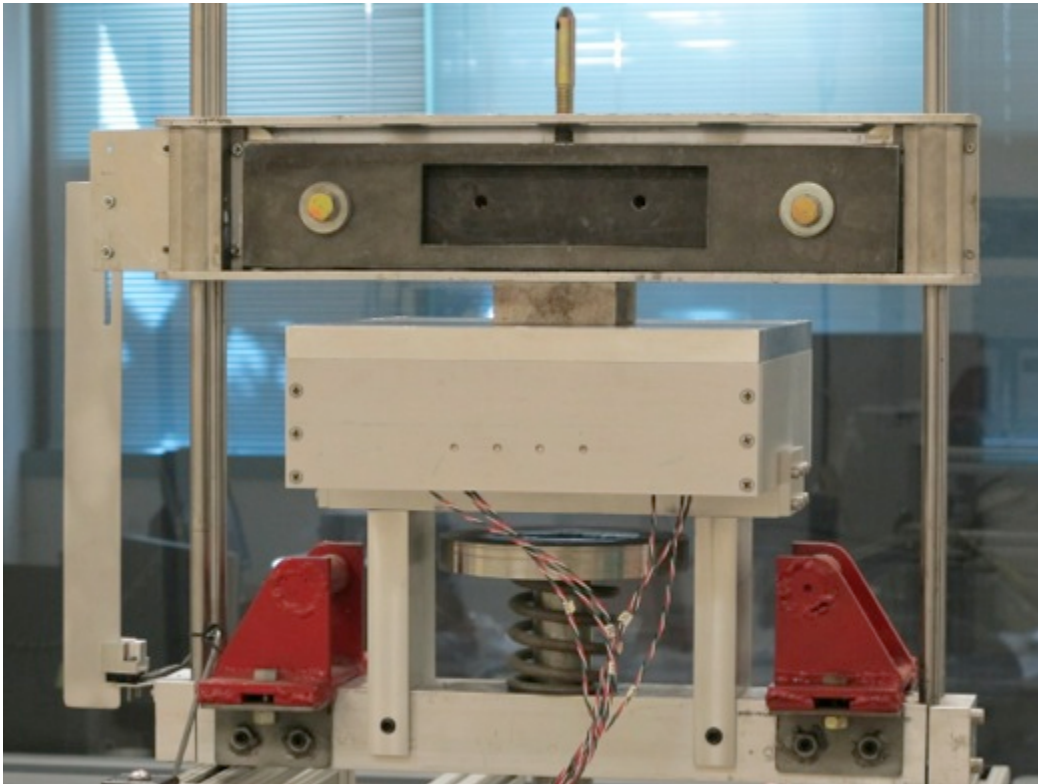


Figure 2. Drop weight and Al box.



Figure 3. Trigger mechanism and sensor.

3. Strain Gauges

The strain gauges used in both impact tests were three element, 45° rosettes shown in Figure 4. The three readings collected from the elements are referred to as gauge strain. The gauge strain must then be converted into principal strain by means of the following transformation equations [5]:

$$\varepsilon_y = \frac{\varepsilon_1 + \varepsilon_3}{2} + \frac{1}{\sqrt{2}} \sqrt{(\varepsilon_1 - \varepsilon_2)^2 + (\varepsilon_2 - \varepsilon_3)^2}$$

$$\varepsilon_x = \frac{\varepsilon_1 + \varepsilon_3}{2} - \frac{1}{\sqrt{2}} \sqrt{(\varepsilon_1 - \varepsilon_2)^2 + (\varepsilon_2 - \varepsilon_3)^2}$$

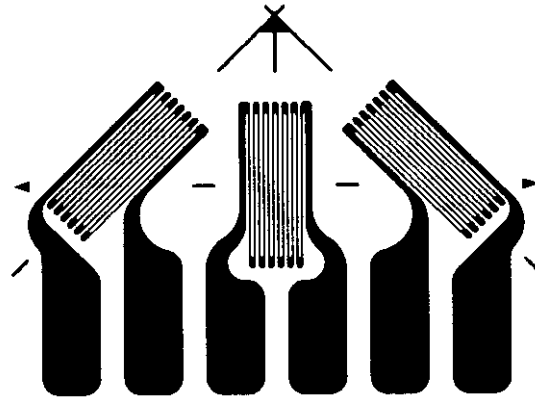


Figure 4. Rectangular, three element 45° rosette (After [6]).

The strain gauges are mounted on the PCB card 90° from positioning shown in Figure 4. This orientation will allow the center strain gauge element to align itself with the x-axis. Therefore, ε_2 is equal to ε_x . Figure 5 pictures the strain gauges mounted to the PCB card and wired for impact testing.

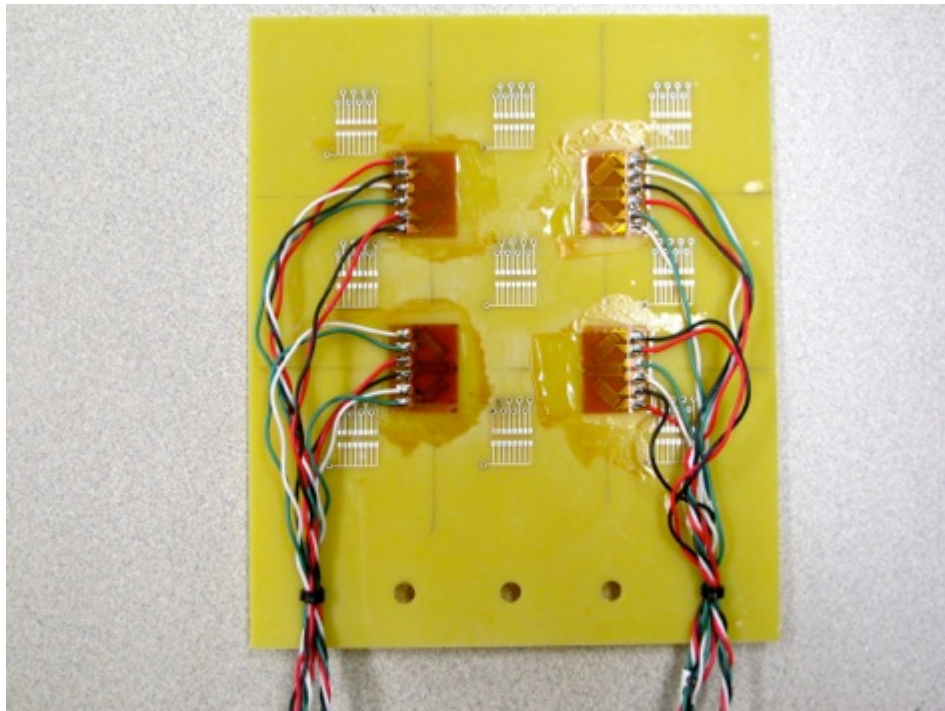


Figure 5. Strain gauges mounted on PCB card.

Figure 6 depicts the four quadrants, beginning with number 1 in the lower right and moving counter clockwise to number 4 in the lower left. The x-axis and y-axis will be referred to as the lateral and longitudinal axis, respectively. Each strain gauge was mounted in the center of its quadrant and numbered accordingly.

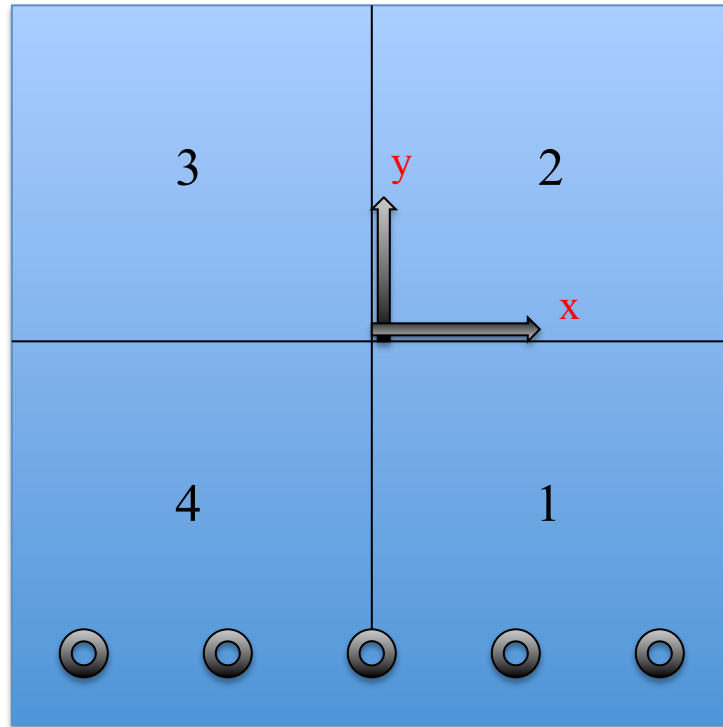


Figure 6. PCB card quadrant numbers.

4. Test Setup and Procedures

The impact test for strain required the PCB card with strain gauges to be mounted inside the Al box as shown in Figure 7. The PCB card was bolted to a small Al bracket, and the assembled PCB card and bracket were then secured to the Al box. This proved to be the most efficient means of switching the PCB cards used in testing. Securing the PCB card to the bracket required both a screw driver and an adjustable wrench to tighten the five bolts, washers and nuts. The Al bracket mounted to the Al box using four hex-head screws that were easily accessible from the bottom opening with an Allen wrench.

For each impact test, the drop weight was raised to a height of 91.4 cm above the Al box. The drop weight was held in place by a steel pin while the data collection was

prepared. Hearing protection and a safety observer were required at all times. A ladder was necessary to both insert and remove the steel pin used to hold the drop weight. Once the pin was removed, the drop weight would fall and trigger the sensor to collect strain data. Weight was added in 5 lb. increments, starting with no additional weight added and finishing with 30 lb. of weight added. Altogether, seven drop tests were conducted and strain data was collected for each.

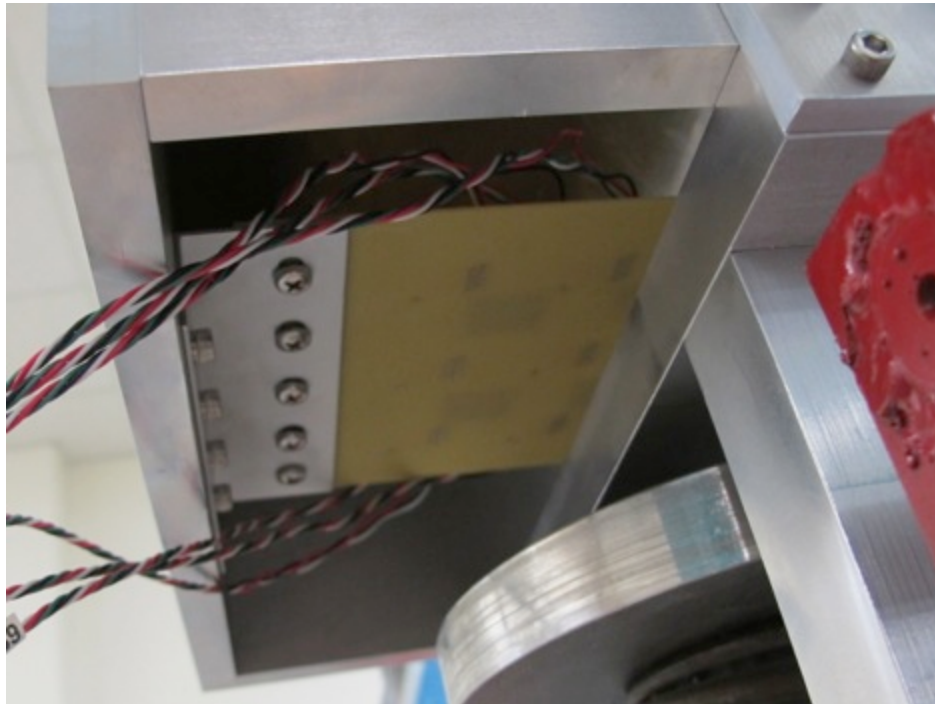


Figure 7. PCB card and Al bracket mounted for testing.

B. IMPACT TESTING FOR SOLDER JOINT FAILURE

1. Preliminary PCB Card Design with BGA Solder Joints

Determining solder joint failure is a difficult process due in part to the small size and location of each joint. Preliminary research was focused on the ball-grid array (BGA) solder joints manufacturing process, as many military applications have begun using BGA technology in the design and manufacture of their electronic components.

The traditional solder joint process is known as pin-grid array (PGA). PGA components have metal pins that must be fit into corresponding holes on the PCB card.

Once the pins have been aligned and pushed through the holes, they are soldered to the bottom side of the PCB card. The soldering connects the pins to connectors called traces. Traces are conductive paths embedded into the PCB card. Once secured and soldered in place, any excess metal wire on the pin is trimmed flush with the solder joint. Figure 8 depicts a typical PGA component.

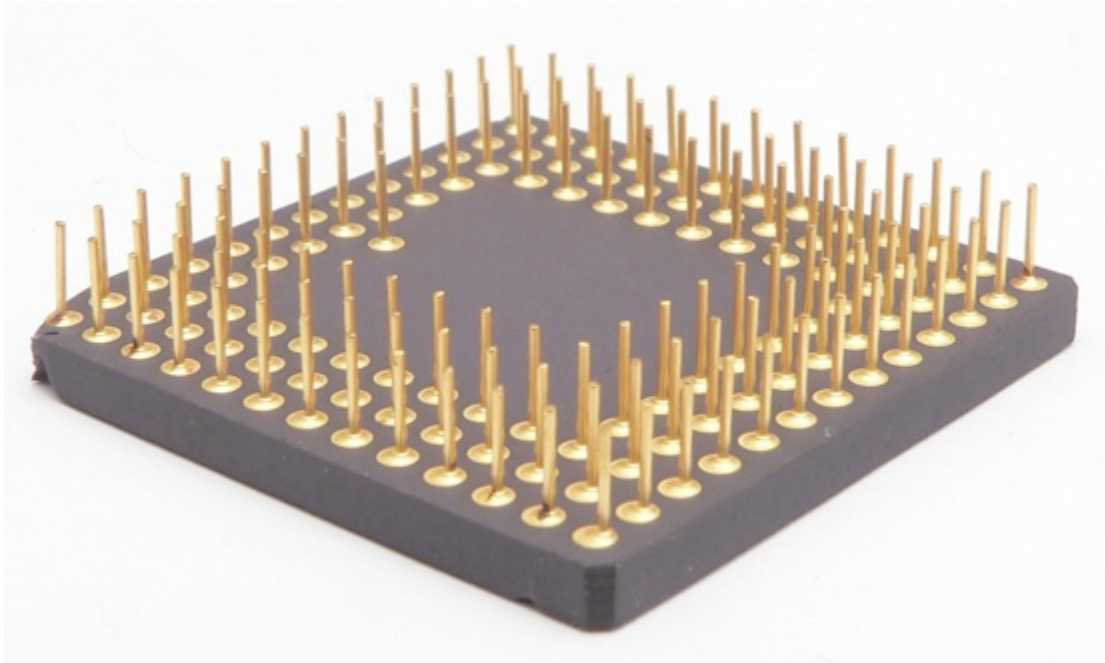


Figure 8. PGA component bottom view (After [7]).

BGA components allow for automated precision in the manufacturing process. Contact pads flush with the surface of the PCB card are connected to each of the traces. A BGA component will have corresponding contact pads on its bottom side. The automated process allows a machine to simultaneously lay an array of solder beads to each of PCB cards contact pads. The BGA component is then aligned and joined to the PCB card by way of the heating the solder beads. Figure 9 shows a standard BGA component prior to assembly.

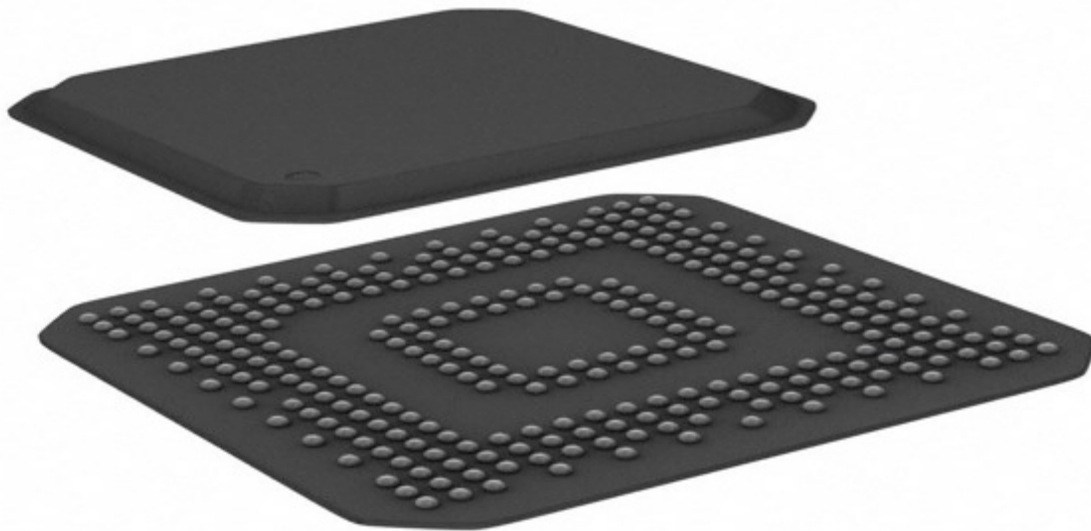


Figure 9. BGA component prior to assembly (After [8]).

The preliminary design for the circuit card used in testing for solder joint failure was to use a BGA component soldered to a standard PCB card. However, determining failure in the interior solder joints proved to be a difficult and labor-intensive process. In addition, it was cost prohibitive to design and build multiple BGA test cards.

2. Secondary PCB Card Design with Resistor Packs

In order to simulate the solder joint interface of a BGA component, the decision was made to design a test card using resistor packs with corresponding mounting pads embedded in the PCB card. The mounting pads connect to the traces on the PCB card, as shown in Figure 10. The traces from each mounting pad leads to an exposed test point on the PCB card. These test points allow the resistance to be measured across each resistor by use of a multimeter. This enables both a visual and resistance inspection to be conducted after each impact test.

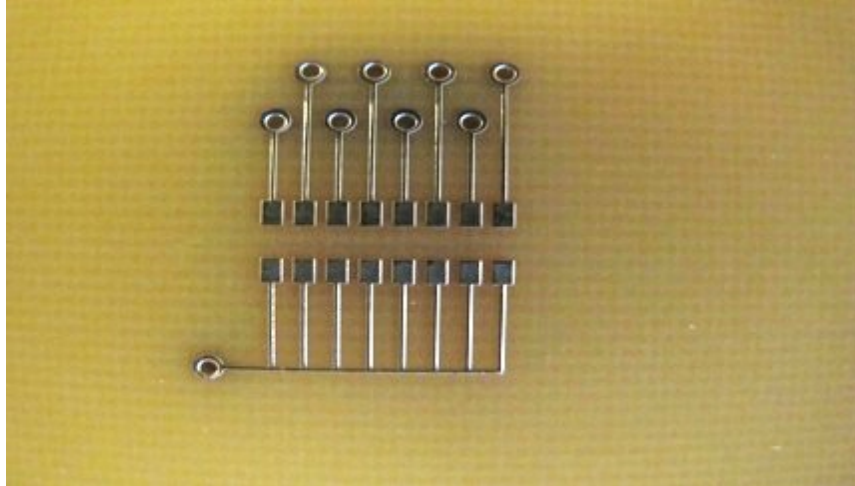


Figure 10. PCB card mounting pad w/o resistor pack.

However, after design and fabrication of the PCB card was complete, an insufficient number of resistor packs, similar to those in Figure 11, were available for procurement due to manufacturing constraints. The 10 PCB cards ordered required nine resistor packs each. A total of 90 resistor packs were required, but the manufacturer only possessed four resistor packs. Thus, a third testing design was necessary.

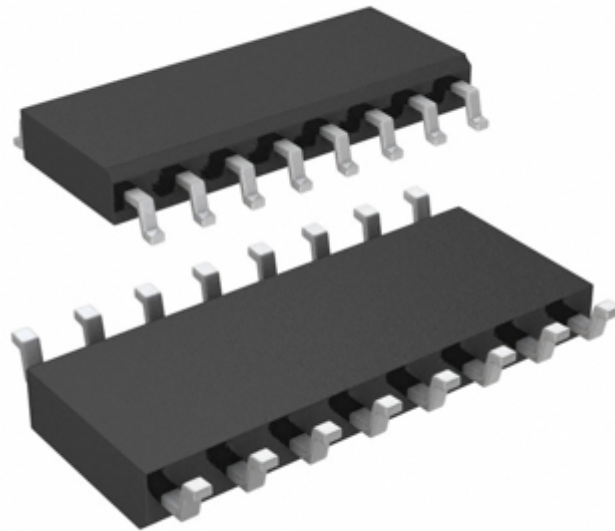


Figure 11. Resistor pack (After [9]).

3. Tertiary PCB Card Design with Soldered Bridge

A decision was made to proceed with the current PCB card with the resistor pack mounting pads. In order to test for solder joint failure, a ball of solder was welded across the resistor pack mounting pads embedded into the PCB card, as shown in Figure 12.

