



Calhoun: The NPS Institutional Archive

DSpace Repository

Theses and Dissertations

1. Thesis and Dissertation Collection, all items

1976-12

Determination of the blade-element performance of a small transonic rotor.

Hawkins, Wayne Randolph

Monterey, California. Naval Postgraduate School

https://hdl.handle.net/10945/17727

This publication is a work of the U.S. Government as defined in Title 17, United States Code, Section 101. Copyright protection is not available for this work in the United States.

Downloaded from NPS Archive: Calhoun



Calhoun is the Naval Postgraduate School's public access digital repository for research materials and institutional publications created by the NPS community. Calhoun is named for Professor of Mathematics Guy K. Calhoun, NPS's first appointed -- and published -- scholarly author.

> Dudley Knox Library / Naval Postgraduate School 411 Dyer Road / 1 University Circle Monterey, California USA 93943

http://www.nps.edu/library

DETERMINATION OF THE BLADE-ELEMENT PERFORMANCE OF A SMALL TRANSONIC ROTOR

Wayne Randolph Hawkins

DUDLEY KNOK LUBRARY NAVAL POSTBRADUATE SCHOOL MONTERCY, CA 53940

NAVAL POSTGRADUATE SCHOOL Monterey, California



THESIS

DETERMINATION OF THE BLADE-ELEMENT PERFORMANCE OF A SMALL TRANSONIC ROTOR

by

Wayne Randolph Hawkins

December 1976

Thesis Advisor:

R. P. Shreeve

Approved for public release; distribution unlimited.

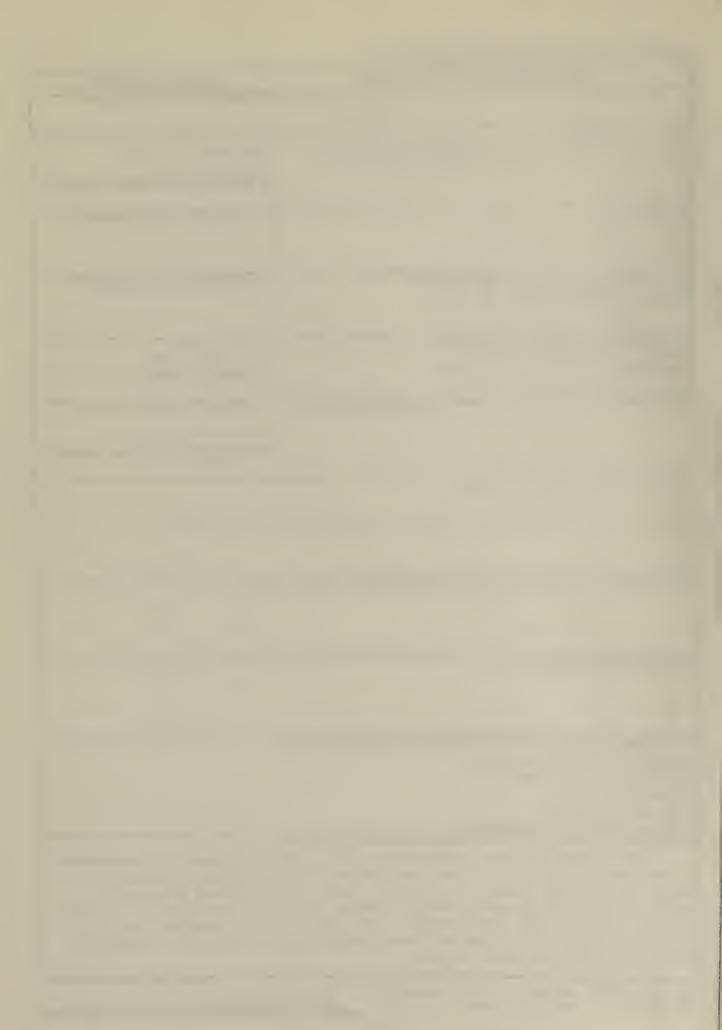
T176657





SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered) READ INSTRUCTIONS BEFORE COMPLETING FORM **REPORT DOCUMENTATION PAGE** . REPORT NUMBER 2. GOVT ACCESSION NO. 3. RECIPIENT'S CATALOG NUMBER 4. TITLE (and Subitite) S. TYPE OF REPORT & PERIOD COVERED Determination of the Blade-Element Per-Master's Thesis formance of a Small Transonic Rotor December 1976 6. PERFORMING ORG. REPORT NUMBER 7. AUTHOR(.) 8. CONTRACT OR GRANT NUMBER(4) Wayne Randolph Hawkins 9. PERFORMING ORGANIZATION NAME AND ADDRESS Naval Postgraduate School 10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS Monterey, California 93940 11. CONTROLLING OFFICE NAME AND ADDRESS 12. REPORT DATE Naval Postgraduate School December 1976 Monterey, California 93940 13. NUMBER OF PAGES 14. MONITORING AGENCY NAME & ADDRESS(If different from Controlling Office) 15. SECURITY CLASS. (of this report) Unclassified 154. DECLASSIFICATION/DOWNGRADING SCHEDULE 16. DISTRIBUTION STATEMENT (of this Report) Approved for Public Release: Distribution Unlimited 17. DISTRIBUTION STATEMENT (of the abstract antered in Block 20, If different from Report) 18. SUPPLEMENTARY NOTES 19. KEY WORDS (Continue on reverse side if necessary and identify by block number) Compressor measurements. Transonic compressor Flow probes Pneumatic probes Blade-element performance 20. ABSTRACT (Continue on reverse side if necessary and identify by black number) The blade-element performance of a small transonic compressor rotor operating at high subsonic speeds is reported. Measurements were made downstream using a small calibrated pneumatic probe, with simultaneous measurements of total pressure, velocity, turning angle, and temperature. In addition, a program is presented to calculate blade-element performance based on empirical data contained in NASA SP-36.

Unclassified



Determination of the Blade-Element Performance of a Small Transonic Rotor

by

Wayne Randolph Hawkins Lieutenant, United States Navy

Submitted in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE IN AERONAUTICAL ENGINEERING

from the

NAVAL POSTGRADUATE SCHOOL December 1976



DUDLEY WHEN LA

ABSTRACT

The blade-element performance of a small transonic compressor rotor operating at high subsonic speeds is reported. Measurements were made downstream using a small calibrated pneumatic probe, with simultaneous measurements of total pressure, velocity, turning angle, pitch angle, and temperature. In addition, a program is presented to calculate blade-element performance based on empirical data contained in NASA SP-36.