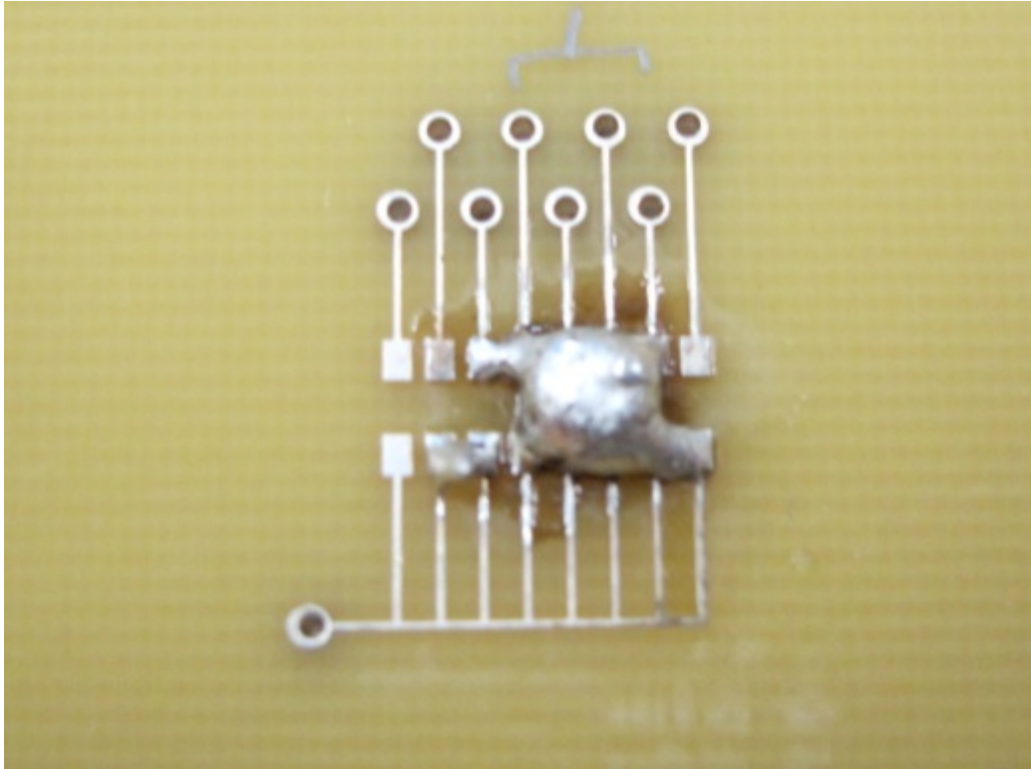


Figure 12. PCB card with soldered bridge.

This soldered bridge solution satisfied the requirement for both visual and resistance inspections to be conducted after each impact test.

4. Test Setup and Procedures

Impact testing for solder joint failure was conducted in a similar fashion to the impact testing for strain. The PCB card with nine soldered bridges was mounted to the Al bracket and in turn mounted inside the Al box, as shown in Figure 7. Weight was added in 5 lb. increments, starting with 0 lb. of weight added and finishing with 30 lb. of weight added. The PCB card was removed from the test platform after each impact test

and was visually inspected for solder joint failure. In addition, the resistance was measured and recorded across each test point. Figure 13 is a picture of the multimeter used for all resistance testing. Altogether, seven drop tests were conducted. Failure never occurred at the solder joint and PCB card interface, and the resistance measurements remained constant throughout each of the seven tests conducted. This lack of failure and degradation can be attributed to the rigidity and substantial nature of the Al box.



Figure 13. FLUKE™ multimeter.

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III. ANALYTICAL

A. FEM MODEL OF SOLDERED ELECTRONIC COMPONENT

An FEM model of a soldered electronic component was built in to order analyze the strain on the individual solder joints. Mounting a strain gauge to a solder joint was not practical do to size constraints. The resulting strain data from the FEM model will be used to validate a theoretical relationship between strains in the PCB card and solder joints. The model was built using SolidWorks™, an engineering CAD software. The model was analyzed using the FEM solver, ANSYS™. The ANSYS™ model shown in Figure 14 is a sample cutout of an electronic component soldered to a PCB card. The base of the model maintains the same material properties as a standard fiberglass composite PCB card. The four solder joints have a cylindrical shape and maintain the same material properties of lead free solder. The cubic feature joined to the top of the four solder joints represents a silicon processor and maintains silicon material properties.

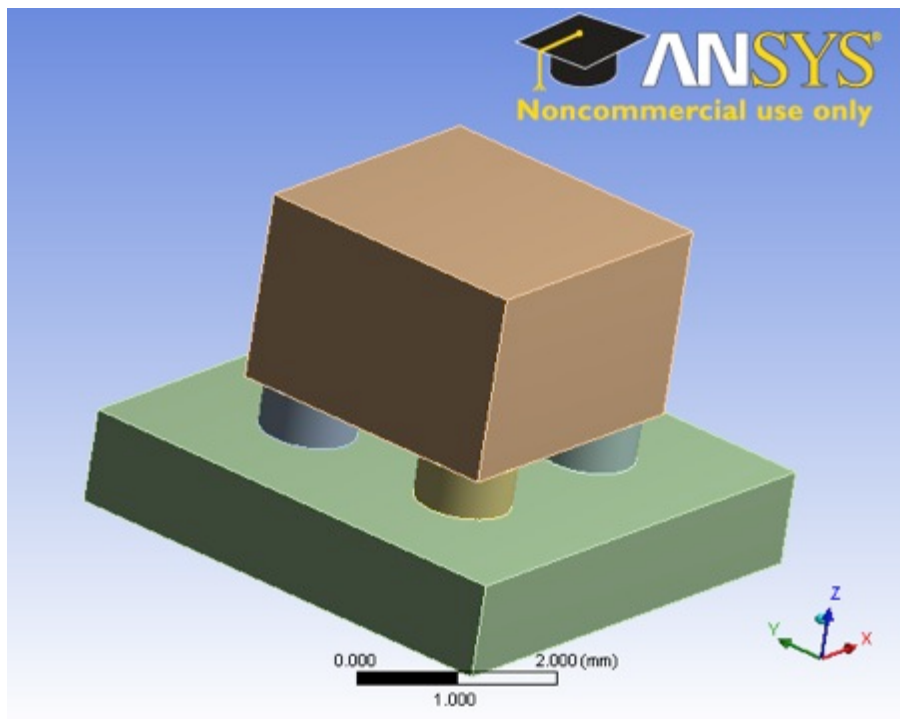


Figure 14. ANSYS™ FEM model of soldered electronic component.

Table 1 shows a list of each component and its material properties. Al is also included in the list, as it was used for the second FEM model of the Al box with mounted PCB card.

Component Parts	Young's Modulus (E) GPa	Poisson's Ratio (ν)	Density (ρ) kg/cm³
PCB Card	19.5	0.33	1985
Solder Joints	45	0.34	7500
Silicon Chip	165	0.22	2330
Al Alloy	71	0.33	2770

Table 1. FEM model component material properties.

The strain data collected from impact testing was applied to the FEM model by inserting a deformation in the longitudinal and lateral directions. Deformation was solved for using the definition of strain, where both strain and the original length in each axis were known.

$$\varepsilon = \frac{\Delta l}{l_0} = \frac{\text{deformation}}{\text{original length}}$$

Using strain data from the impact test with 30 lb. added weight, the peak values for strain were recorded in quadrant 4 from Figure 7. Table 2 shows the values for strain and original length that led to the corresponding deformation input for the FEM model. Table 3 gives the dimensions of each component in the soldered electronic component FEM model.

Axis	Strain ($\mu\epsilon$) mm/mm	Original length (l_0) mm	Deformation (Δl) mm
Longitudinal	11.6	5.0	5.8e-5
Lateral	1.12	5.0	5.6e-6

Table 2. FEM model deformation inputs.

Component	Length (l) mm	Width (w) mm	Height (h) mm	Diameter (d) mm
PCB Card	5.0	5.0	1.0	-
Solder Joints	-	-	0.5	1.0
Silicon Chip	3.0	3.0	2.0	-

Table 3. FEM model dimensions.

B. FEM MODEL OF BOX WITH MOUNTED PCB CARD

The second model built in SolidWorks™ was a full-scale version of the Al box, Al bracket and mounted PCB card. Figure 15 is a wire frame picture of the model in SolidWorks™ prior to analysis in ANSYS™. This view clearly shows the orientation and location of the Al bracket mounted inside the Al box. Figure 16 is a picture of the model following the strain analysis in ANSYS™.

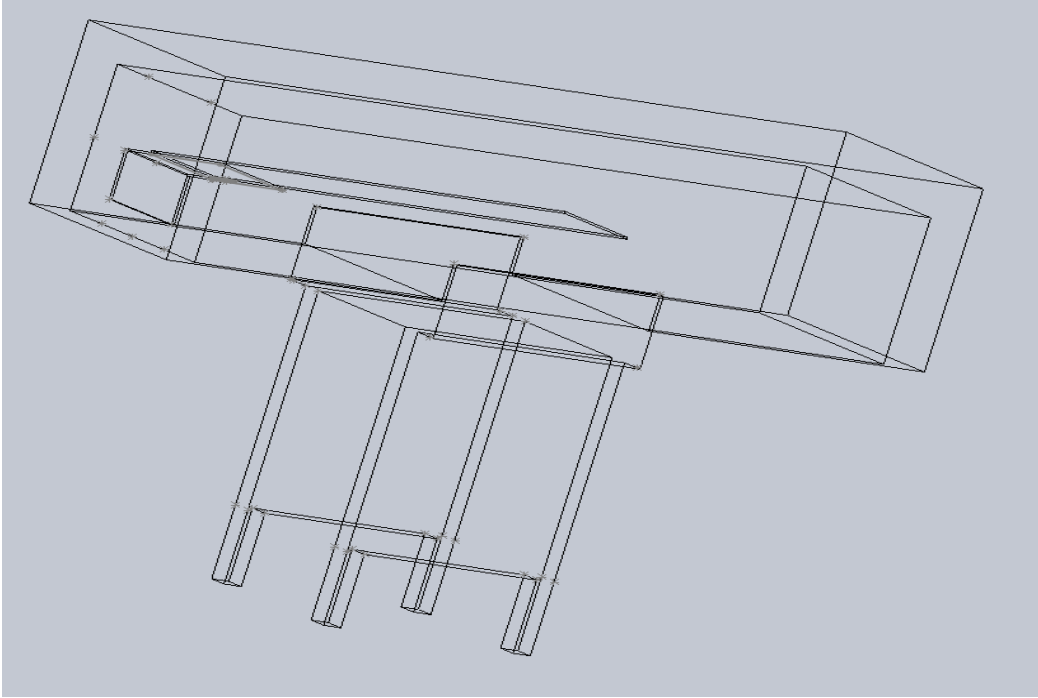


Figure 15. SolidWorks™ wire frame view of Al box and mounted PCB card.

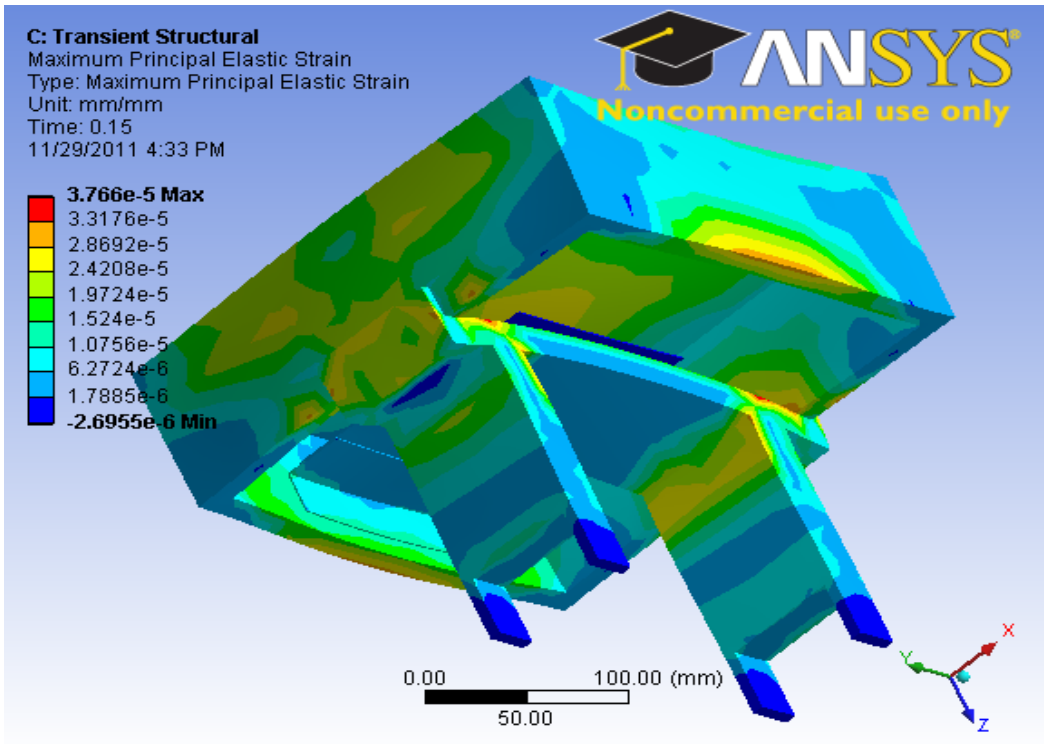


Figure 16. ANSYS™ FEM model of Al box and mounted PCB card.

The Al Box with mounted PCB card model was designed to exact specifications and dimensions as the Al box and PCB card used in the experimental impact testing. Table 4 shows the dimensions for both the Al box and the PCB card.

Component	Length (l) cm	Width (w) cm	Thickness (t) cm
Al Box Top	27.9	27.9	1.9
Al Box Sides	27.9	7.6	1.3
PCB Card	15.2	12.7	0.1

Table 4. Al box and PCB card dimensions.

Fixed conditions were applied to the vertical mounting brackets extending down from the Al box. A vertical impact force of 10 kN was applied to the top of the Al box. The total test interval was set to 0.1 s. The impact was simulated by turning on and off the force over a 0.01 s interval. Force data was input into a table within ANSYS™ as shown in Figure 17. These data point were then plotted as a function of time. Figure 18 is a plot in ANSYS™ of the impact force as a function of time. The number 1 at the far right hand side of the graph represents 0.1 s and the end of the test interval. The graph shows the impulse turn on at 0.1, peak at 0.15, and return to zero at 0.2.

	Steps	Time [s]	<input checked="" type="checkbox"/> X [N]	<input checked="" type="checkbox"/> Y [N]	<input checked="" type="checkbox"/> Z [N]
1	1	0.	= 0.	= 0.	0.
2	1	0.1	0.	0.	0.
3	2	0.15	= 0.	= 0.	10000
4	3	0.2	= 0.	= 0.	0.
5	4	1.	= 0.	= 0.	0.

Figure 17. ANSYS™ tabular data input.

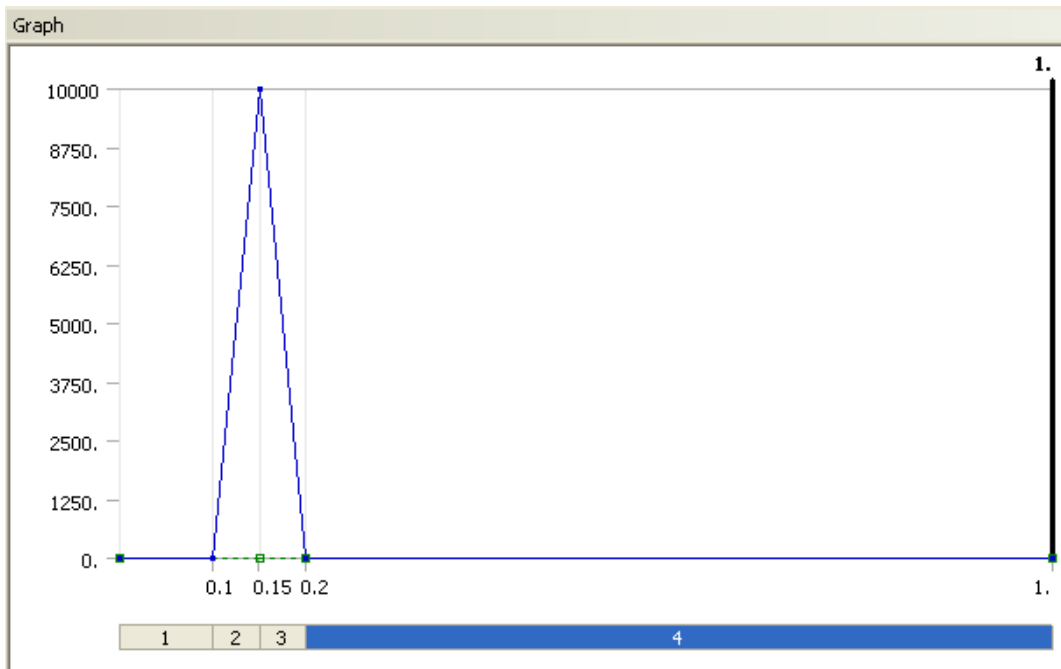


Figure 18. ANSYS™ plot of force vs. time for a 0.1 s interval.

IV. RESULTS AND DISCUSSION

A. LONGITUDINAL AND LATERAL STRAIN IN PCB CARD

1. Longitudinal and Lateral Strain as a Function of Time

Seven impact tests were conducted with added weights of 0, 5, 10, 15, 20, 25, and 30 lb. For each impact test, the max values for strain were found in the longitudinal axis in quadrant 4 from strain gauge number 4. Quadrants 1 and 4 saw higher strain values as they were closest to the mounted AI bracket. Figures 19 through 25 are plots of both longitudinal and lateral strain versus time over a period of 0.1 s.

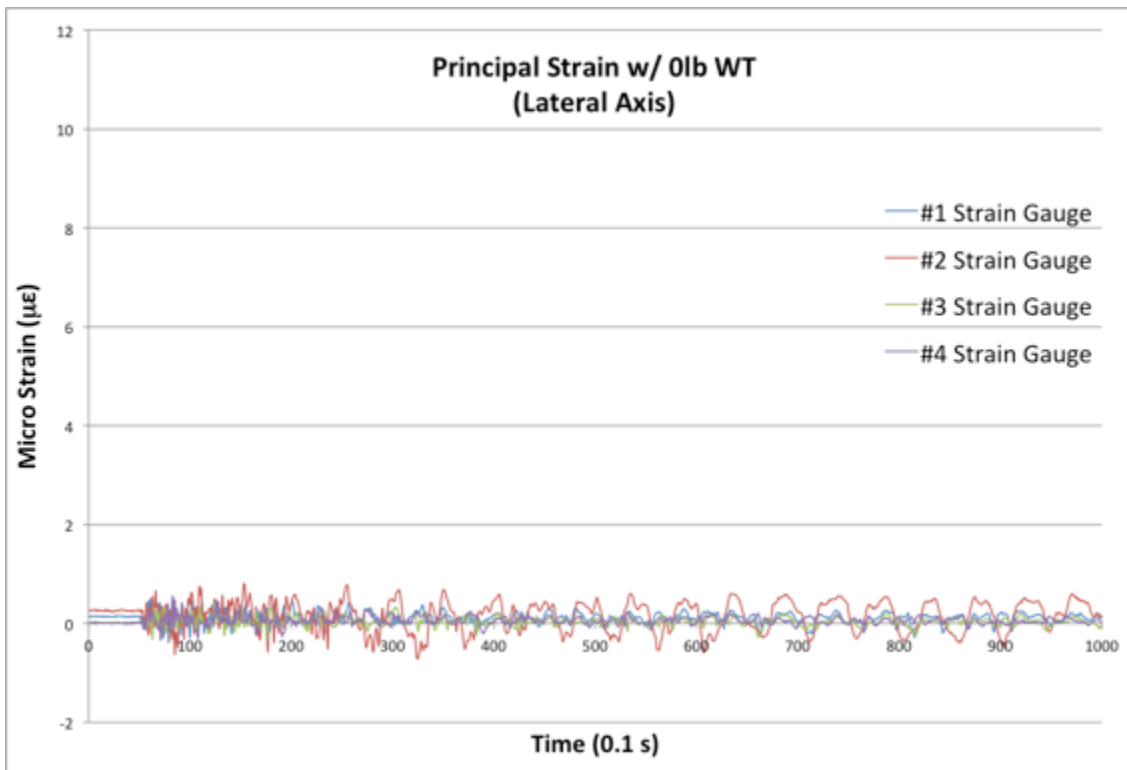
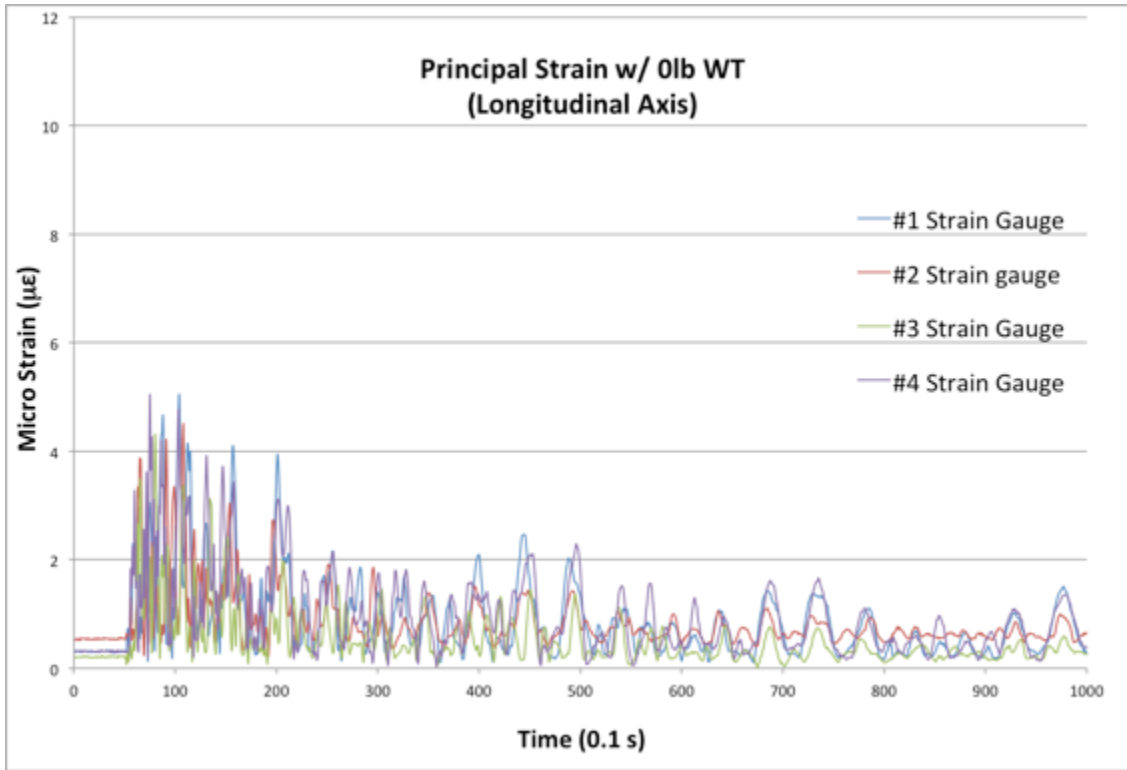


Figure 19. Longitudinal and lateral strain with 0 lb. added weight.

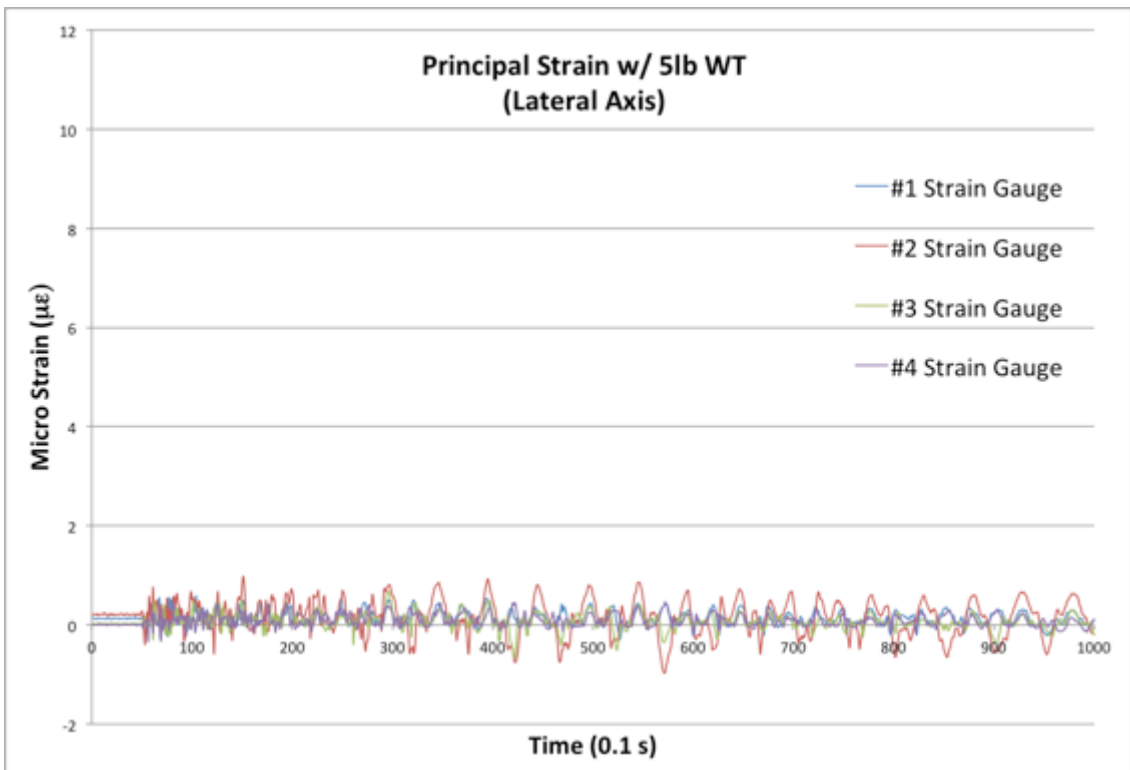
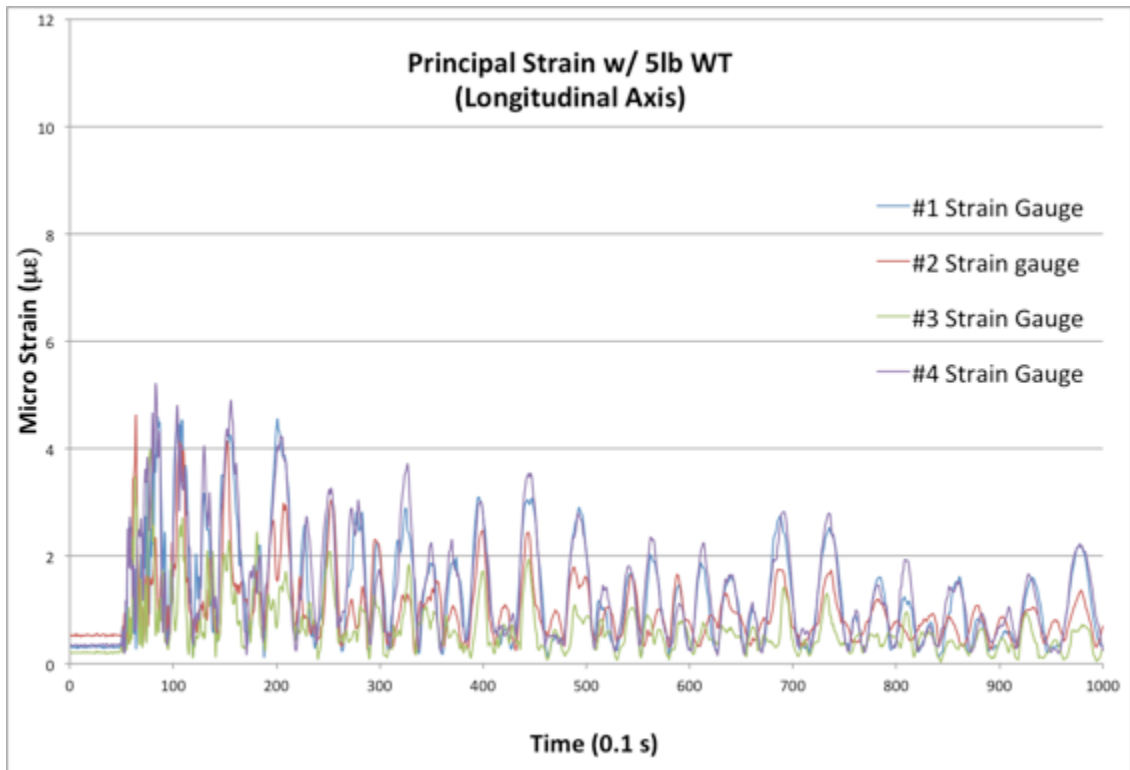


Figure 20. Longitudinal and lateral strain with 5 lb. added weight.

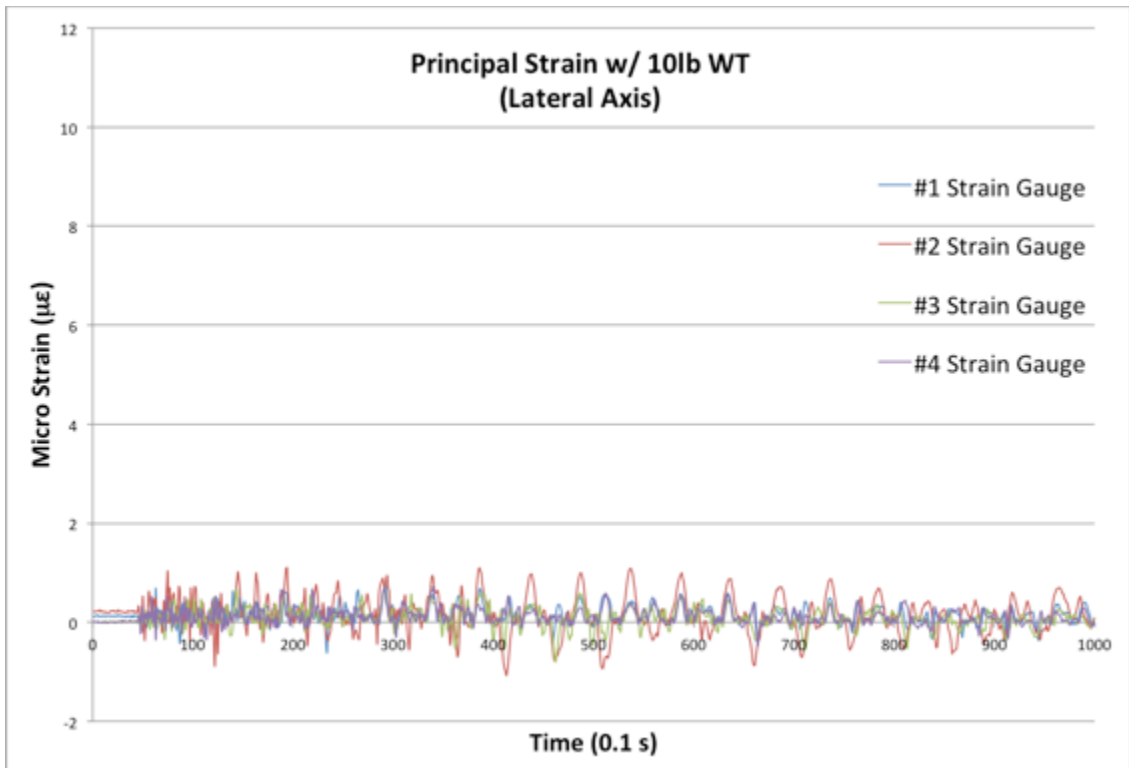
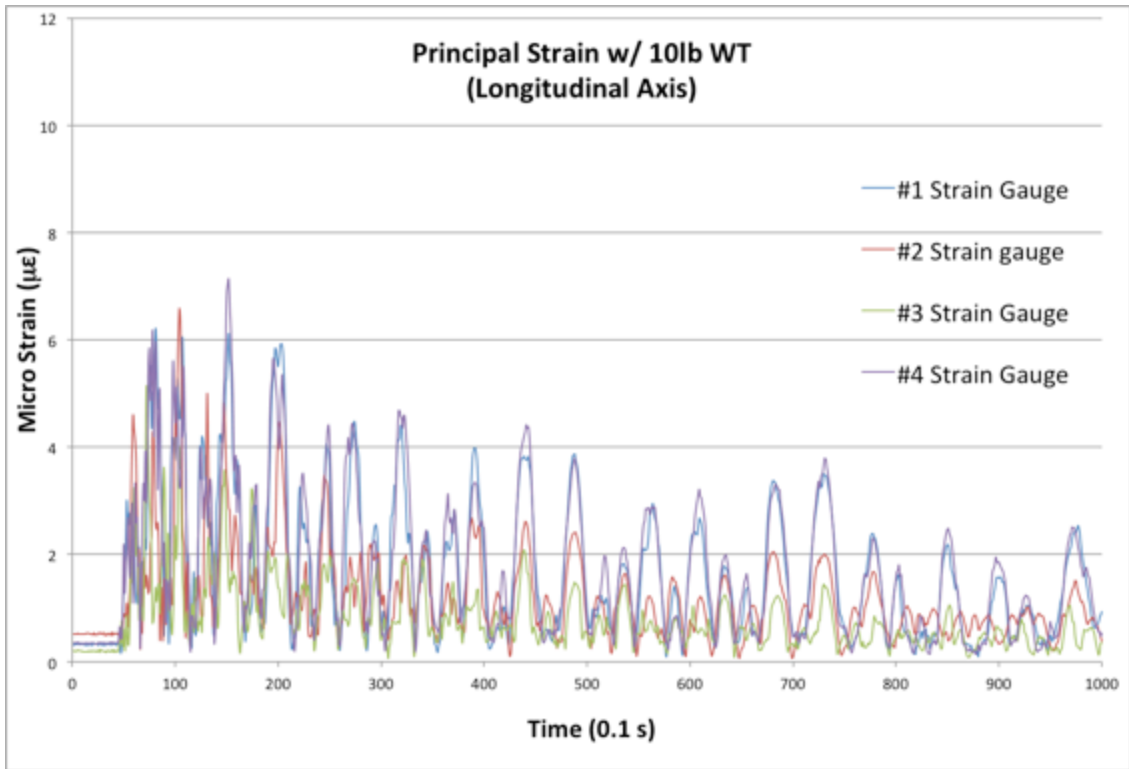


Figure 21. Longitudinal and lateral strain with 10 lb. added weight.

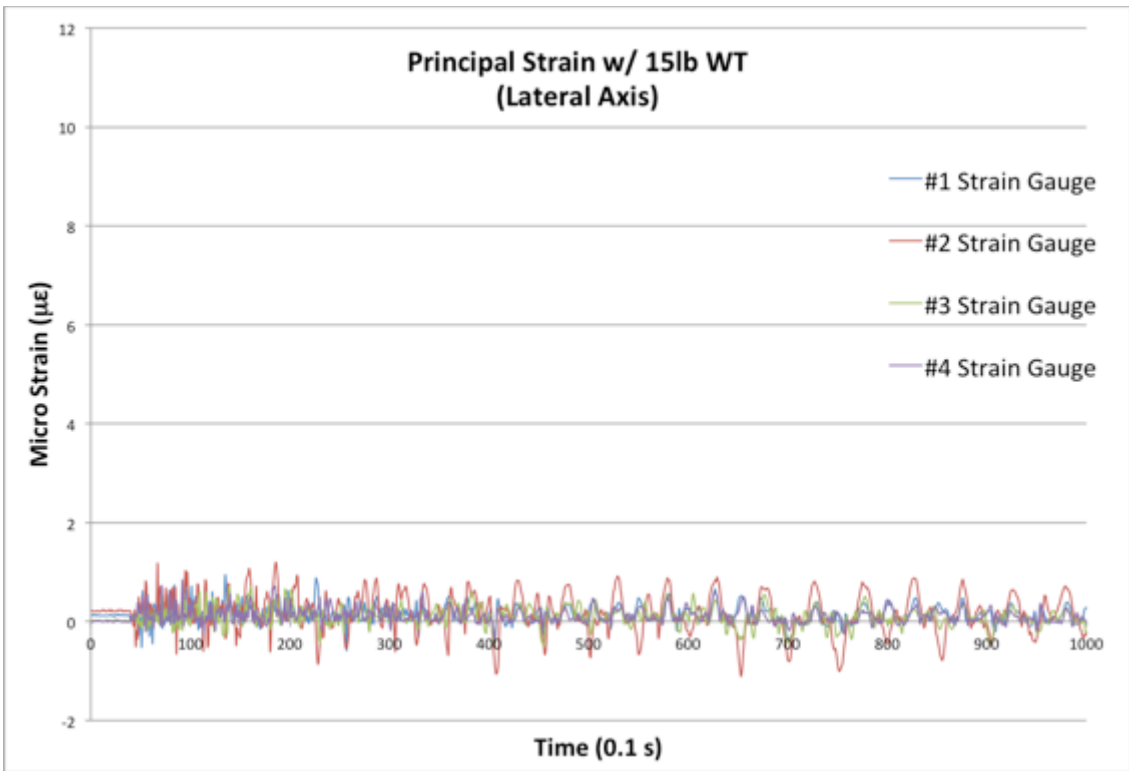
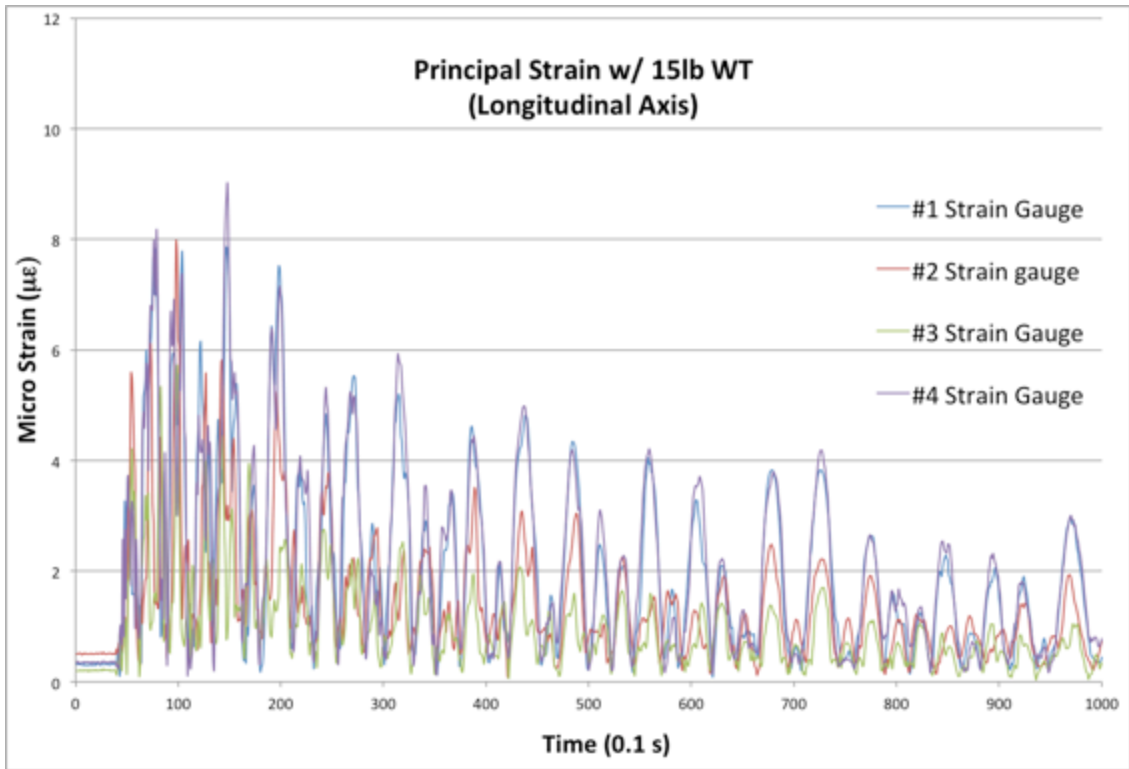


Figure 22. Longitudinal and lateral strain with 15 lb. added weight.

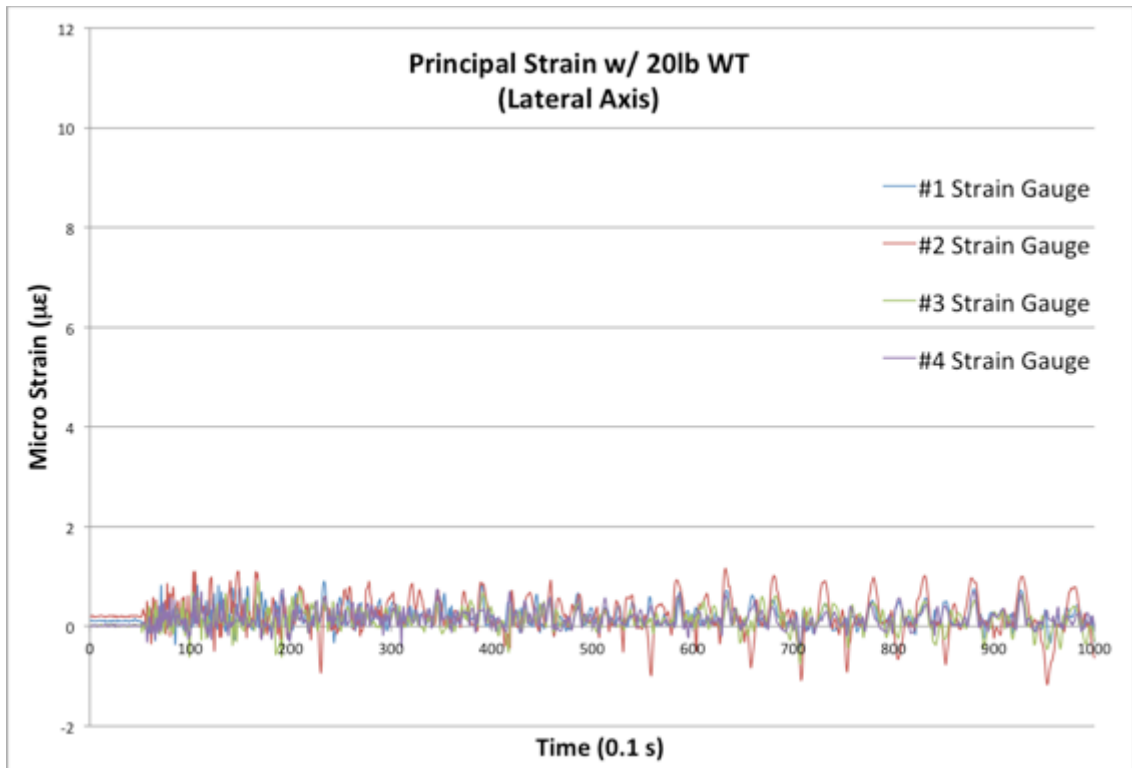
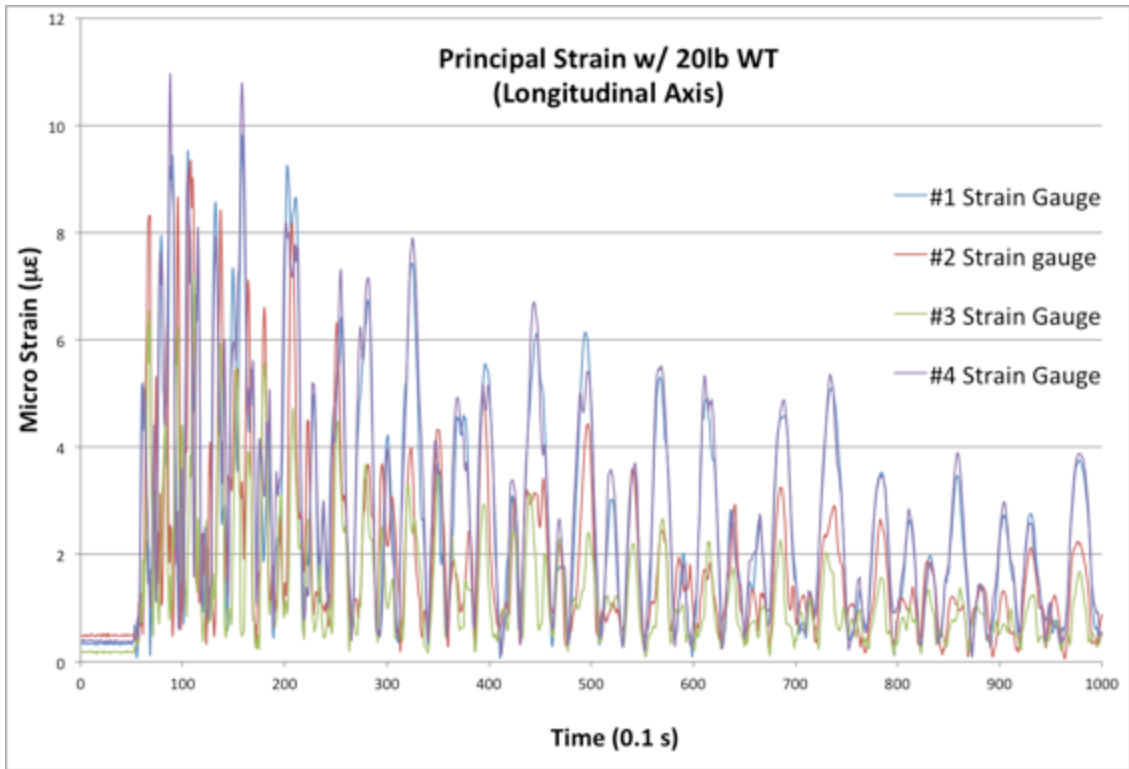


Figure 23. Longitudinal and lateral strain with 20 lb. added weight.