TABLE OF CONTENTS

I.	INTR	ODUCTI	ON	14
II.	TRAN	ISONIC (COMPRESSOR	16
	A.	DESCRI	PTION	16
	В.	INSTRU	MENTATION	17
	С.	DATA A	CQUISITION AND REDUCTION	19
III.	METH	IOD OF	APPROACH	20
	Α.	METHOD	• • • • • • • • • • • • • • • • • • • •	20
	Β.	INLET	FLOW FIELD REPRESENTATION	21
	C.	PROGRAI	M OF MEASUREMENTS	23
IV.	RESU	LTS AN	D DISCUSSION	24
	Α.	TIME A	/ERAGED FLOW FIELD	24
	Β.	DEVIAT	ION ANGLES	25
	С.	LOSSES	• • • • • • • • • • • • • • • • • • • •	27
V.	CONC	LUSION	5	30
Append	lix A	.: BLAI	DE ELEMENT PERFORMANCE PREDICTION	56
	A.1	INTRO	DUCTION	56
	A.2	METHO	D	57
		A2.1	Two-Dimensional Incidence Angle	57
		A2.2	Two-Dimensional Deviation Angle	58
		A2.3	Correction for Three-Dimensional	
			Effects	59
		A2.4	Loss Coefficient	59
	A.3	POLYN	OMIAL REPRESENTATION OF CORRELATIONS.	60
	A.4	COMPU	IER PROGRAM	62
		A4.1	Description	6.2

A4.	2 Operation		••••	63
Appendix B: C	ALIBRATION AND	CORRECTION OF	PNEUMATIC	
F	PROBES		• • • • • • • • • • •	82
B.1 FRE	E JET APPARATUS	• • • • • • • • • • • • • • • •		82
B.2 CAI	JIBRATION OF THE	COMBINATION P	ROBE	83
B.3 BOU	JNDARY EFFECT ON	COMBINATION P	ROBE	
MEA	SUREMENTS	• • • • • • • • • • • • • • • •		85
B.4 COM	BINATION PROBE	MEASUREMENTS I	N STEADY	
SWI	RLING FLOW		• • • • • • • • • • •	87
B.5 CAI	JERATION OF THE	WEDGE PROBE		88
Appendix C: I	NLET FLOW FIELD	DETERMINATION	• • • • • • • • • • •	102
C.1 MET	HOD OF APPROACH		• • • • • • • • • • •	102
C.2 APF	LICATION	•••••		104
Appendix D: R	OTOR LOSSES			109
D.1 NAS	A LOSS COEFFICI	ENTS		109
D.2 DIF	FUSION FACTOR		••••	112

LIST OF TABLES

A1.	Coefficient Values for Slope Factor m	65
A2.	Reduction Coefficients	66
A3.	NASA36 Program Listing	67
A4.	NASA36 List of Variables	77
B1.	Coefficients for Combination Probe Calibration Free of Boundary Effects	90
B2.	Error Analysis of Velocity Measured by Combination Probe	91
C1.	Table of Flow Rates Used for Inlet Velocity Determin- ation	

-

LIST OF ILLUSTRATIONS

1.	The Compressor Test Rig	33
2.	Transonic Compressor Assembly	34
3.	Transonic Compressor Rotor Blading Design	35
4.	Photograph of the Combination Probe	37
5.	Drawing of the Wedge Probe	38
6.	Schematic of the Hewlett-Packard Model 9830A Calcu- lator Data-Reduction System	39
7.	Results of Probe Surveys Downstream of the Transonic Compressor Rotor Run 50 Point 3	40
8.	Results of Probe Surveys Downstream of the Transonic Compressor Rotor Run 52 Point 3	41
9.	Results of Probe Surveys Downstream of the Transonic Compressor Rotor Run 52 Point 23	42
10.	Results of Probe Surveys Downstream of the Transonic Compressor Run 52 Point 46	43
11.	Velocity Distribution Downstream of the Rotor Using the Combination Probe	44
12.	Pitch Angle Distribution Downstream of the Rotor Using the Combination Probe	45
13.	Static Pressure Distributions Downstream of the Rotor Derived Using the Combination Probe Calibration and Impact Pressure Measurement	
14.	Static Pressure Distributions Measured Downstream of the Rotor Using the Wedge Static Probe	47
15.	Boundary Effect Correction Applied to the Combination Probe Results	1 48
.6 a .	Velocity Triangles at Midstream for Run 50 Point 3	49
66.	Velocity Triangles at Midstream for Run 52 Point 3	50
.6 c .	Velocity Triangles at Midstream for Run 52 Point 23	51
.6d.	Velocity Triangles at Midstream for Run 52 Point 46	52

	17.	Deviation Angles from Probe Measurements and Calculations	53
	18.	Loss Coefficients for the Transonic Compressor Rotor	54
	19.	Diffusion Factor Correlation of Loss Coefficients	55
	A1.	Nomenclature of Cascade Blade	78
	A2.	Total-Pressure-Loss Coefficient vs. Incidence Angle	79
	A3.	Deduced Variations of Slope Factor M in Deviation Angle Rule for Circular-Arc-Mean-Line Blades	80
	A4.	Variation of Coefficients of Polynomial Curves in Fig. A3	81
	B1.	Free-Jet Apparatus Used to Calibrate Probes	92
	B2.	Velocity Profiles for Various Mach Numbers Measured in a 4.2 Inch Free-Jet	93
	B3.	Error in Pitch Angle Derived from the Combination Probe Calibration	94
	в4.	Distribution of Velocity Measured in a 10 Inch Pipe Flow	95
	35.	Error in Velocity Due to Boundary Effects in a 10 Inch Pipe Flow	[.] 96
	в6.	Coefficients for Boundary Effect Correction	97
	В7.	Magnitude of the Correction in Velocity Resulting From Boundary Effect	98
	B8.	Error in Pitch Angle Due to Boundary Effect in a 10 Inch Pipe Flow	99
	В9.	Photographs of Swirl Annulus	100
I	310.	Static Pressure Measured by the Combination Probe in a Steady Swirling Flow	101
	C1.	Total Flow Function vs. Normalized Displacement Up- stream of the Rotor	106
	C2.	Normalized Flow Function vs. Normalized Displacement Upstream of the Rotor	107
	03.	Flow Function at Mid Span vs. Referred Flow Rate	108

TABLE OF SYMBOLS

Latin

- a Speed of sound based on stagnation conditions, ft./sec.
 - C Chord length
 - D Diffusion factor
 - F6 Combination probe calibration factor
 - Fe Combination probe calibration factor
- D_m Diameter of rotor profile
 - E Chord with sharp leading and trailing edges
 - H Angle of cone through stacking radius
 - i Incidence angle; angle between inlet-air direction and tangent to blade mean camber line at leading edge, degrees.
- (i₀)₁₀ Zero-camber reference minimum-loss incidence angle

(iref)2-D Two-dimensional reference incidence angle

- i_{3-D} Three-dimensional reference incidence angle
- $(K_{k})_{SH}$ Correction for blade shape
 - $(K_{i})_{+}$ Correction for blade thickness
 - (K_i)_t Correction for the effect of blade thickness for zero-camber reference minimum-loss incidence
 - $(K_{\delta})_{t}$ Correction for effect of blade thickness for zero-camber reference deviation angle
 - m Slope factor for circular-arc-mean line blades
 - M Mach number
 - M₁, Relative Mach number
 - n Slope factor in incidence-angle relation
 - P Pressure

R	Blade
S	Blade spacing
t	Blade maximum profile thickness
T	Temperature
U	Tangential rotor velocity
V	Velocity
W	Relative Velocity
**	Referred flow rate
Х	Non-dimensional or limiting velocity
Greek	
Δ	Finite difference
α	Angle of attack, angle between inlet-air direction and blade chord; or, flow angle with respect to axis
ę	Air angle, angle between air velocity and axial direction.
X	Stagger angle
۶'	Ratio of specific heats
8	Deviation angle, angle between outlet-air direction and tangent to blade mean camber line at trailing edge
(Sref) _{2-D}	Reference two-dimensional deviation angle
б 3-D	Three-dimensional deviation angle
E	Fractional error
Ø	Flow pitch angle
ø	Blade camber angle
୧	Density of air
σ	Blade solidity
Ð	Flow function

$\overline{\overline{\Phi}}$ Normalized flow function $\overline{\omega}'$ Rotor loss coefficient

Subscripts

.