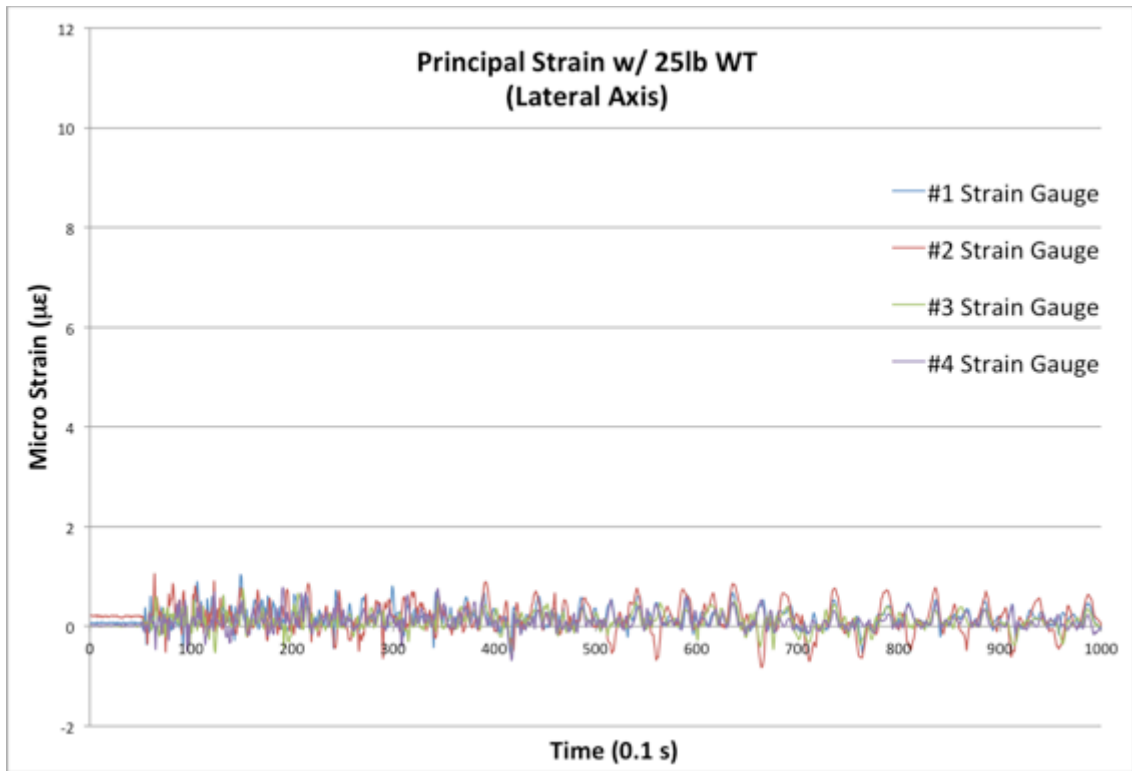
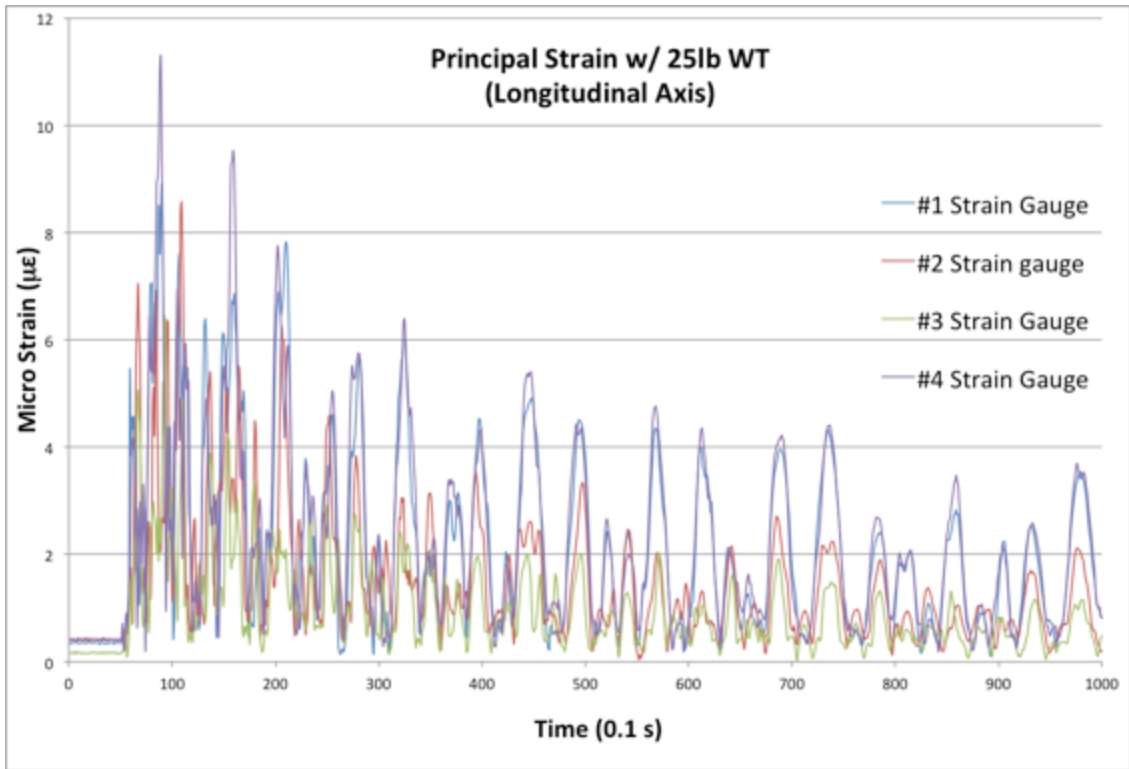


Figure 24. Longitudinal and lateral strain with 25 lb. added weight.

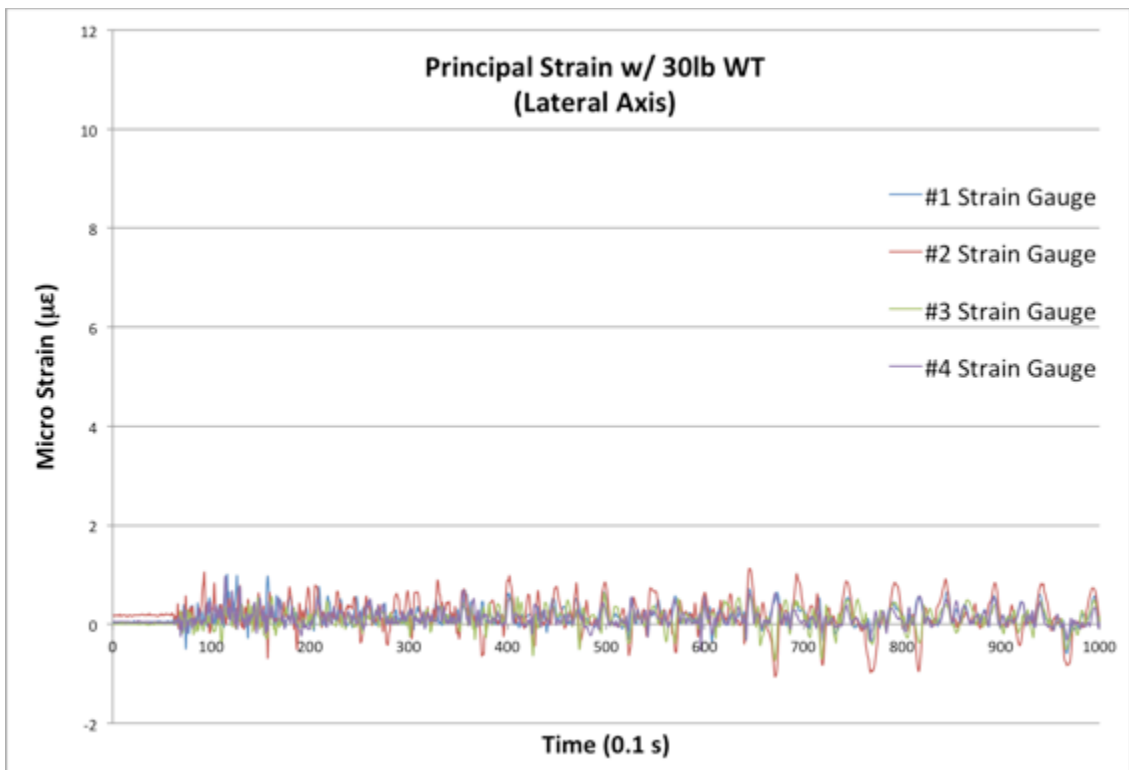
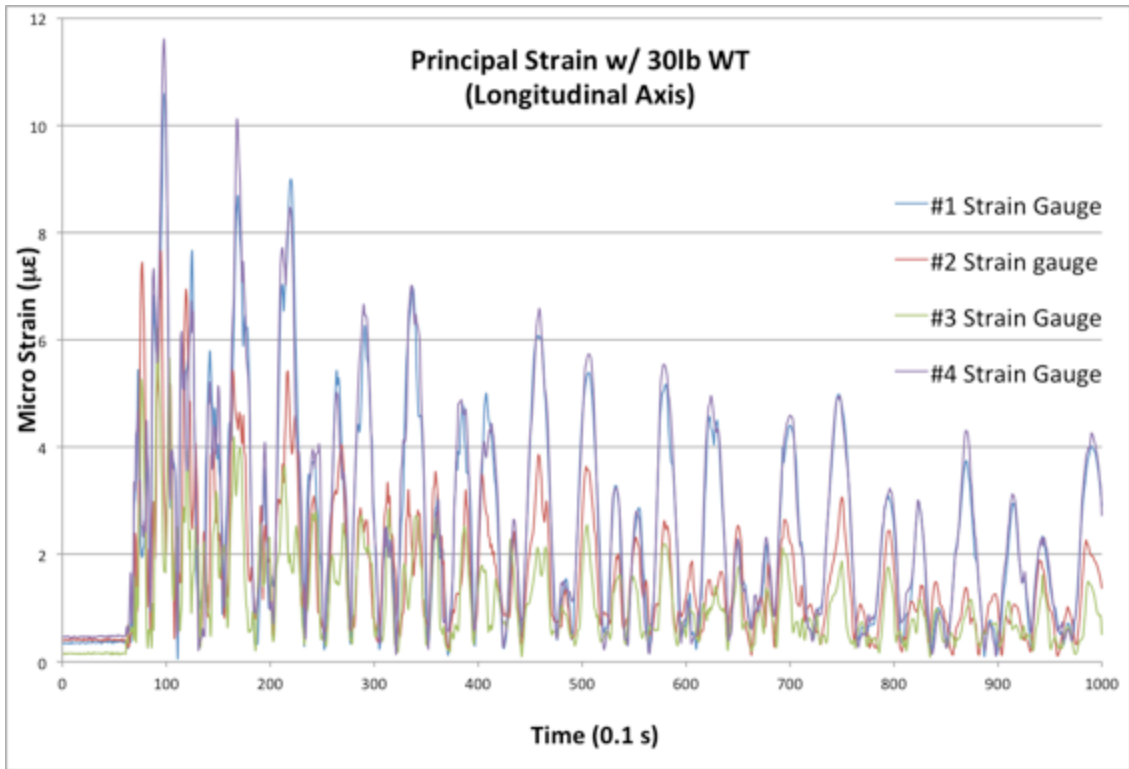


Figure 25. Longitudinal and lateral strain with 30 lb. added weight.

2. Longitudinal and Lateral Strain as a Function of Added Weight

A second series of plots, Figures 26 through 32, were created in order to show the maximum longitudinal strain values recorded during each impact test. These values, recorded in Table 5, were plotted as a function of added weight as shown in Figure 33. The maximum values for longitudinal strain ranged from 5.04 $\mu\epsilon$ at 0 lb. added weight to 11.60 $\mu\epsilon$ at 30 lb. added weight. The increase in longitudinal strain was roughly linear over the 0 to 30 lb. range, where the lateral strain remained constant at approximately 1 $\mu\epsilon$.

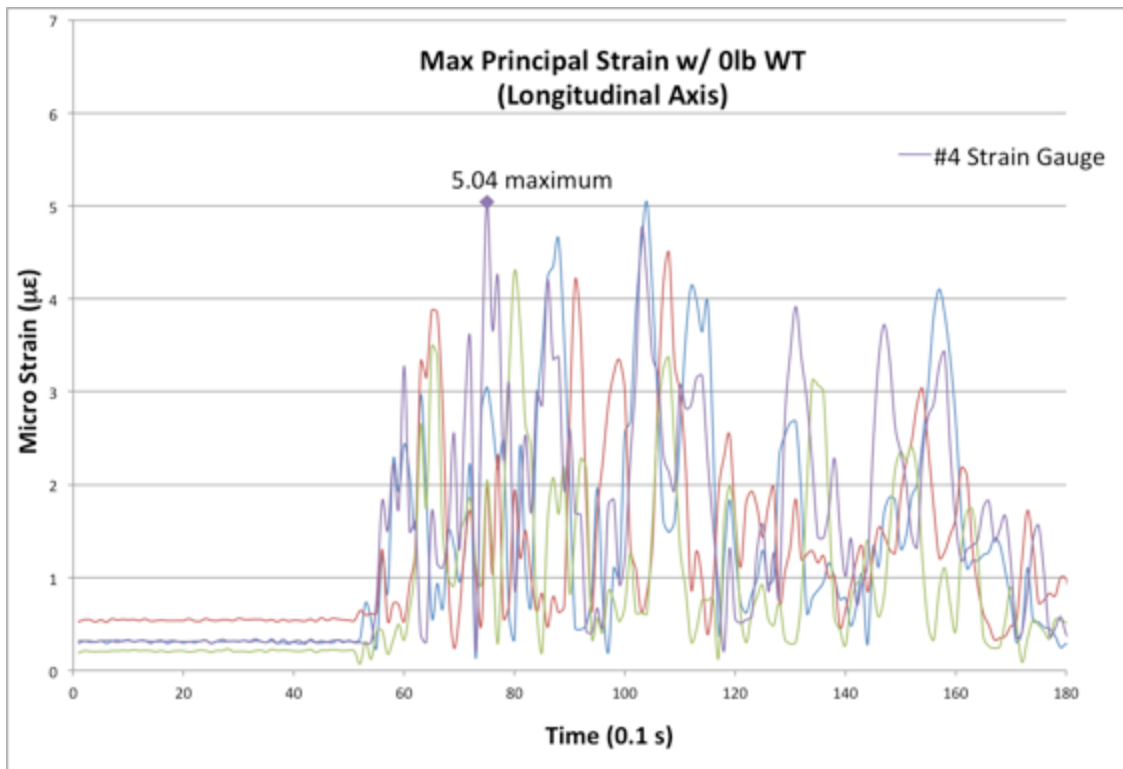


Figure 26. Max Longitudinal strain with 0 lb. added weight.

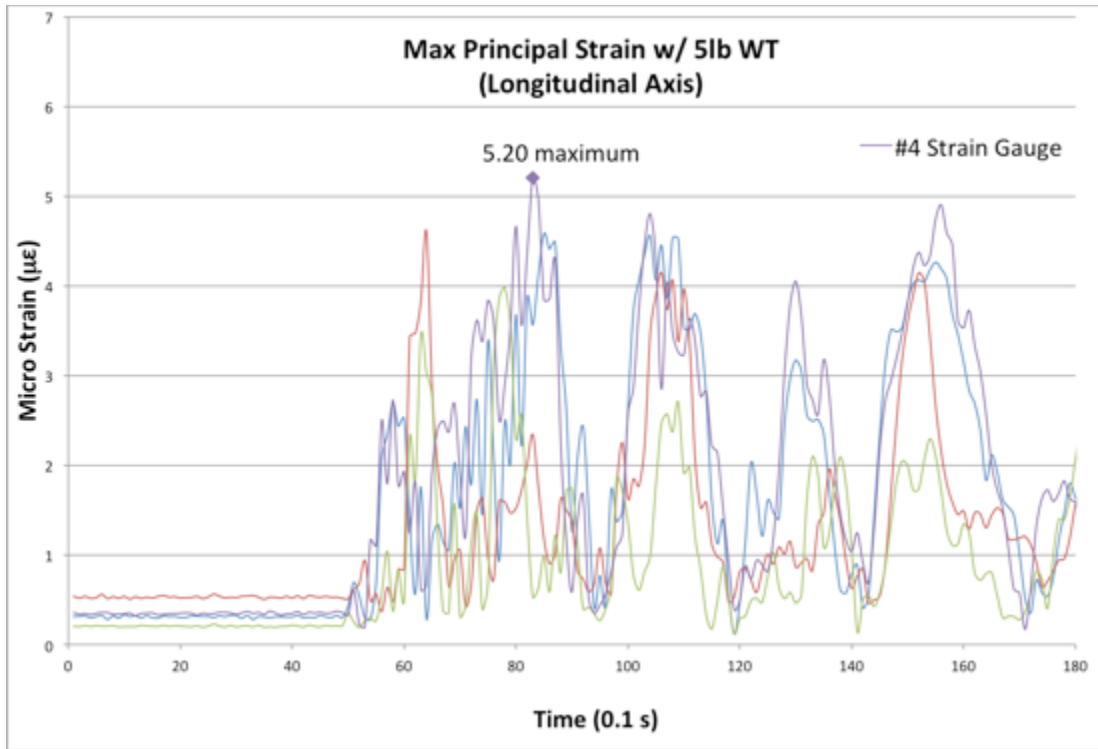


Figure 27. Max Longitudinal strain with 5 lb. added weight.