CL	Centerline value
i	i th value
ref	Reference
t	Total or Stagnation value
1	Upstream of the rotor
2	Downstream of the rotor

ACKNOWLEDGMENT

The experimentation and analysis reported in this paper would not have been possible without the endless counseling and guidance of my thesis advisor, Associate Professor R. P. Shreeve. I wish to express my gratitude for his seemingly infinite patience and genuine interest in this field.

The preparation of experiments, calibration of equipment, and overall technical expertise were provided by Mr. J. E. Hammer. His practical knowledge, coupled with an engineering background, made the transition from theory to application a much simpler process.

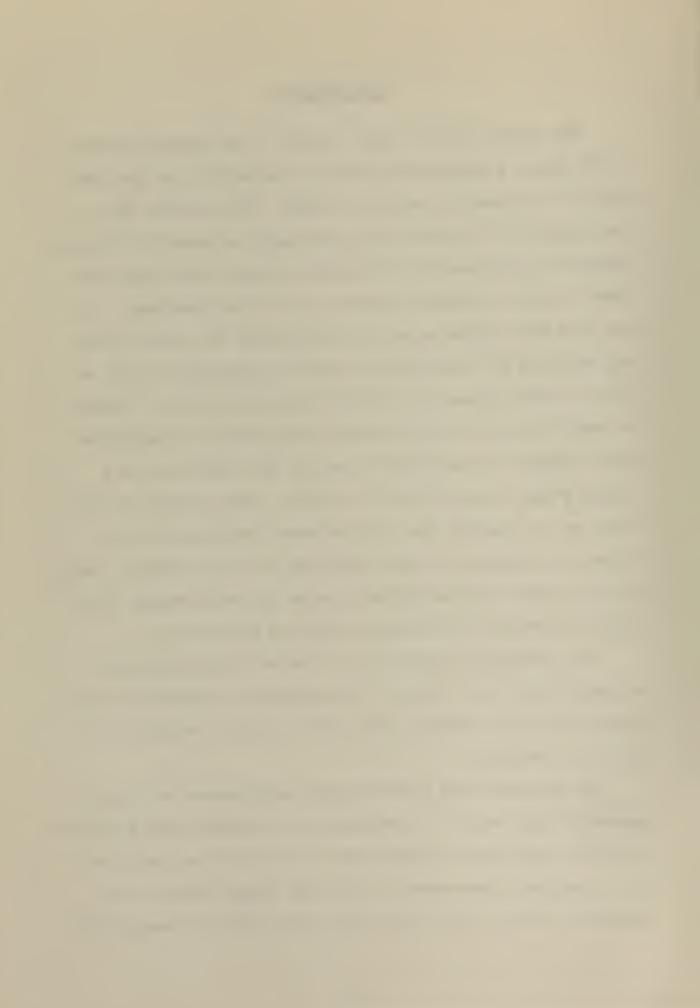
- -

I. INTRODUCTION

The study reported here is part of an ongoing program at the Naval Postgraduate School to determine the performance of a transonic compressor stage. The overall goal of the program is to develop the knowledge necessary to design compressors with multiple transonic stages which are efficient, light in weight, and free of flutter problems. It has long been appreciated that increasing the wheel speed and relative air velocities in axial compressors would result in fewer stages for a given energy addition. However. in order to achieve high overall efficiencies in multiple axial stages, the ability to predict the behaviour of a single stage correctly must be shown. The purpose of this study was to measure the blade-element performance of a transonic compressor rotor operating at high subsonic speeds and to compare the measurements with the performance calculated according to the method given in Reference 1.

The transonic compressor and drive turbine were designed by Dr. M. H. Vavra. The program is supported by the Naval Air System Command, Code 310, through the office of Dr. H. J. Mueller.

To determine the blade-element performance of a compressor blade row, it is necessary to evaluate radial veloc-ity and angle distributions into and out of the blade row. In a transonic compressor, at or near design speed, the unsteady nature of the flows with large pressure amplitudes



complicates the problem. In addition, the possibility that wakes might induce vibrations in the highly stressed blades prohibit the use of probes upstream of the rotor. Measurements can be made downstream of the rotor; however, since the flow area is small, boundary effects on probe measurements can be significant.

In order to carry out the present study, a small combination temperature-pneumatic probe was designed by Dodge (Ref. 2) specifically to be used immediately downstream of the rotor. In previous work, the flow upstream of the rotor was determined at different flow rates (Ref. 3). It was left to the present work to represent the inlet flow field analytically, to calibrate the combination probe for boundary effects, and both to measure and to calculate the rotor blade element performance.

In this report the transonic compressor and test rig are first described in Section II. The method of approach and program of measurements are described in Section III.

The results of the measurements are then described and discussed in Section IV, and conclusions are given in Section V. In order to maintain a clear presentation of the relevant results, the details of the calculations and of the calibration measurements are given in separate Appendices.

II. THE TRANSONIC COMPRESSOR

A. DESCRIPTION

A drawing of the compressor test rig is shown in Fig. 1. The test rig consists of an air-turbine drive unit and an induction section containing a filter, a throttle, a settling chamber and a flow measuring nozzle. The air turbine is designed to deliver 450 horsepower at 30,000 RPM. The relative blade tip Mach number of the rotor at design point is 1.5. The compressor flow rate is controlled by an electric-hydraulic rotating throttle plate. Power is provided by a compressed air supply from an Allis-Chalmers multistage axial compressor. A complete description of the Turbopropulsion Laboratory and test facilities is contained in Ref. 4. A drawing of the transonic compressor is shown in Fig. 2.

The blade design for the transonic compressor rotor was derived from circular-arc elements wrapped on six conical surfaces. The outer surface (at the case wall) is a cylinder. The blading geometry is given in Fig. 3. The blade pressure side is flat and the suction side is a circulararc. The solidity is fairly constant with a value of 1.35 at the mid-streamline. The outer diameter of the rotor blade is 11 inches with a channel height of 1.92 inches downstream and a radius ratio at the inlet face of 0.5.

B. INSTRUMENTATION

The transonic compressor is equipped with stationary probes to provide routine performance data. Triple redundancy is provided in the measurement of the power; either the mass flow rate and temperature drop through the drive turbine, or the mass flow rate and temperature increase through the compressor, or the speed and the measurement of torque can be used. The torque is measured by strain gauges on flexures against which the stator assembly is free to rotate. Flow straighteners before and after the stage ensure that the stator and rotor torques are equal. The method based on torque and speed is the most accurate since it is independent of flow profiles. Static pressure taps were installed on both outer and inner walls of the compressor casing. The rotative speed of the test rotor was determined by a magnetic flux cutter and electronic counter. The fixed instrumentation will not be described further. It was used in the present tests only to provide the reference conditions for the survey measurements. The compressor cylindrical casing was modified to accommodate a variety of probes and sensors which may be required in the program of steady state and unsteady flow pressure measurements. The casing can be rotated to position probes in the peripheral direction.