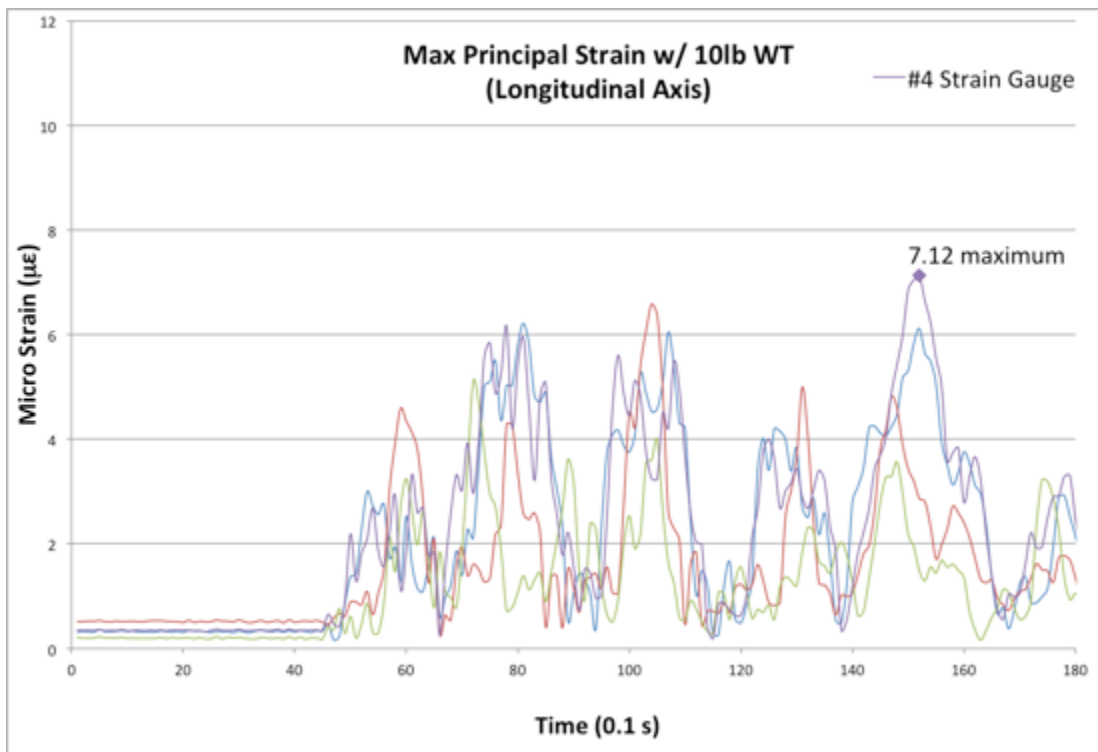


Figure 28. Max Longitudinal strain with 10 lb. added weight.

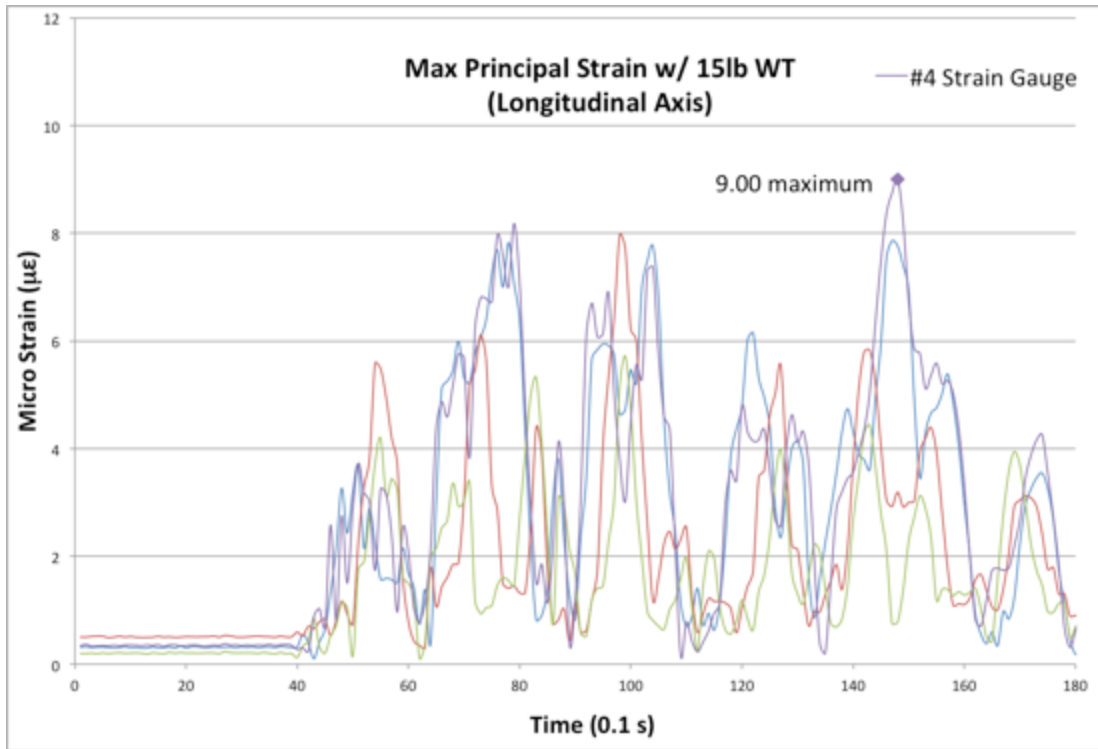


Figure 29. Max Longitudinal strain with 15 lb. added weight.

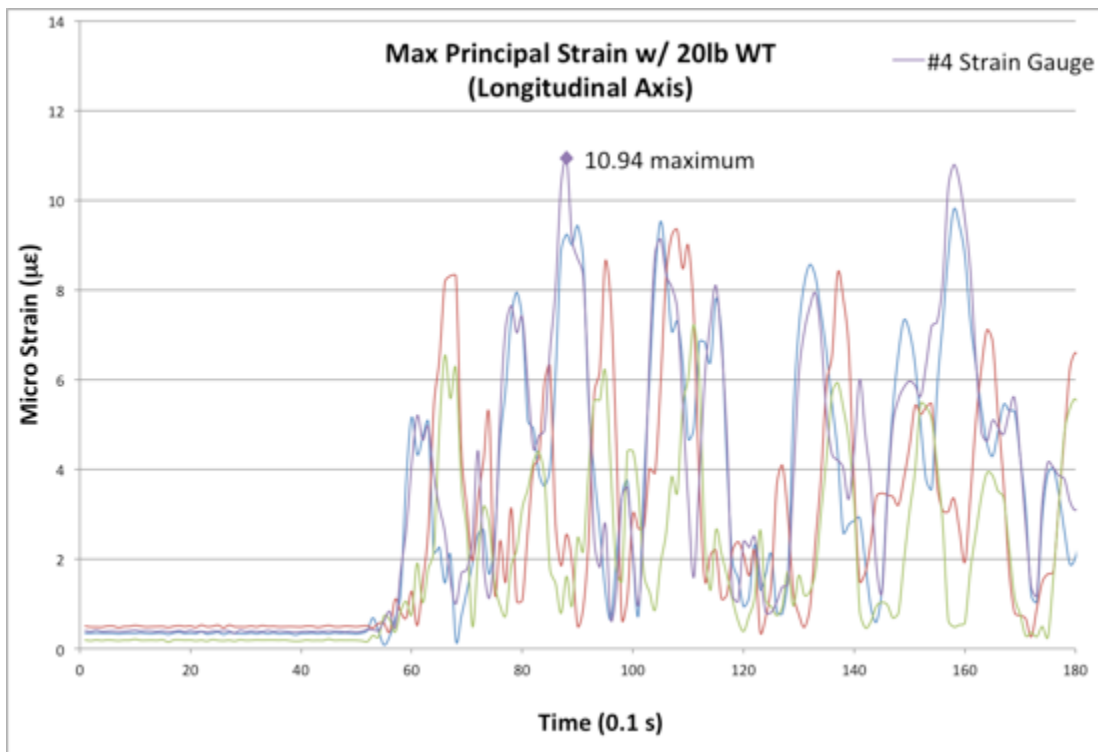


Figure 30. Max Longitudinal strain with 20 lb. added weight.

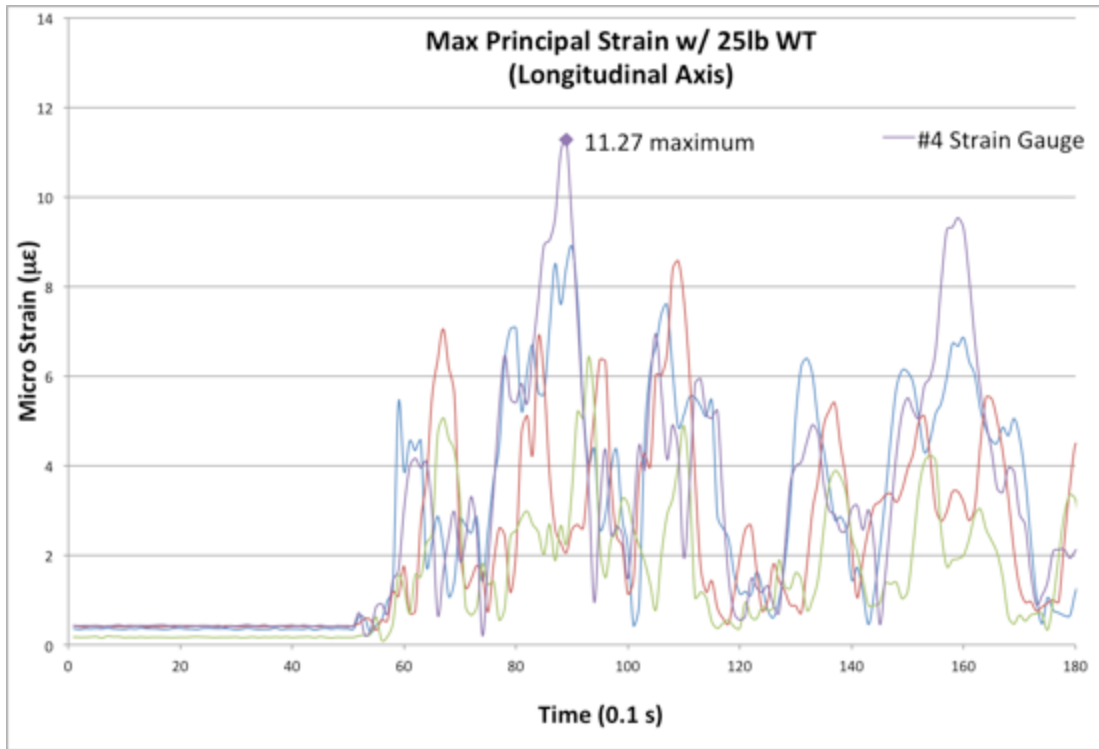


Figure 31. Max Longitudinal strain with 25 lb. added weight.

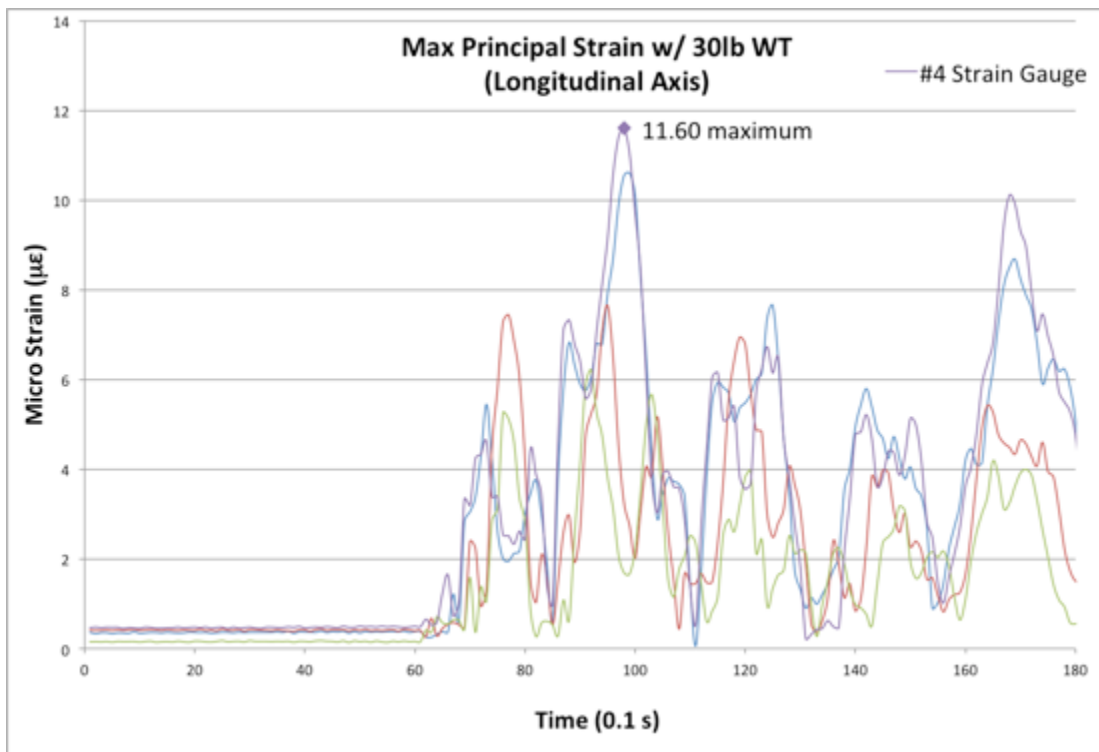


Figure 32. Max Longitudinal strain with 30 lb. added weight.

Strain ($\mu\epsilon$)	0 lb. added WT	5 lb. added WT	10 lb. added WT	15 lb. added WT	20 lb. added WT	25 lb. added WT	30 lb. added WT
Longitudinal	5.04	5.20	7.12	9.00	10.94	11.27	11.60
Lateral	0.80	0.85	0.91	1.12	1.13	0.81	1.06

Table 5. Max Longitudinal and lateral strain values.

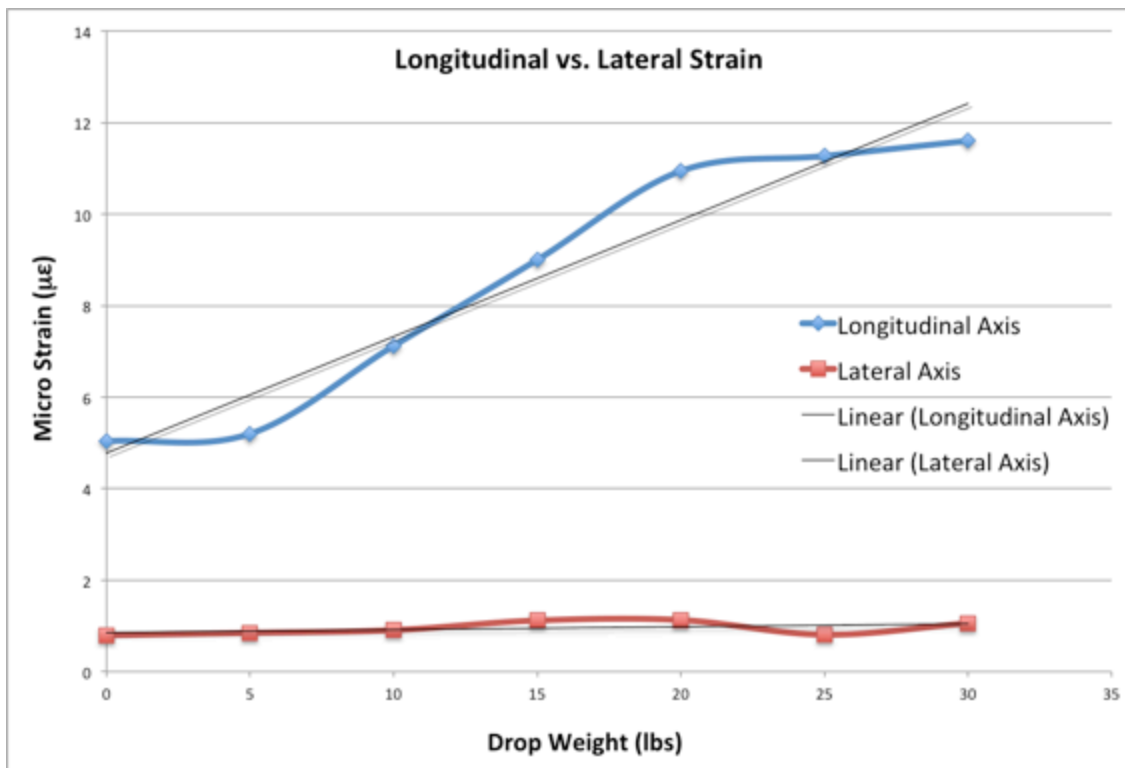


Figure 33. Max Longitudinal and lateral strain as a function of added weight.

B. FEM ANALYSIS OF SOLDERED ELECTRONIC COMPONENT

The FEM analysis of the soldered electronic component provided both visual and numerical solder joint strain results. Tables 6 and 7 list the magnitudes of the five different strains analyzed in ANSYS™. Included in the tables are the maximum values for normal strain in the longitudinal and lateral axis, as well as the maximum principal strain for the model. Also found in the tables are max values for shear strain in the XY and YZ plane and the max shear strain for the model.

Strain Axis	Normal Strain ($\mu\epsilon$)	Max Principal Strain ($\mu\epsilon$)
Longitudinal (Y)	21.34	28.15
Lateral (X)	3.32	

Table 6. Max longitudinal, lateral, and principal strain values for the model.

Strain Plane	Shear Strain ($\mu\epsilon$)
XY	13.19
YZ	40.33

Table 7. Shear in the XY and YZ plane.

The ANSYS™ images produced following the analysis of the five strain values provide a visual reference to the location of the strain. Figures 34 through 43 are color coded to show the maximum and minimum values for strain. Locations on the model colored red represent maximum strains, and those locations colored blue represent minimums. The included legend on the far left hand side of each image represents all values between the maximums and minimums. Images showing only four cylindrical solder joints were created by suppressing all other bodies in the model. This allows the viewer to observe strain characteristics on all surfaces of the solder joint.

Figures 34 through 38 are full model views of the maximum principal, normal, and shear strains on the soldered electronic component. From top to bottom, the silicon chip is joined to the PCB card by means of four lead free solder joints.

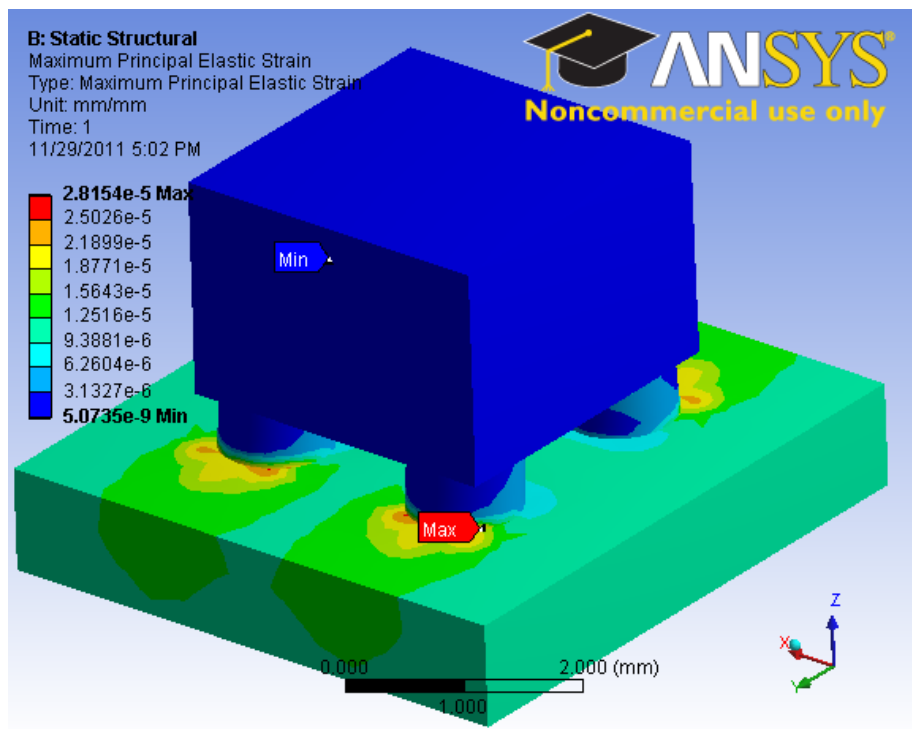


Figure 34. Max principal strain.

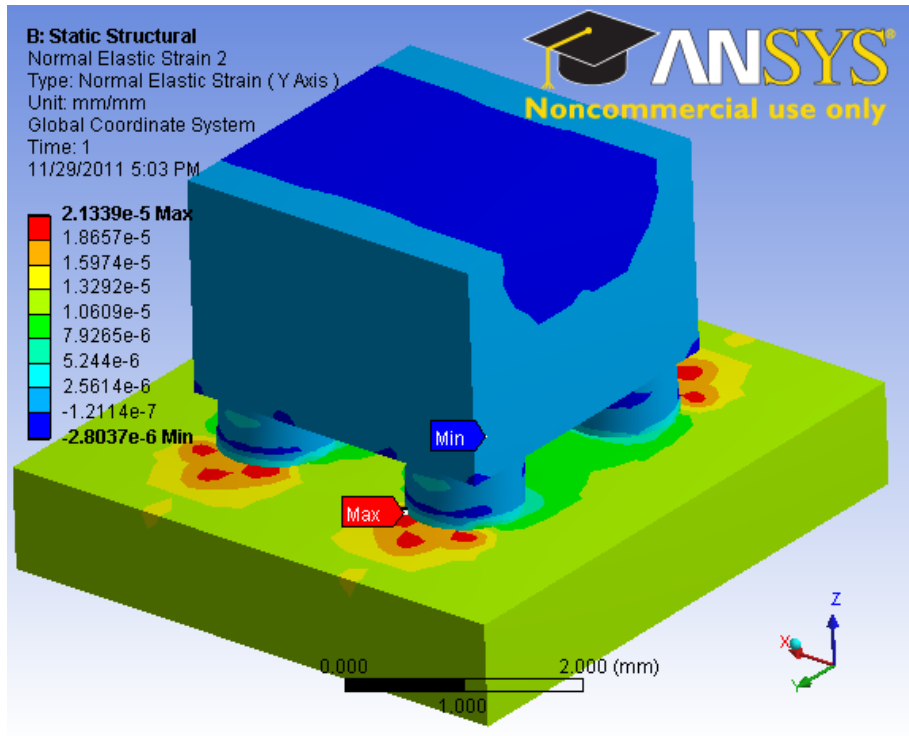


Figure 35. Normal strain in the longitudinal (Y) axis.