The rotor exit survey measurements reported here were obtained using a combination probe (Fig. 4) designed by Lt. F. J. Dodge (Ref. 2). The combination probe, following

calibration, was used to determine total pressure rise, total temperature rise, and flow velocity in magnitude and direction. In addition, static pressure was measured using the wedge static probe shown in Fig. 5, which was based on a NASA design provided by Mr. Lloyd N. Krause of NASA Lewis Research Center. Each probe had two "static pressure" sensors which, if the probes were rotated until the indicated static pressures were equal, allowed the probes to be aligned with the flow direction. It was determined that better accuracy could be attained, however, by aligning both probes to the flow direction sensed by the combination probe. This was because the sensors on the wedge probe were separated in the radial direction. A chromel-constantan fine-wire thermocouple in the combination probe was used in conjunction with a similar sensor mounted upstream of the rotor to measure, differentially, the total temperature rise.

Radial surveys were taken at a fixed peripheral case angle by manually positioning the probe in the flow using a United Sensor traverse unit, manually rotating the combination probe to balance indicated static pressures, and adjusting the wedge probe to the same angle. All pressures were measured by a calibrated transducer in a Scanivalve arrangement. (A capability exists to remotely control probe movement and balancing through the use of a programmable microprocessor and a probe traversing mechanism designed by Lt. D. D. Patton (Ref. 5). Remote operations will be needed as higher operational speeds are developed.)

C. DATA ACQUISITION AND REDUCTION

Pressures, temperatures, rotational speed and other data were scanned and punched onto paper tape by a B & F Model 24133 solid state data acquisition system. A complete description of this system is contained in Ref. 4. The punched tape data was processed using Hewlett-Packard Model 9830A programmable calculator data system. The data was transferred to a Model 9867B mass memory disk unit for storage prior to data reduction. The data facilities are shown in Fig. 6.

A program, designated "WH001" was written to transfer raw data from tapes to the mass memory. A second program "HAWK1" was written to calculate temperature, corrected non-dimensional velocity, turning angle, total pressure, and static pressure. Two other programs, used in sequence ("REPR01" and "RA5C") completed the data reduction process. Plotting routines developed by Dr. R. P. Shreeve were adapted to plot distributions of Mach number, pressure rise, temperature rise, flow angle, and loss coefficients, using the X-Y plotter.

In reducing the probe measurements to obtain velocities and loss data, the thermocouple calibration reported in Ref. 2 was used. However, new pneumatic calibrations were performed and corrections were derived as described in Appendix B.

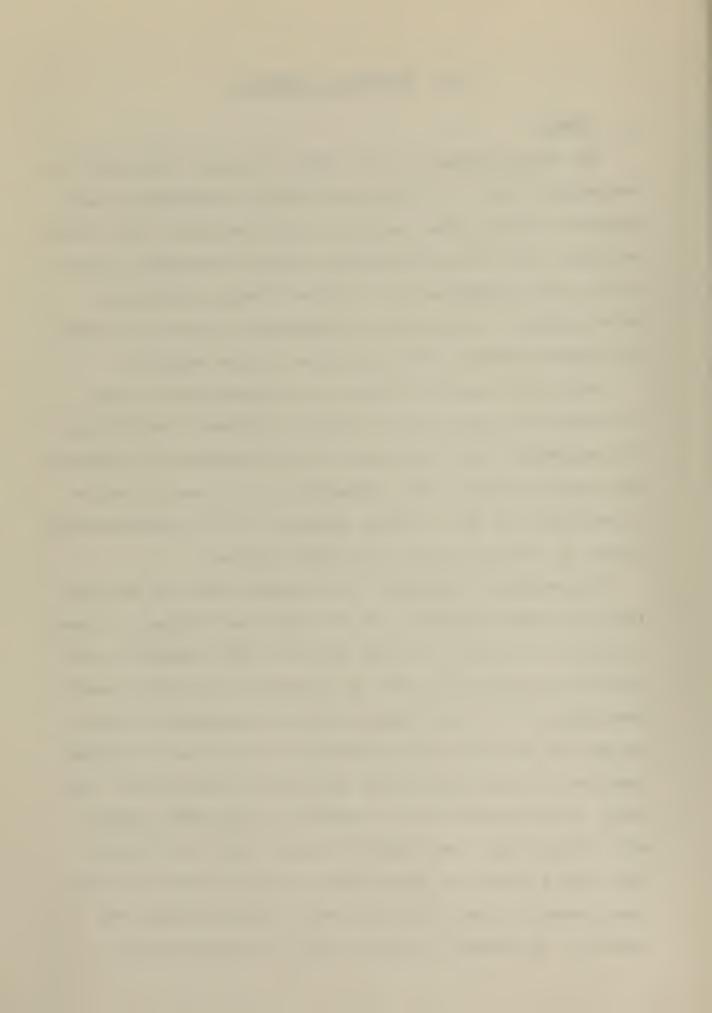
III. METHOD OF APPROACH

A. METHOD

The usual approach to the design of axial compressors is described in Ref. 1. The method involves combining an axisymmetric through-flow analysis, which prescribes the stream surfaces, with a two-dimensional cascade performance calculation which determines the required blading geometry on those surfaces. The blading is generally layed out on conical approximations of the prescribed stream surfaces.

When a new machine is built, the opportunity is there to compare the actual blade element performance established by measurement with that which can be calculated by applying the design approach. The comparison can be used to derive corrections for use in future designs, and it is particularly useful to obtain data for new blade profiles.

The transonic compressor investigated here was designed using the above approach, and the resulting blading is shown in Fig. 3. It is to be noted that the rotor blading is not typical in design. In order to establish the blade element performance of a rotor experimentally, measurements should be made of the flow into and out of the rotor on the stream surfaces on which the blading profiles are prescribed. However, it is desirable not to operate at high wheel speeds with strong wakes from upstream probes, and so in the present work a method of prescribing the inlet flow field from measurements of only total flow rate and wheel speed was derived. The method is given in the following section.



The flow downstream of the rotor was determined using two calibrated probes. The calibration and corrections required for the probes are described in Appendix B. From the rotor exit flow measurements, the blade element loss coefficient and the local deviation angle were calculated.

Finally, as described in Appendix A. the method of calculating deviation angle and loss coefficient given in Chapter 7 of Reference 1 was programmed for the Hewlett-Packard Model 9830A calculator so that these quantities could be computed for four blade element surfaces at any given compressor flow rate and operating speed.

B. INLET FLOW FIELD REPRESENTATION

The flow field ahead of the rotor was measured in early tests using a calibrated pneumatic probe (Ref. 3). The measurements were compared with the results of a compressible finite difference calculation reported in Reference 6, and blockage factors were derived to relate the inviscid calculations to the measured flow field.

The method adopted here was based only on Anderson's measured data. As described in Appendix C a polynomial relation was found to correlate the measured velocity distributions away from the hub and tip regions. The flow function in this region was therefore calculated using Eq. C(3) and Eq. C(7).

C. USE OF FLOW PROBES

Pressure probes are designed to exploit the distribution of pressure which occurs over a body immersed in a moving fluid. These pressure variations depend mainly on the flow velocity so that with a carefully selected choice of body shape, having multiple sensors, a probe can be calibrated to determine flow velocity. The relationship between pressure and velocity must be established over a range of Mach numbers. In addition to flow velocity in magnitude and direction, the distributions of stagnation temperature, and total and static pressure are usually required. The probe designed by Dodge and reported in Ref. 2 is a small lightweight probe of aerodynamic design which allows these quantities to be determined at any position in the flow.

In order to provide an independent measurement to compare with the combination probe, the static pressure distribution was measured with a second probe, and static pressures were also recorded at hub and tip wall taps. The wedge static probe shown in Fig. 5 has the favorable characteristic that when it is aligned with the flow in the yaw plane (by balancing the pressures measured on the wedge surfaces) the indicated static pressure is relatively insensitive to angle variation in the pitch plane. As reported in Ref. 7 this type of probe has been used successfully up to a Mach number of 1.6. Further, for measurements in the transonic regime the probe has favorable characteristics. If the leading edge is sharp and the wedge is small, Ref. 7 states that the

calibration is also independent of Mach number. This was found to be the case for the probe used in the present work.

D. PROGRAM OF MEASUREMENTS

The combination probe and the wedge static probe were mounted at the exit of the rotor with a peripheral separation of 120 degrees. Four surveys were conducted at 50 percent of design speed, at throttle conditions varying from near surge to maximum flow rate. Case angle for the first survey was 345 degrees. Subsequent surveys were conducted at a case angle of 357 degrees because it was determined that peripheral variations induced by the stator blading were felt least at this setting. RPM was the same $(15,230 \pm 30)$ for all four runs.

The procedure in each survey was to move the probes inward simultaneously, balance the combination probe to sense the flow angle, and then set the wedge probe to the measured angle. A data scan was taken, and the procedure was repeated at 0.1 inch intervals. Because of the hooked geometry of the wedge probe, measurements with this probe of static pressure could not be made closer than .6 inches to the outer wall boundary. Static pressures were derived for the complete passage through the use of the combination probe calibration. Wall static pressure measurements at the hub and tip were also recorded. Yaw angle and linear displacement were recorded manually. All other data were automatically recorded by the data recording system. Pressures were recorded to an accuracy of .1 inches of water.

V. RESULTS AND DISCUSSION

A. TIME-AVERAGED FLOW FIELD

The distributions of total pressure rise, total temperature rise, Mach number and flow angle measured using the combination probe downstream of the rotor are shown in Figs. 7, 8, 9, and 10.

The total pressure rise was nearly constant with radius, whereas the temperature rise was indicated to be larger toward the tip. The larger indicated temperature rise near the case wall might be caused by higher temperatures in the incoming case wall boundary layer. Both the Mach number and the flow angle increase toward the hub, so that the through-flow velocity tends to remain constant. The results for the flow angle are qualitatively consistent; however, a large decrease can be observed in the magnitude of the flow angle for the open throttle case (Fig. 8). No definitive explanation was found, but as will be shown later this measurement leads to inconsistencies in the correlation of blade element performance.

The velocity and pitch angle distributions, which were derived from the probe calibration and corrected for boundary effects (Appendix B), are shown in Fig. 11 and Fig. 12. The pitch angle shows a smooth variation between the values of the wall slopes at the hub and tip boundaries. It is shown in Appendix B that the pitch angle is determined to only $1\frac{1}{2}^{\circ}$ accuracy, so that the variations in pitch angle indicated in Fig. 12 might be exaggerated.



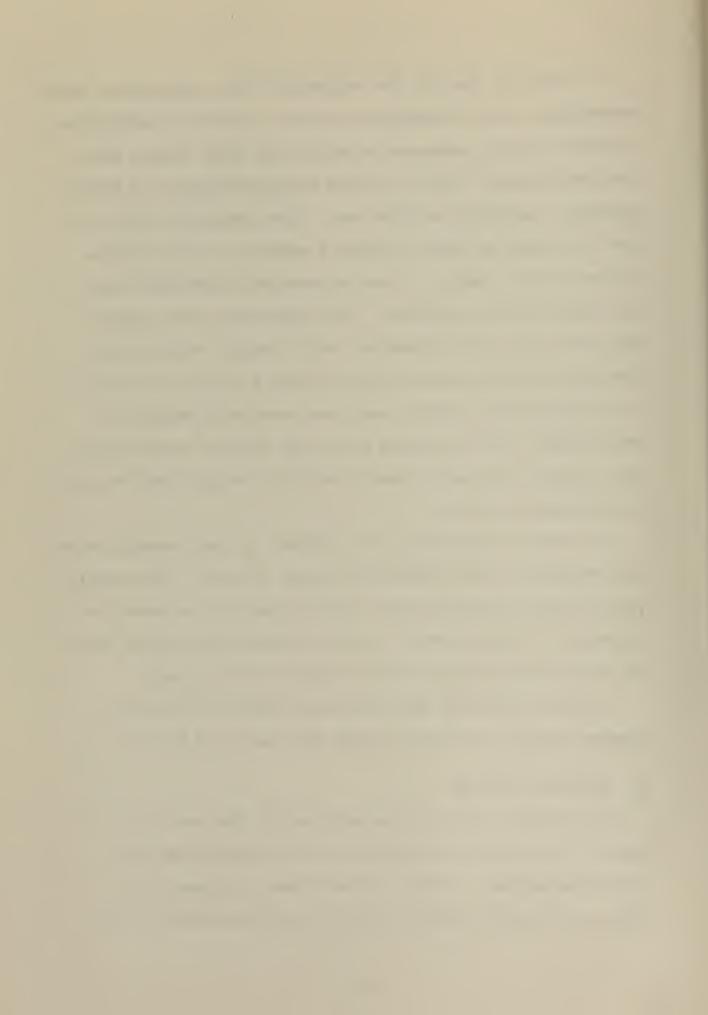
A sensitive test of the accuracy of the combination probe measurements was to examine the static pressure distribution inferred from the measured velocity and probe impact pressure measurement. Fig. 13 shows the distribution of static pressure calculated in this way. Also included in Fig. 13 are the values of static pressure measured at the hub and tip wall static taps. It can be seen that agreement near the case wall was excellent. The comparison near the hub wall was not as good; however, very similar results were obtained from the wedge probe as shown in Fig. 14. While no readings were possible near the outer wall using the wedge probe, the two probes gave very similar results near the hub wall, and gave almost identical results for the survey at open throttle.

As shown in Appendix B, the effect of flow boundaries on the readings of the combination probe is small. The magnitude of the correction which was included in the above results can be seen in Fig. 15. The correction is less than 1% in velocity over the useful range of the survey.

Velocity diagrams near the mean radius (0.55 of the channel height) are shown in the four parts of Fig. 16.

B. DEVIATION ANGLES

The design procedure for calculating the deviation angles for a given blade profile, with corrections for three-dimensional effects, is described in Appendix A. Blade profiles are known on four conical surfaces in the



flow field, on which the blading dimensions are those given in Fig. 3. Using relative flow angle β_2 from the velocity diagram data (Fig. 16 for example), the flow deviation angle (S) can be calculated from the stagger angle (Y) and camber angle (ϕ') using the relation

$$\delta = \beta_2 - \delta + \frac{\phi}{2}$$

The results for the four probe surveys are shown in Fig. 17 in comparison with the results of calculations following Ref. 1.