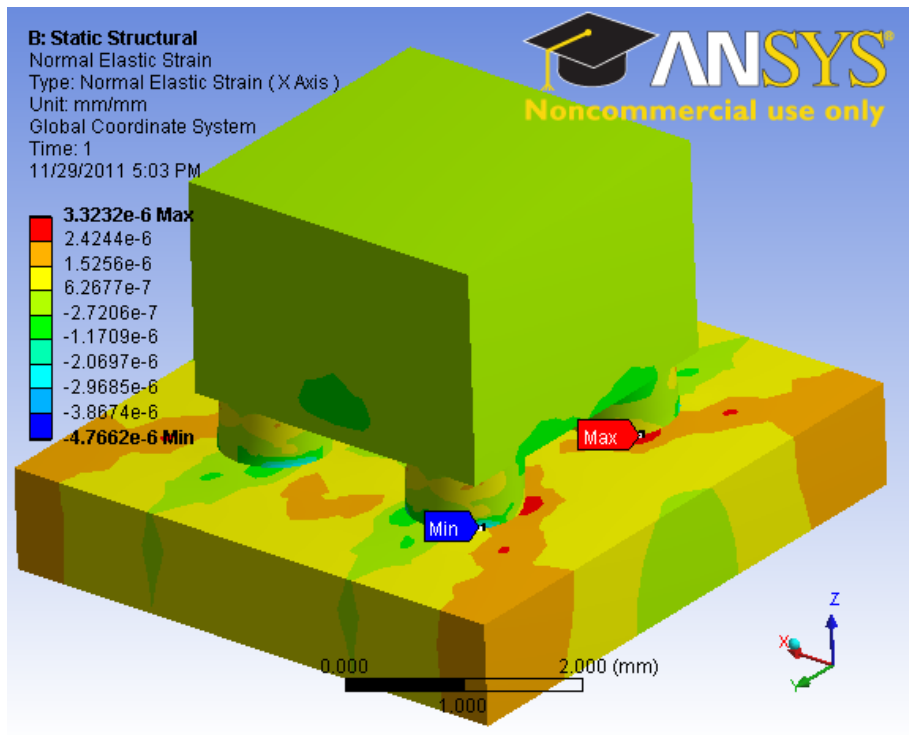


Figure 36. Normal strain in the lateral (X) axis.

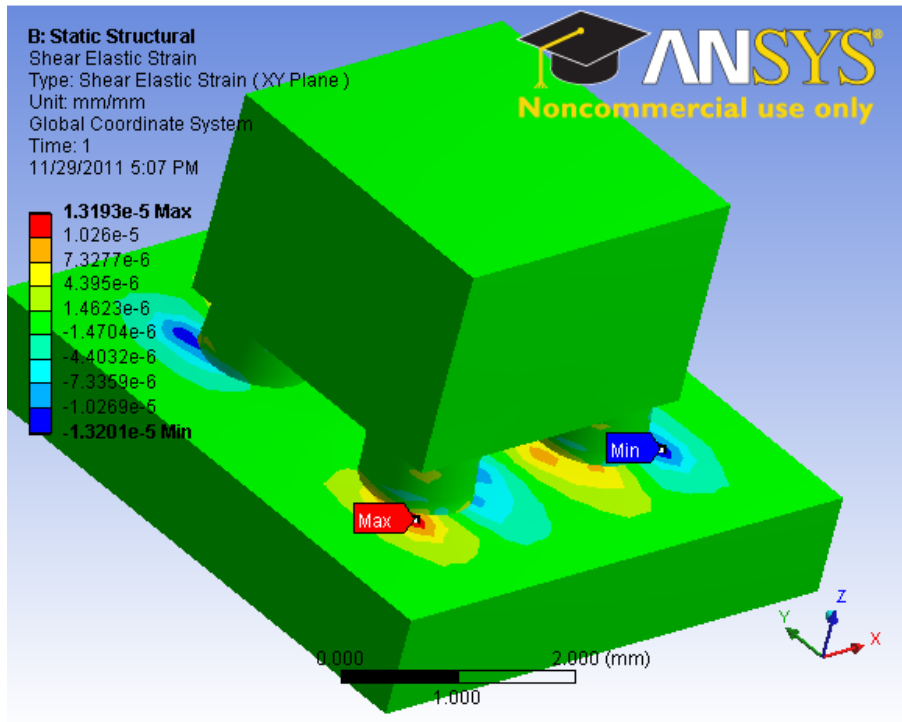


Figure 37. Shear strain in the XY plane.

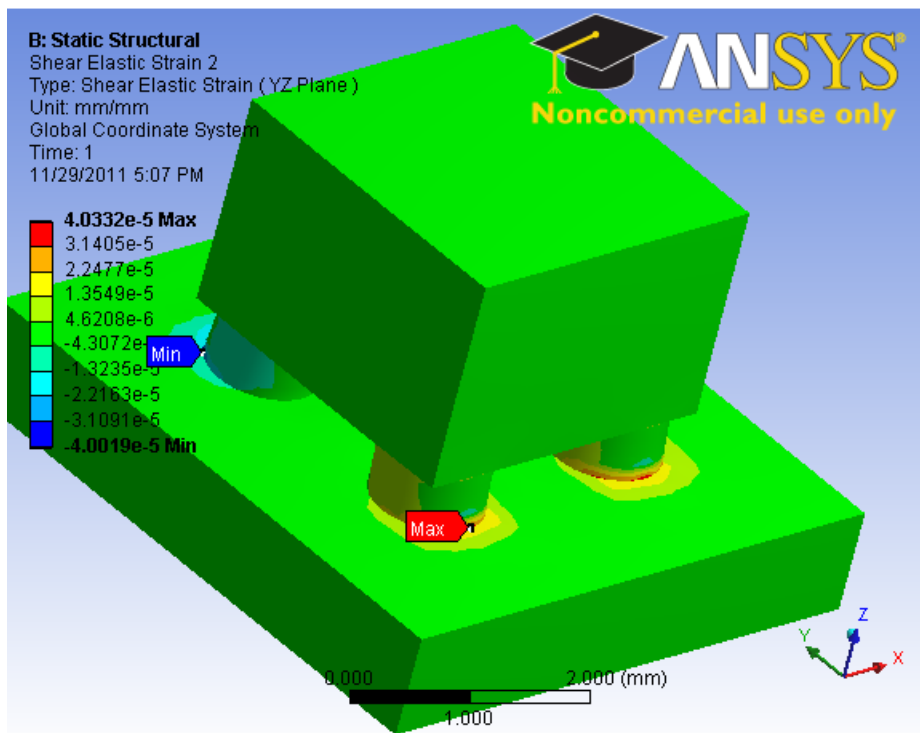


Figure 38. Shear strain in the YZ plane.

The maximum values for strain are consistently found at the solder joint and PCB card interface. Figures 39 through 43 show a suppressed view of the model with only the four solder joints and their corresponding strains solder joint. These images provide an unobstructed view of the strains on the PCB card and solder joint interface.

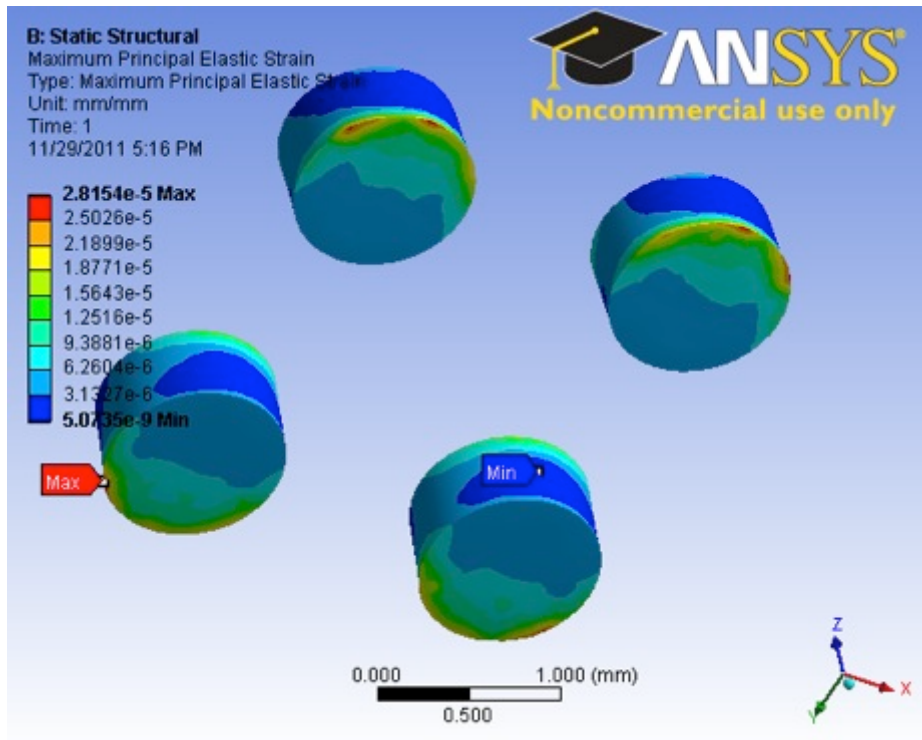


Figure 39. Max principal strain on solder joint.

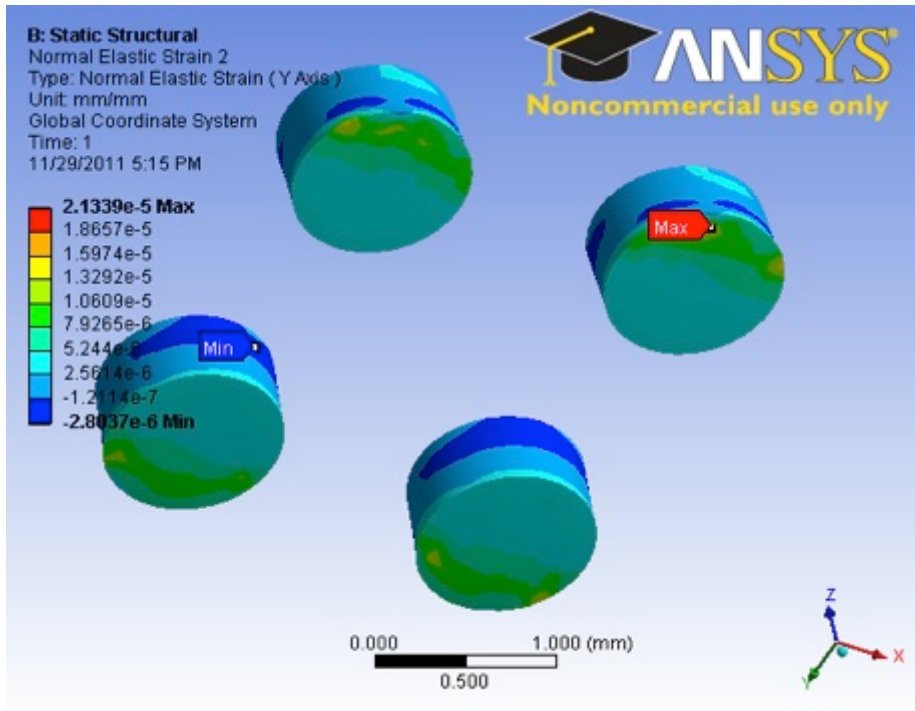


Figure 40. Normal strain on solder joint in the longitudinal (Y) axis.

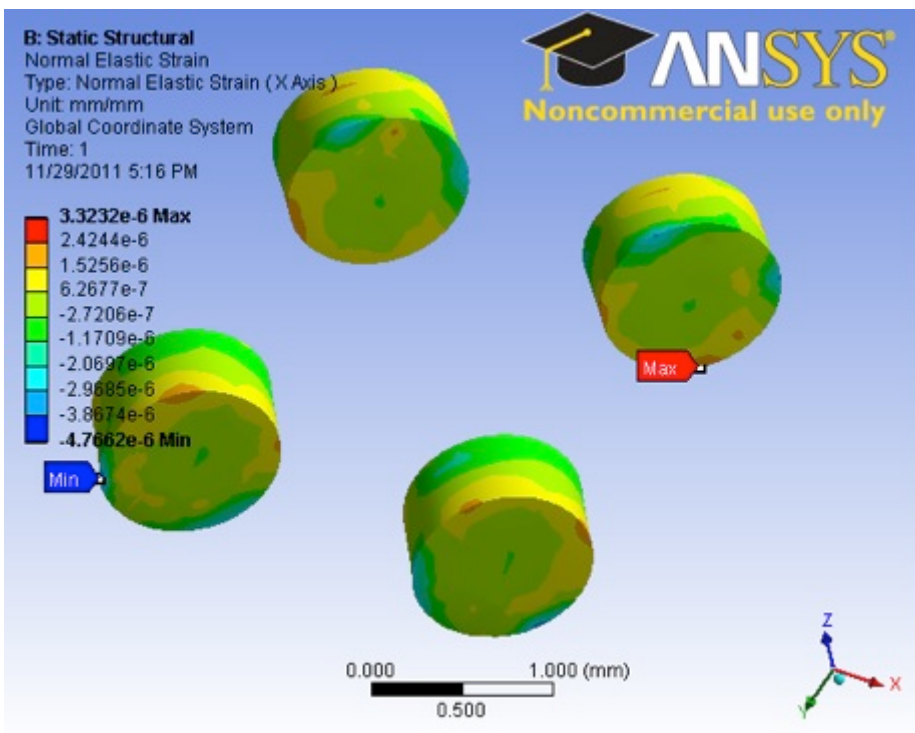


Figure 41. Normal strain on solder joint in the lateral (X) axis.

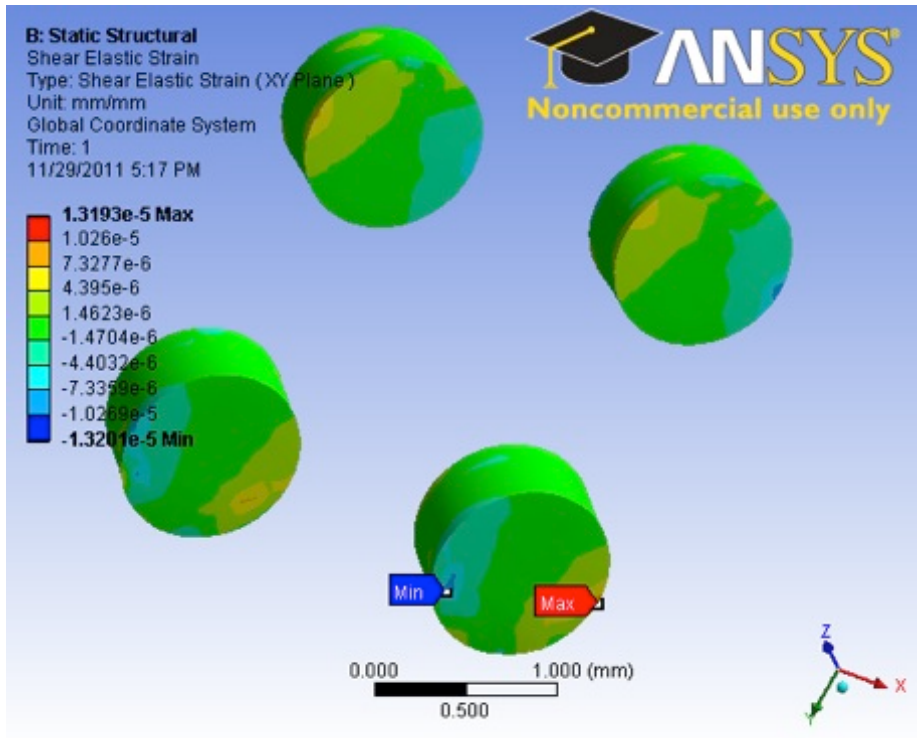


Figure 42. Shear strain on solder joint in the XY plane.

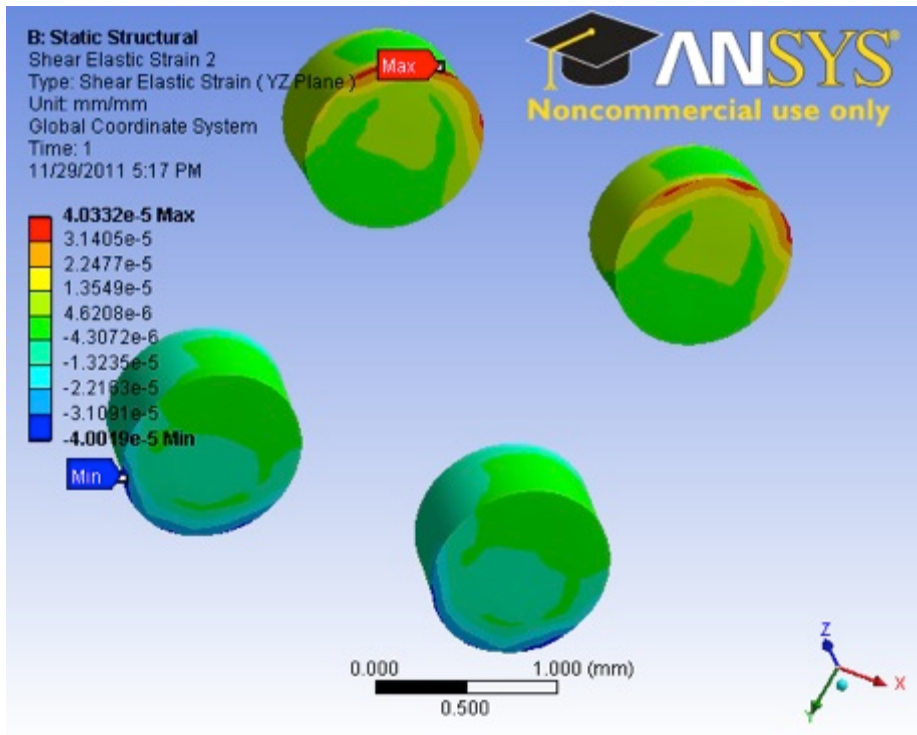


Figure 43. Shear strain on solder joint in the YZ plane.

C. FEM ANALYSIS OF BOX WITH MOUNTED PCB CARD

The second FEM model analysis conducted in ANSYS™ was a full-scale version of the Al box and PCB card used in experimental testing. A 10 kN impact force was used to simulate the experimental impact test using the 30 lb. of added weight. Tables 8 and 9 list the maximum values of strain observed in the ANSYS™ analysis of the PCB card. The results from ANSYS™ are compared to the values of strain found on the PCB card from the experimental testing.

Strain Axis	Normal Strain ($\mu\epsilon$)	Max Principal Strain ($\mu\epsilon$)
Longitudinal (X)	12.5	10.75
Lateral (Y)	0.75	

Table 8. Max longitudinal, lateral, and principal strain values in ANSYS™ PCB card.

Strain Plane	Shear Strain ($\mu\epsilon$)	Max Shear Strain ($\mu\epsilon$)
XY	13.50	22.10
XZ	7.95	

Table 9. XY, XZ, and max shear strain values in ANSYS™ PCB card.

Table 10 compares the experimental values for both longitudinal and lateral strains with those found in the ANSYS™ analysis of the PCB card. The difference in values can be attributed to the approximated 10 kN impact force used in the FEM model. In addition, the location of the strain gauges in the experimental testing was not identical to the location of the strains used from the FEM model. Although variations exist, the error between the ANSYS™ and experimental values of strain in the PCB card are negligible.

PCB Card	Normal Strain Longitudinal ($\mu\epsilon$)	Normal Strain Lateral ($\mu\epsilon$)
ANSYS™	12.50	0.75
Experimental	11.60	1.06

Table 10. Shear in the XY and YZ plane, and max shear strain for the model.

Figures 44 through 49 depict both a top and bottom view of the 6 different strains analyzed on the AI box and mounted PCB card. Figures 50 through 55 are top down views of the PCB card and the six different strains analyzed, with the AI box and AI bracket suppressed. Each image was captured at the peak of impact force at time step 0.15. Consistent with the experimental impact results, max strain values on the PCB card were seen closest to the mounting location on the AI bracket.