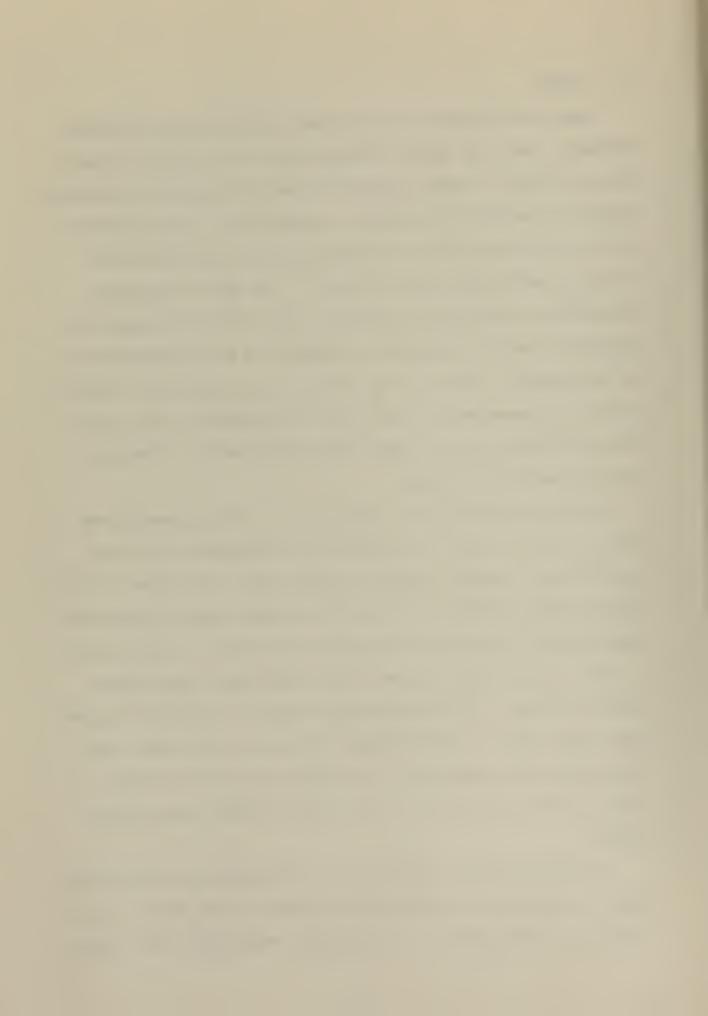
Departures from values predicted using Ref. 1 are quite large. However, the design procedure strictly applies only to the case where the operation is at the point of minimum loss for the given blade element. A closer correlation might be expected as the higher operating levels are achieved and closer to design conditions are attained. (Ref. 1 states that at transonic inlet Mach number levels, the point of minimum loss should constitute the desired design setting.) It is noted that the through-flow velocity is considerably increased through the rotor at the 50% design speed setting, and this would effect the deviation angle. No explanation was found for the indication of negative values of deviation angle near the hub, although a careful check was made on the accuracy of the probe yaw angle measurements and on the accuracy of the data reduction program. It must tentatively be concluded that there are strong three-dimensional effects present which can lead to the indication (locally) of negative deviation angles. More data must be obtained to investigate this speculation. 26

C. LOSSES

Loss coefficients for the flow over the blade elements, assuming that the stream surfaces were the conical surfaces given in Fig. 3, were calculated from the probe measurements using the methods described in Appendix D. The calculated loss coefficient ($\bar{\omega}'$) was consistent with the definition of loss coefficient used in Ref. 1. Of the two methods described in Appendix D, Method 1 uses both the stagnation pressure rise and stagnation temperature rise measurements of the probe. Method 2 does not use the stagnation temperature rise measurement, but uses a temperature rise calculated from the velocity and angle measurements, through Euler's turbine equation.

The results are shown in Fig. 18. Good agreement was obtained between the two methods of calculating the loss coefficient, however negative values were calculated for the inner stream surface. It should be noted that all measured data and all blade properties varied smoothly with radius, so that smooth curves between the individual data values could be drawn. The distributions are in qualitative agreement with earlier measurements, and it is noted that negative values of losses were previously reported by Dodge (Ref. 2) from measurements made with the same combination probe.

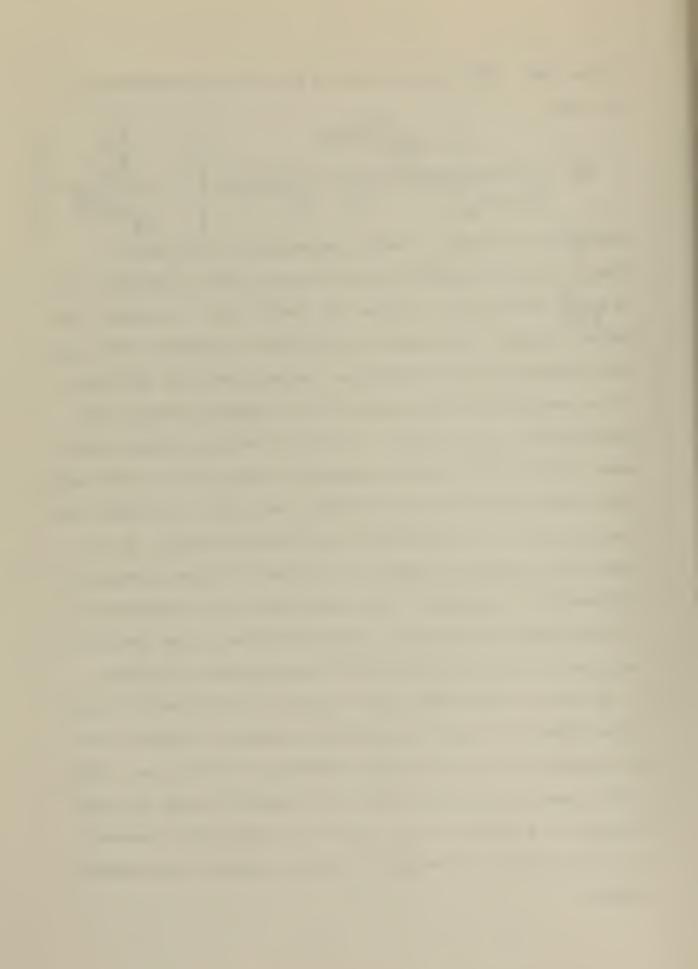
A negative value of the loss coefficient can result only from a measurement of stagnation pressure rise which is too high, or a measurement of stagnation temperature rise which



is too low. This can be seen if Eq. D(13) is rewritten in the form

$$\tilde{\omega}' = \frac{\left[1 + x_{u_2}^2\right]^{\frac{p}{2}}(\frac{q}{1-1})}{\left[1 + x_{u_2}^2\right]^{\frac{p}{2}}(\frac{q}{1-1}) - \left[1 - x_1^2\right]^{\frac{p}{2}}(\frac{q}{1-1})} \left\{ \begin{array}{c} \frac{P_{t_2}}{P_{t_2}} \\ 1 - \frac{P_{t_2}}{\frac{P_{t_2}}{\frac{q}{2}}} \\ \frac{p}{\sqrt{q}}(\frac{2\frac{q}{2}}{\sqrt{q-1}}) \end{array} \right\}$$

where Ψ is the ratio of total temperatures, (T_{t_2}/T_{t_1}) . Clearly, since X_{u_2} and X_{u_1} are positive, $\bar{\omega}'$ is negative only if $\frac{28}{8-1} > (P_{t_2}/P_{t_1})$. Since the prediction of Method 1 and Method 2 agree, and because a favorable comparison with earlier unreported measurements of temperature rise was made. it is tentatively concluded that the impact pressure rise measurement is too large. A positive error in impact pressure could result from the pneumatic integration of the periodic unsteadiness of the flow from the rotor. All parts of the probe are the open ends of continuous tubing. It is known that pneumatic probes of different designs integrate differently in periodic flow conditions. An investigation of the pneumatic averaging characteristics of the probe is required in order to correct the measurements of losses. It should be noted that the velocity and pitch angle calculated from the time-averaged probe readings should not be as sensitive to the averaging behaviour of the probe. This is because all parts are made from similar tubing and will average in a similar way. The loss coefficient, however, is very sensitive to errors in impact pressure measurement alone.

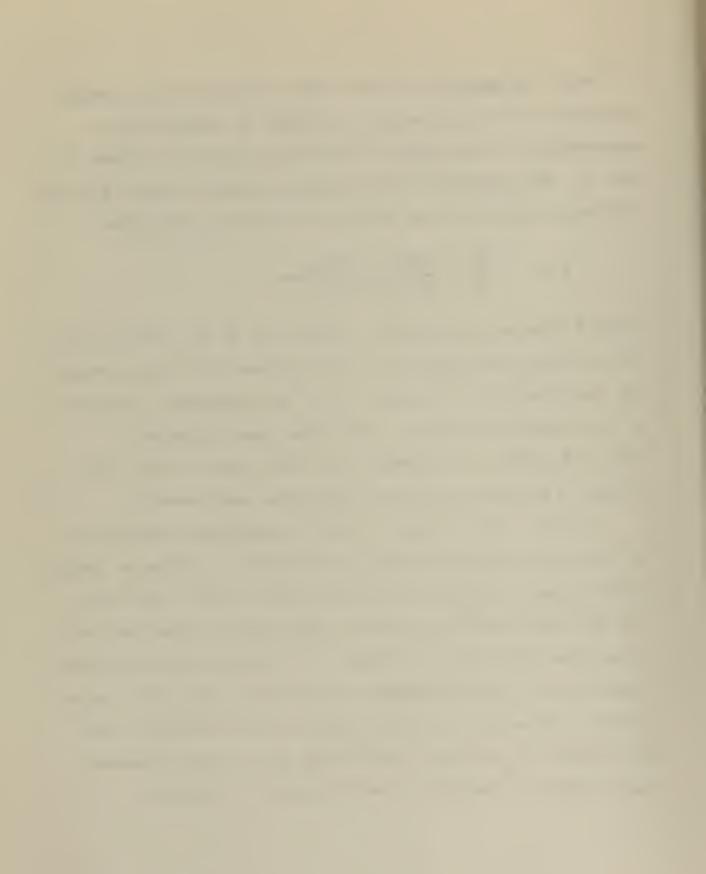


While the magnitude of the loss coefficients is clearly in error, it is of interest to attempt to correlate the measurements on the basis of diffusion factor as defined in Ref. 1. The result of this attempt is shown in Fig. 19. The diffusion factor (D) was calculated from the definition

$$D = 1 - \frac{W_2}{W_1} + \frac{R_1 W_{u1} + R_2 W_{u2}}{\sigma (R_1 + R_2) W_1}$$

where W denotes the relative velocity, R is the radius, σ is the solidity and subscripts 1 and 2 denote stations upstream and downstream of the rotor. W_u is the peripheral component of the relative velocity. The "total loss parameter", $(\bar{\omega}'\cos \beta_2/2\sigma)$ is consistent with that shown in Fig. 203 of Ref. 1 and was calculated from probe measurements.

It can be seen in Fig. 19 that a reasonable correlation of the loss coefficient data on the basis of diffusion factor was obtained for three of the four sets of data. The data for full open throttle departed significantly from the data from three other test conditions. It should now be recalled that the flow angles measured for this test were also inconsistent. More data is again needed, and a correction must be devised for unsteady flow effects on the probe measurements before a complete correlation can be obtained.



VI. CONCLUSIONS

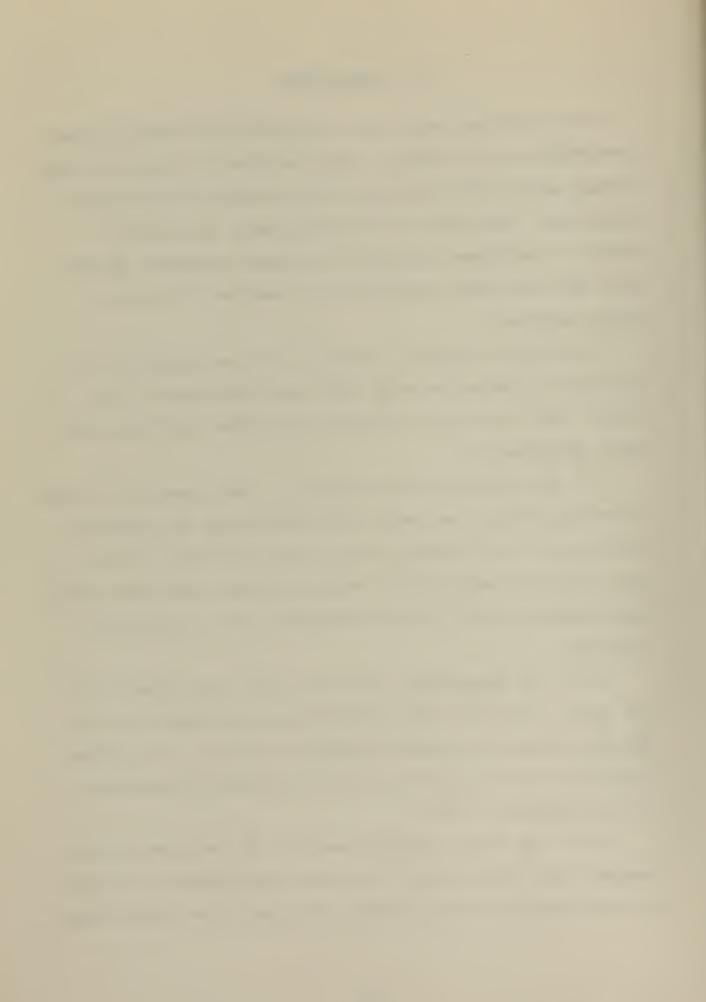
The attempt was made here to determine the blade element performance of an "impulse" rotor designed for transonic flow (design point) but operating at high subsonic (off-design) conditions. The results were preliminary, but served to define the problems involved in obtaining necessary design data from empirical correlations of measurements made in actual machines.

The results obtained depended on the performance of a particular combination probe when used downstream of the rotor. The following conclusions were drawn concerning the probe measurements :

(i) The effect of the presence of flow boundaries on the probe measurements was small, but corrections were derived and applied in the present work. Static pressure derived from the probe measurements, static pressure from wedge probe measurements and wall static pressures were in reasonable agreement.

(ii) The temperature rise across the rotor measured by the probe, using the probe calibration, was consistent with the rise deduced from Euler's turbine equation. All indications were that the probe provided an accurate measurement of the temperature rise.

(iii). The impact pressure measured by the probe in the unsteady flow downstream of the rotor was probably too high. An investigation of the unsteady response of the tubing used



in the probe design is required in order to correct the data obtained so far.

(iv) The flow velocity derived from the probe measurements was probably not as sensitive to unsteady flow effects since all the pressure sensors on the probe were constructed from the same tubing. The derived velocity depends mainly on differences between the pressures registered by the sensors. In steady flow the velocity was determined to better than 1.0% accuracy, to nearly sonic speeds.