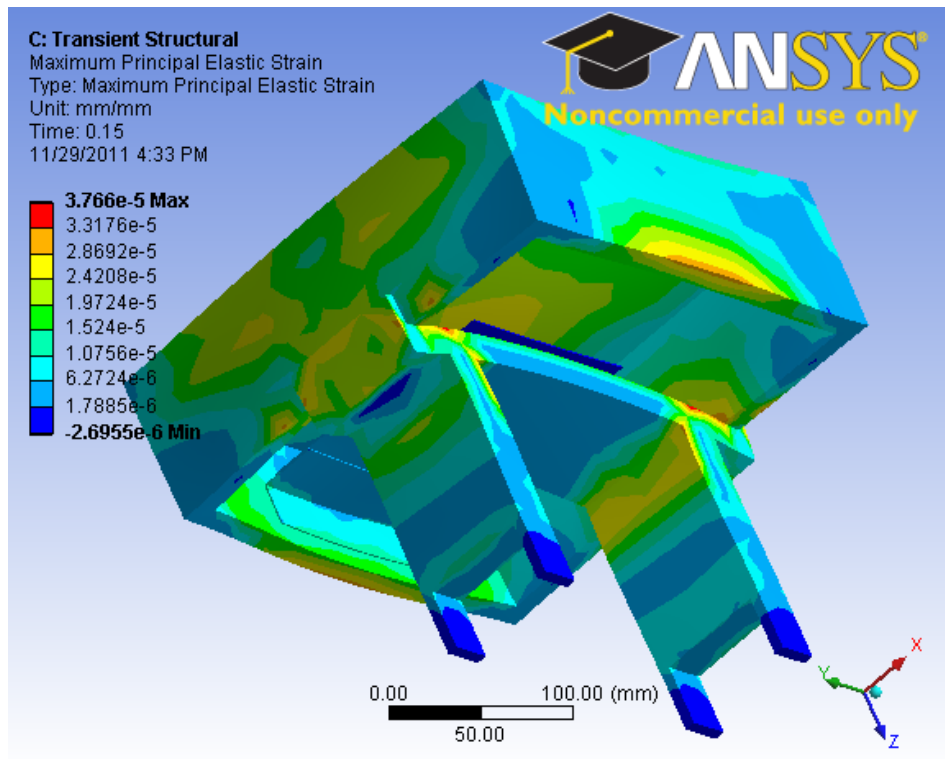
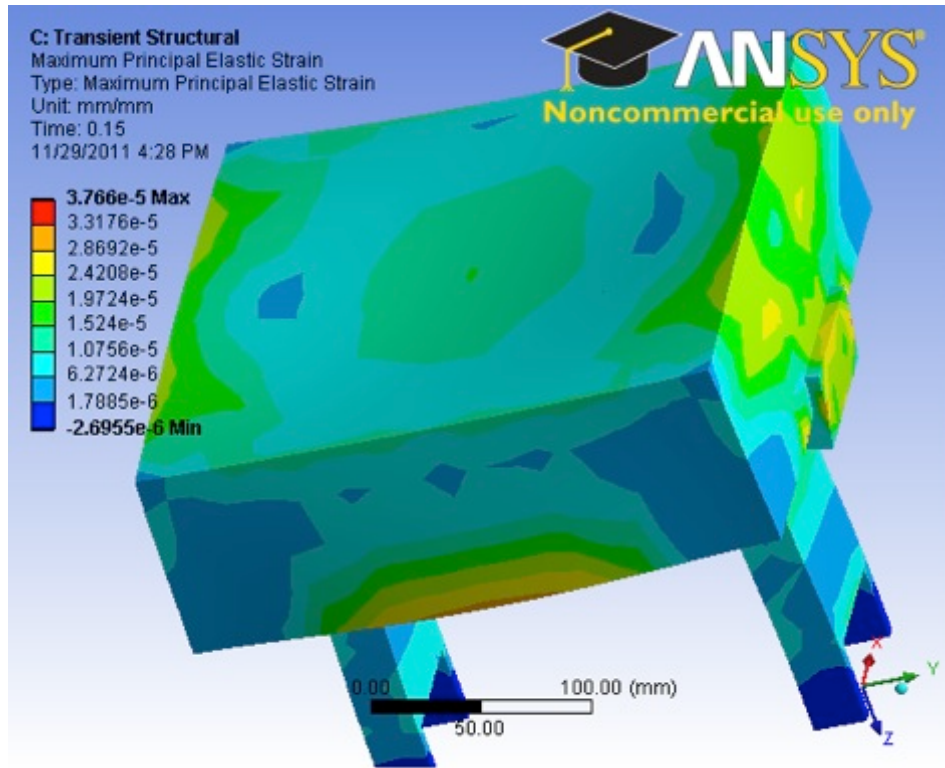


Figure 44. Max principal strain in Al box and PCB card.

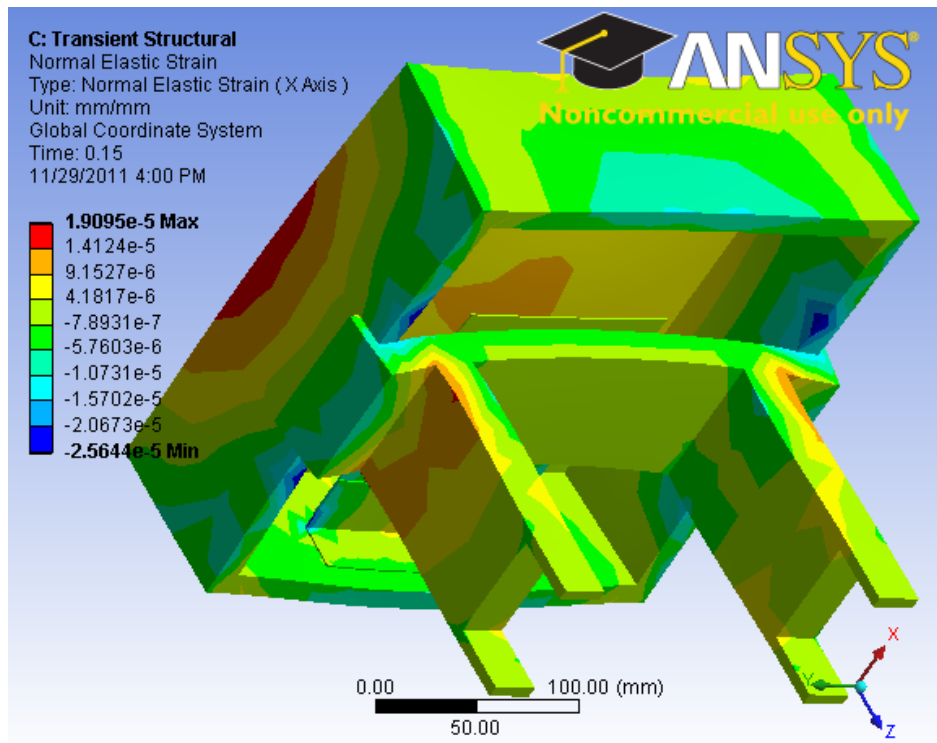
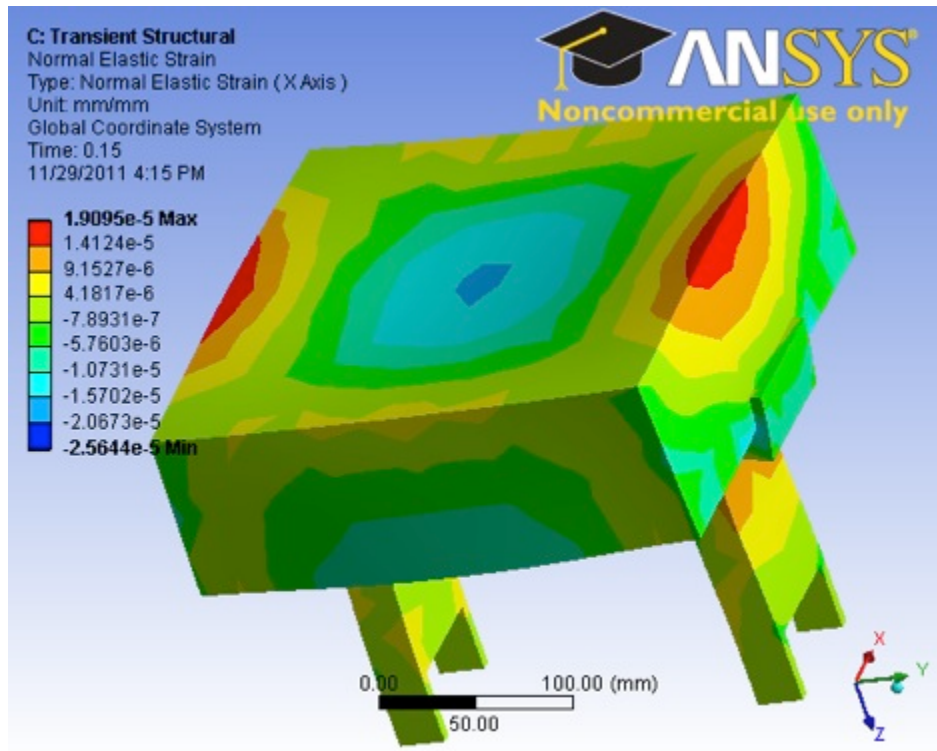


Figure 45. Normal strain in the longitudinal (X) axis in Al box and PCB card.

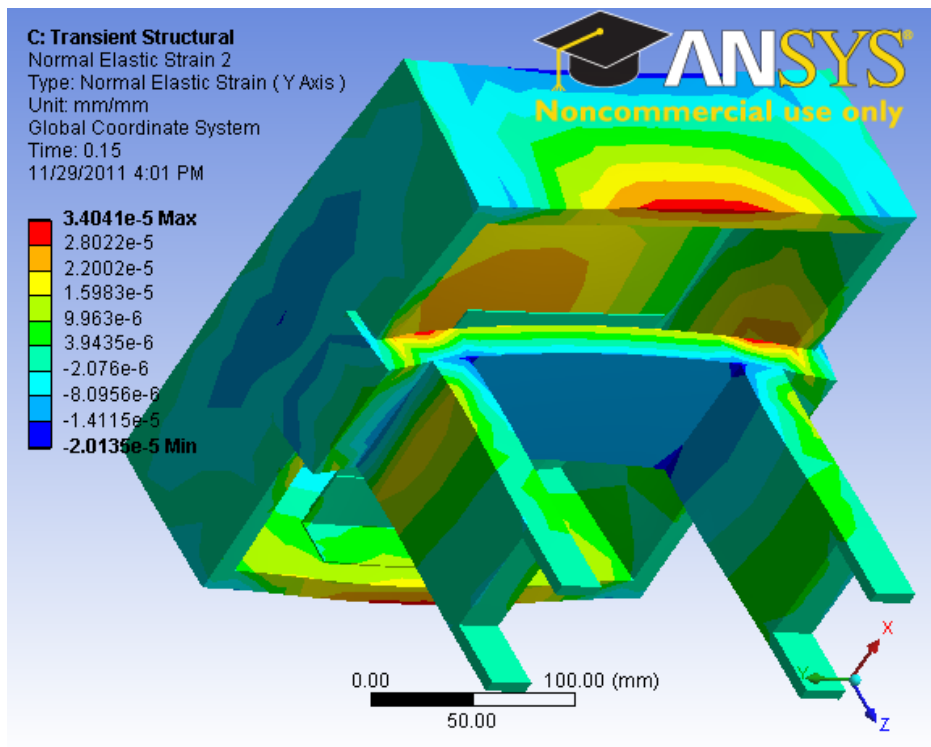
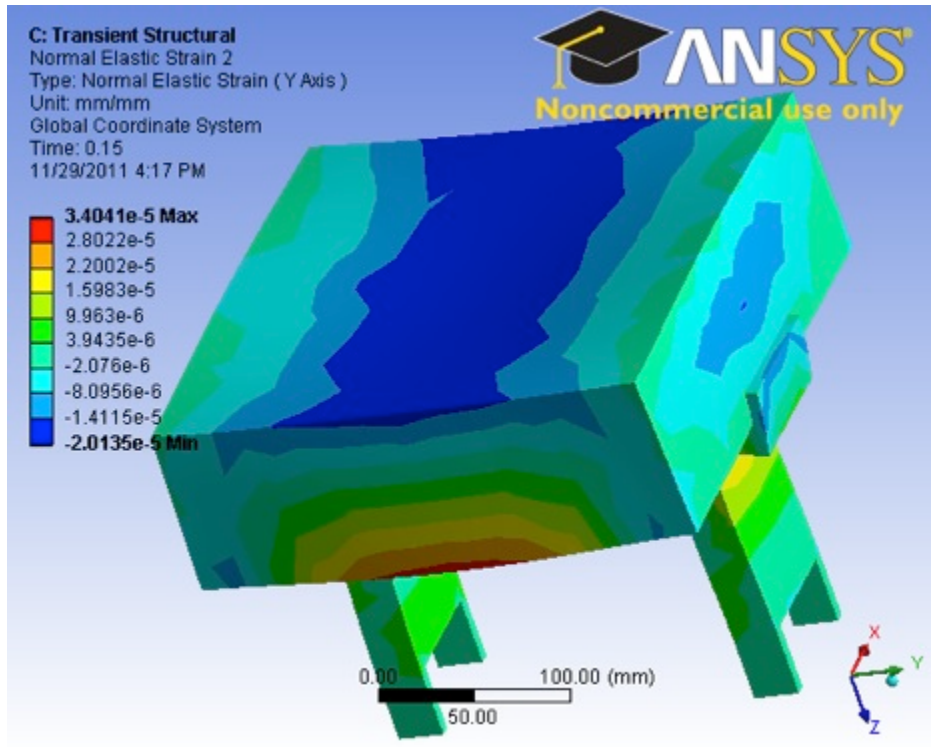


Figure 46. Normal strain in the lateral (Y) axis in Al box and PCB card.

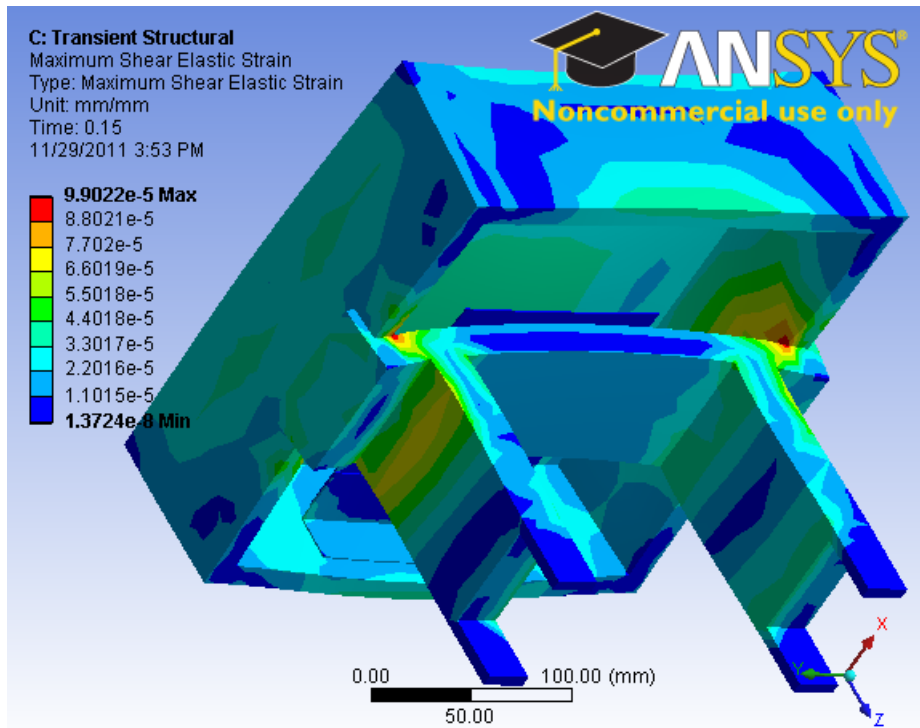
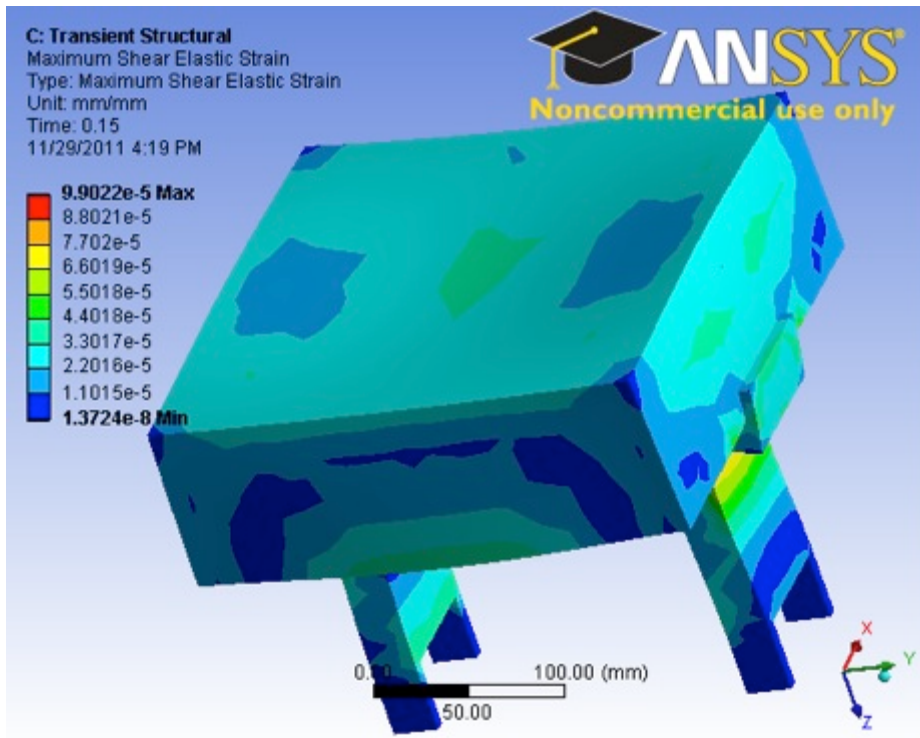


Figure 47. Max shear strain in Al box and PCB card.

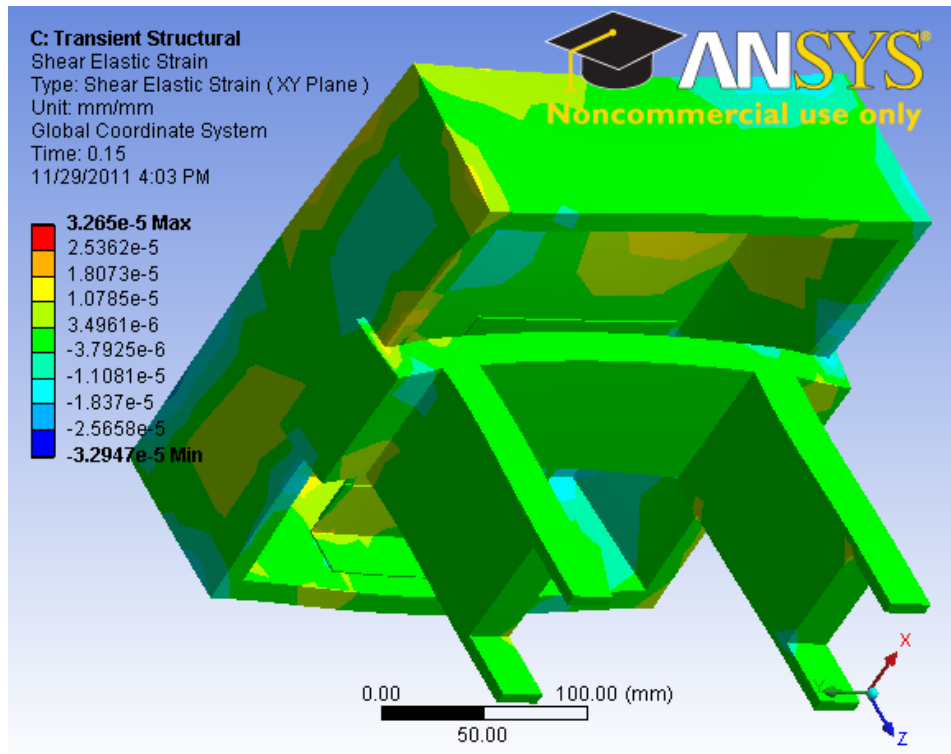
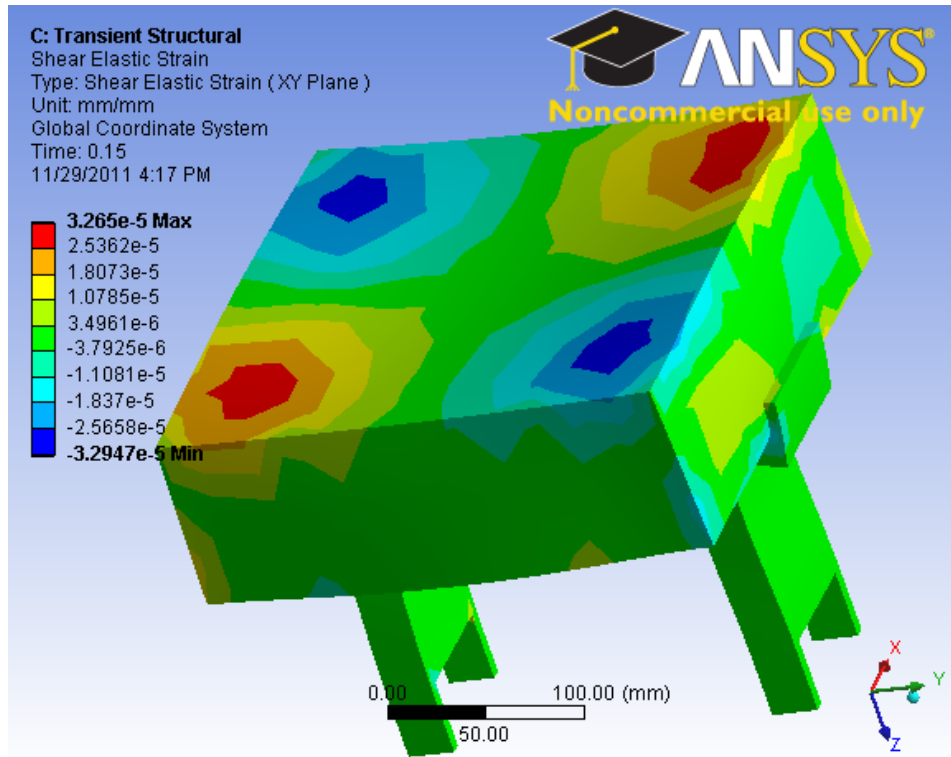


Figure 48. Shear strain in XY plane on Al box and PCB card.

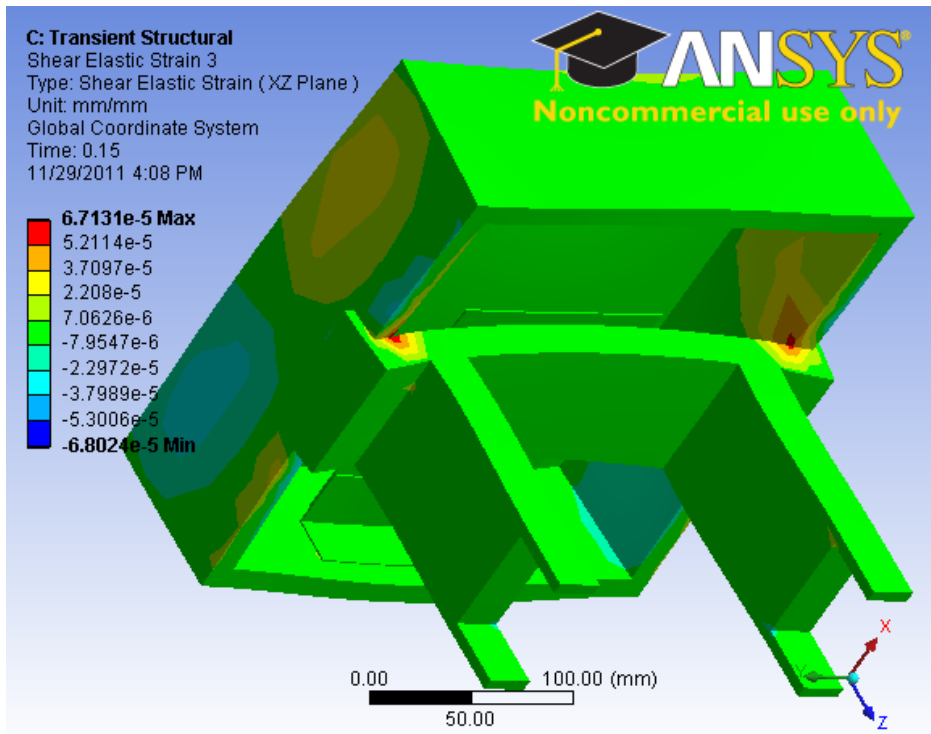
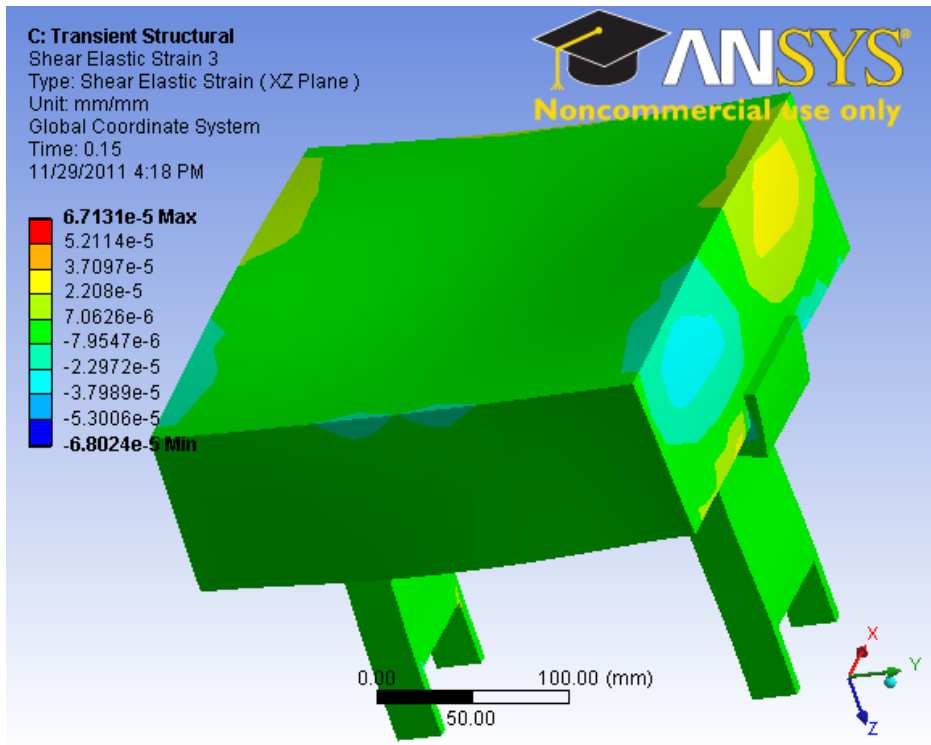


Figure 49. Shear strain in XZ plane on Al box and PCB card.

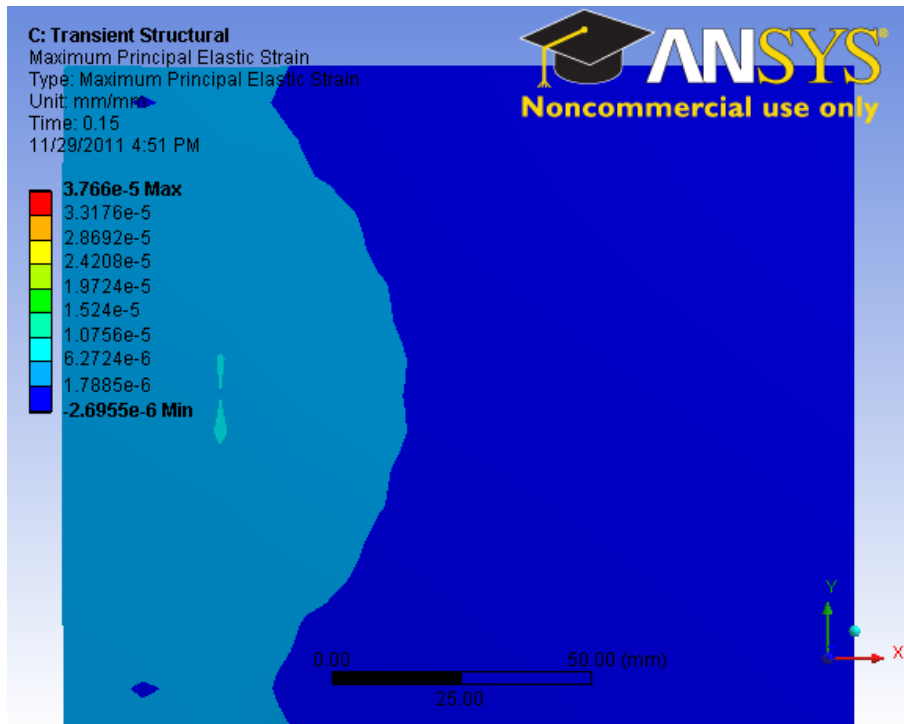


Figure 50. Max principal strain on PCB card.

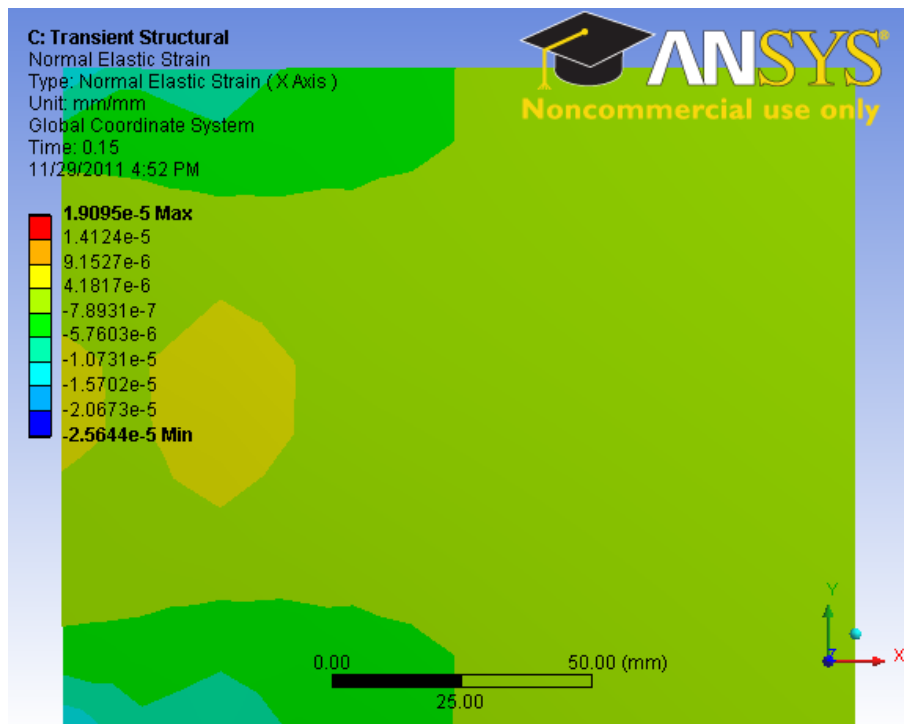


Figure 51. Normal strain in the longitudinal (X) axis on PCB card.

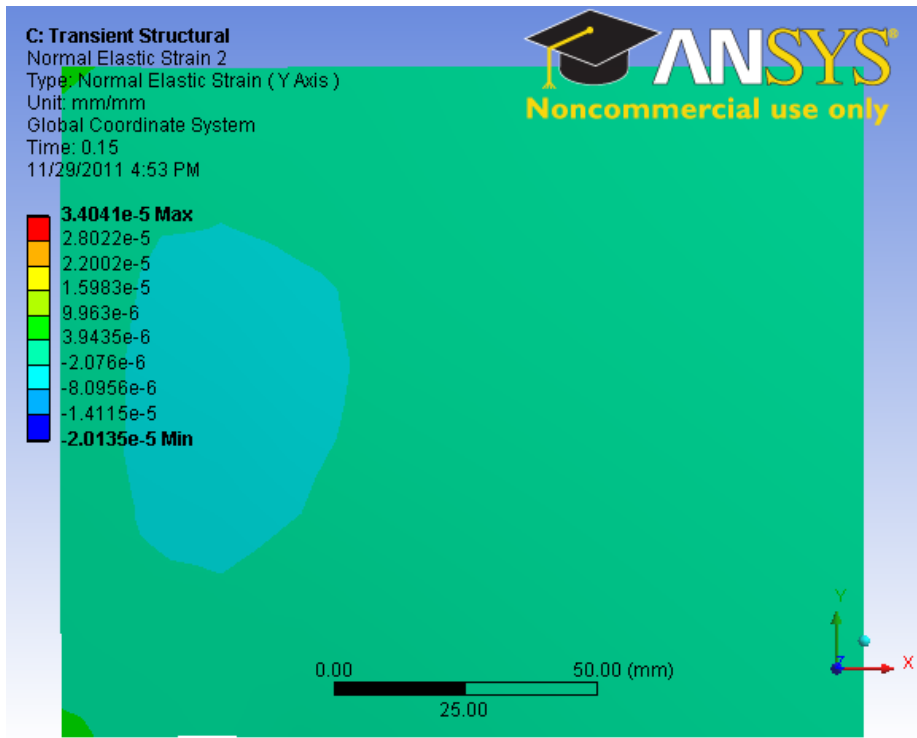


Figure 52. Normal strain in the lateral (Y) axis on PCB card.

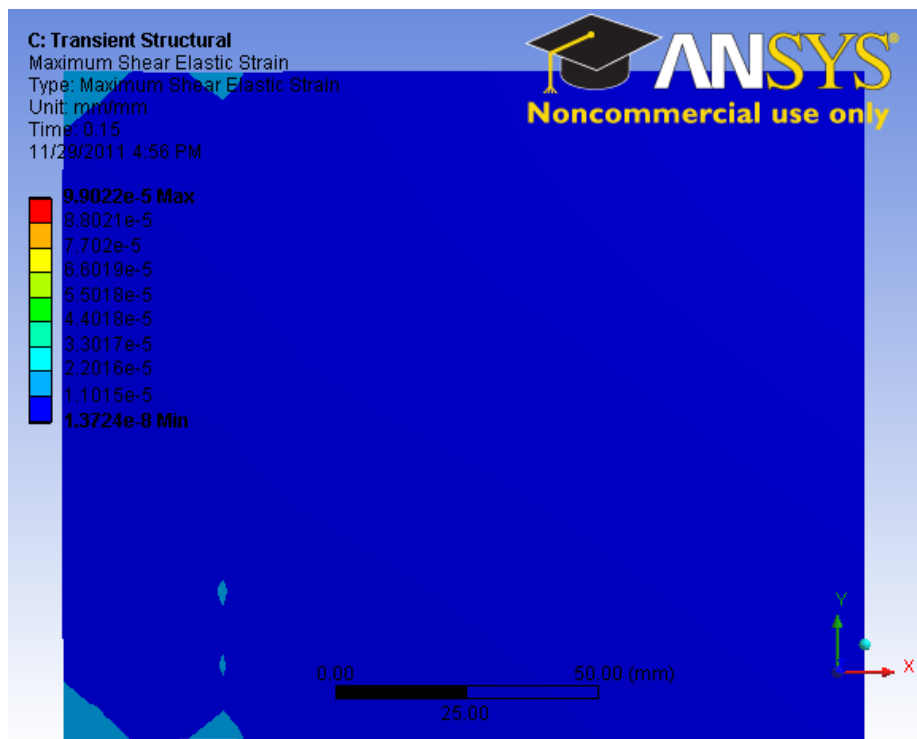


Figure 53. Max shear strain on PCB card.

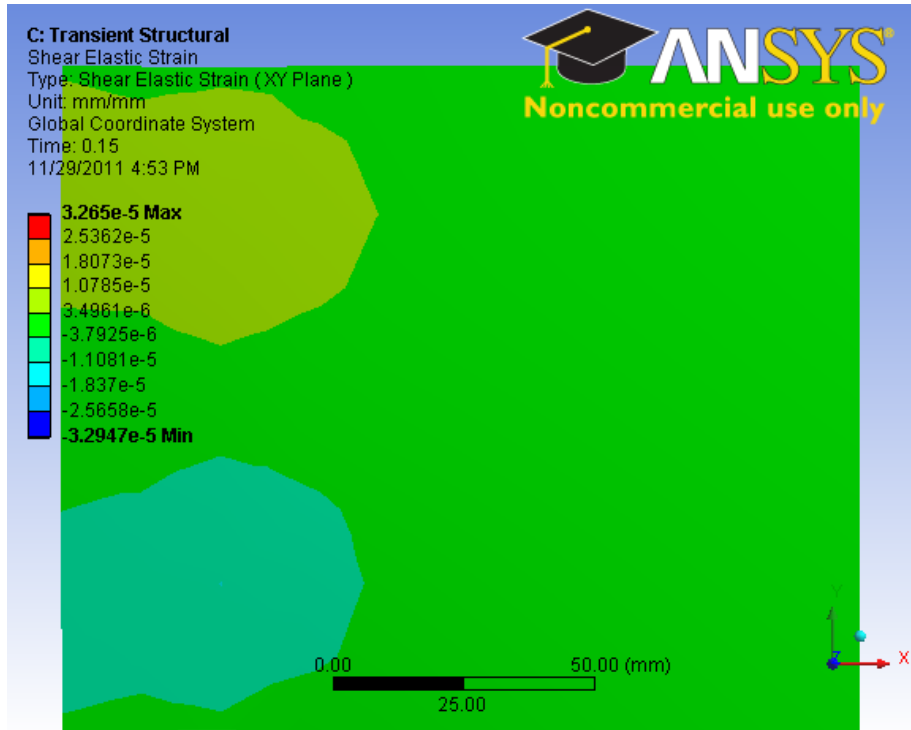


Figure 54. Shear strain in XY plane on PCB card.

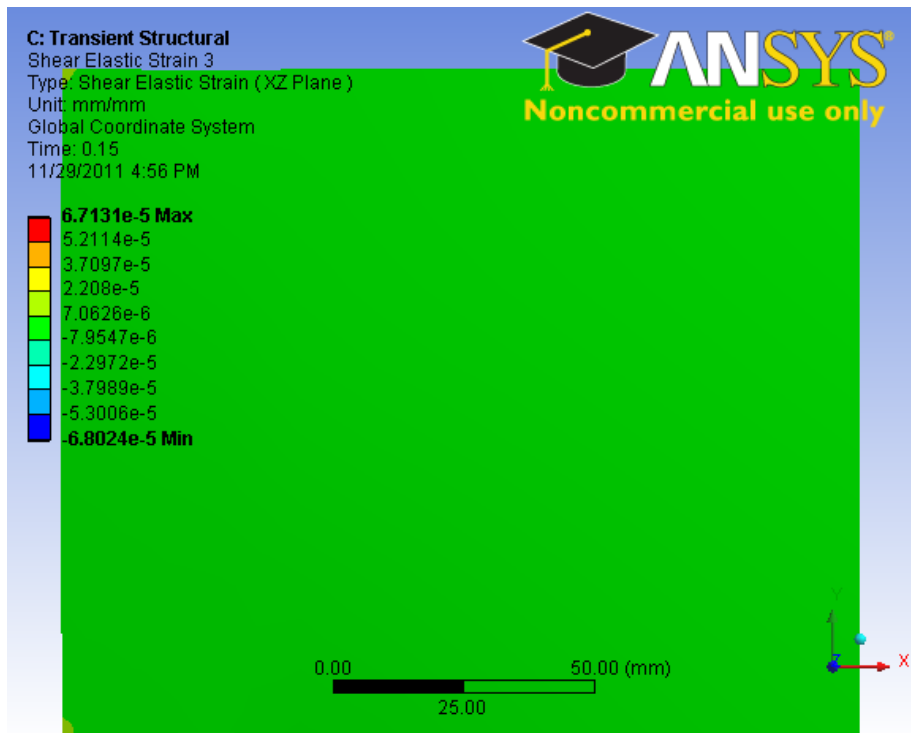


Figure 55. Shear strain in XZ plane on PCB card.

D. STRAIN RELATIONSHIP BETWEEN PCB CARD AND SOLDER JOINT

Establishing a relationship between strains in the PCB card and corresponding solder joints was a critical objective in this study. A FEM model's accuracy will greatly depend on the size or detail of the applied mesh. A very fine mesh can take days or weeks to solve. Solder joints present a difficult problem in the fact that they are often on the scale of 1.0 mm or less at their diameter. In the FEM model of the soldered electronic component, a 5 mm x 5 mm PCB card cutout was used for analysis. This zoomed in view of the card and component allowed a medium sized mesh to provide accurate results.

The reason this model worked was the minimal size difference between the solder joints and the PCB card cutout. A very specific location and value for strain were known from experimental testing, and this allowed a corresponding deformation to be applied at a precise point on the FEM model. In order to find accurate results using this zoomed in approach, an additional FEM model would need to be created for every location of known strain. This method is extremely time intensive and unrealistic in large scale applications.

The second FEM model of the AI box and the mounted PCB card did not include any solder joints. Since the model was built to the exact specifications of the experimental test platform, the size difference between the PCB card and individual solder joints would have been too great to apply an accurate mesh. Therefore, establishing a strain relationship would allow this second model to provide PCB card strain values corresponding potential solder joints in the same location.

A theoretical strain relationship was developed. Figure 56 shows this relationship between the normal and shear strains in the PCB card and corresponding solder joints.

- Relationship between PCB and solder joint strains

$$\begin{aligned} \epsilon_{sx} &= e_{px} & s &= \text{solder joint} \\ \epsilon_{sy} &= e_{py} & p &= \text{PCB card} \\ \gamma_{sxy} &= e_{px} + e_{py} & a &= 1.0 \text{ mm (diameter of solder joint)} \\ \gamma_{syz} &= e_{py}(a/h) & h &= 0.5 \text{ mm (height of solder joint)} \\ \gamma_{sxz} &= e_{px}(a/h) & & \end{aligned}$$

Figure 56. Theoretical relationship between normal and shear strains in PCB cards and corresponding solder joints.

The solder joint average strain values were collected from the FEM analysis of the soldered electronic component. Each ANSYS™ image provided a range of strain values at each solder joint. These values were interpolated and input into the strain relationships. Table 11 shows the results of this comparison between the theoretical and the ANSYS™ FEM model of the soldered electronic component. As the results show, the differences found between the theoretical and ANSYS™ values were very small. What little error that does exist can be attributed to the average values of strain collected from the ANSYS™ images. Therefore, the theoretical strain relationships have been validated by the FEM model, and a relationship has been established between PCB card and solder joint strain.

Analysis Method	ϵ_y ($\mu\epsilon$)	ϵ_x ($\mu\epsilon$)	γ_{xy} ($\mu\epsilon$)	γ_{yz} ($\mu\epsilon$)
Theoretical	11.40	1.05	12.50	22.80
ANSYS™	12.20	1.06	11.50	22.10

Table 11. Theoretical and ANSYS™ strain comparison.

V. CONCLUSIONS AND RECOMMENDATIONS

Testing was conducted in order to analyze the effects of impact loading on electronic component failure. An existing impact test platform was modified to incorporate the use of an Al test box. This design and modification allowed for both impact testing for PCB card strain as well as solder joint failure. Experimental impact testing for strain revealed an approximately linear relationship between longitudinal strain and added weight, where lateral strain remained constant throughout. In addition, analytical results from the FEM model of the soldered electronic component have verified a valuable theoretical relationship between strain in a PCB card and corresponding solder joints. Though a failure criteria was not established by means of experimental impact testing, the FEM model of the Al box and PCB card will allow improvements and optimizations for future impact study.

The current study may be extended in the following ways:

- (i) Further FEM modeling should be conducted to modify existing impact test apparatus, in order to produce solder joint failure and develop failure criteria.
- (ii) Extensive testing should be conducted on various electronic components and solder joint methods, to include a variation in size and orientation.
- (iii) Analyze the effects of underwater impact loading on solder joint failure.

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