(v) The pitch angle was determined by the same probe to within $1\frac{1}{2}^{0}$.

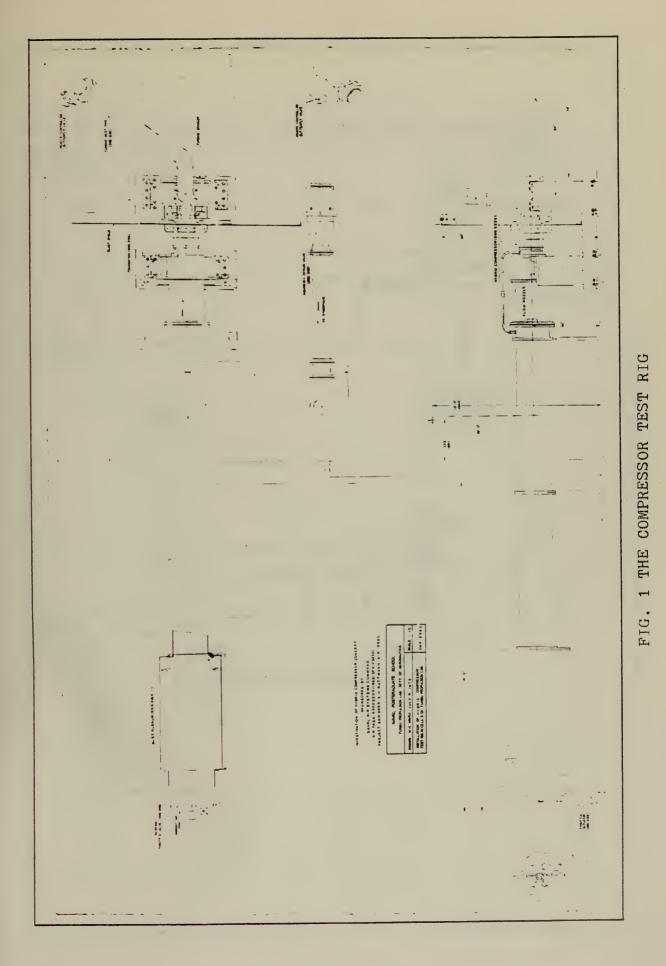
(vi) The wedge probe provided a good measurement of static pressure in the compressor when rotated to a premeasured flow angle.

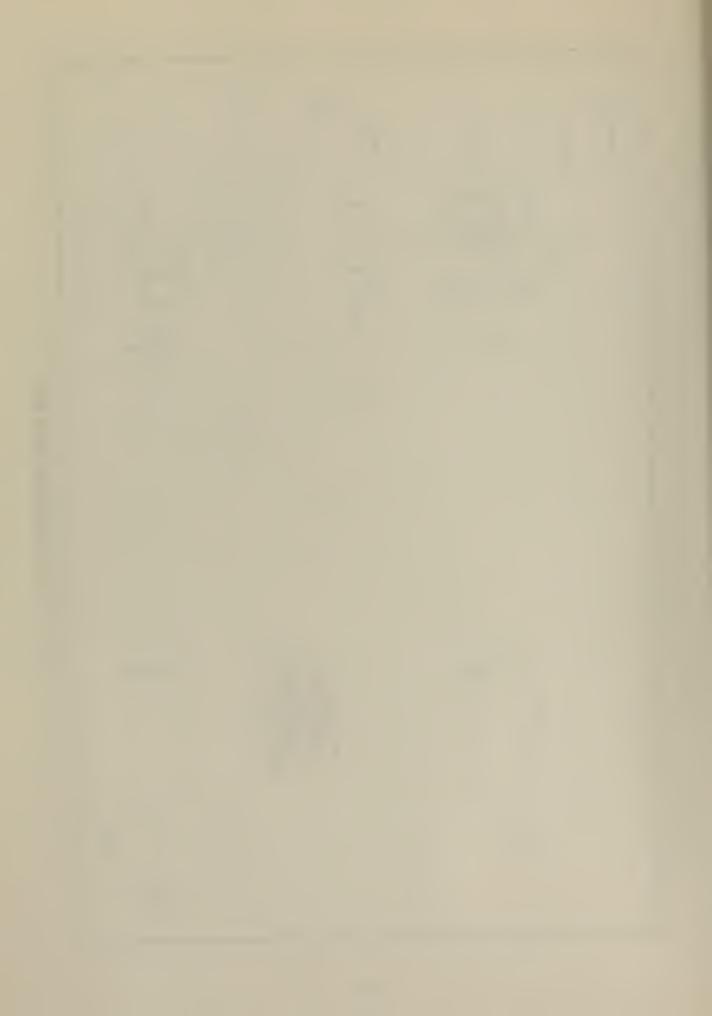
As a result of (iii), the loss coefficients determined from probe measurements were too small, becoming negative over the blading near to the hub. A correction to the impact pressure measurements and more data are needed before a useful correlation of the losses can be obtained. However, it was found that the present results from three tests and four different blade-element surfaces correlated reasonably well in terms of the NASA diffusion factor.

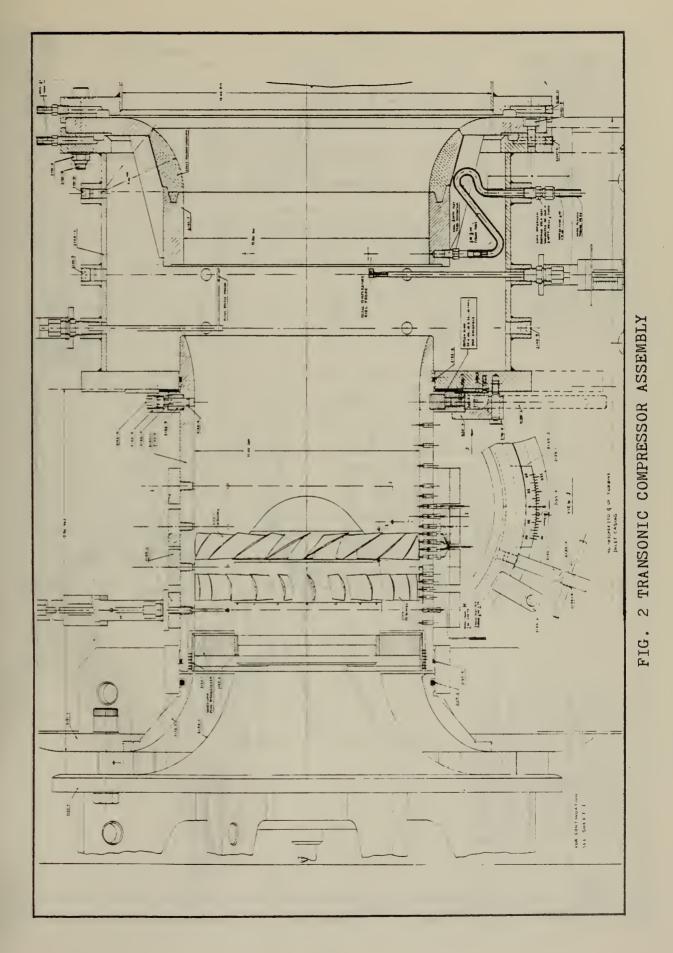
The deviation angles measured in the present tests departed significantly from the values predicted using NASA SP-36. No explanation was found for the negative values measured near to the hub, although the possibility exists that they could be caused by three-dimensional effects in the

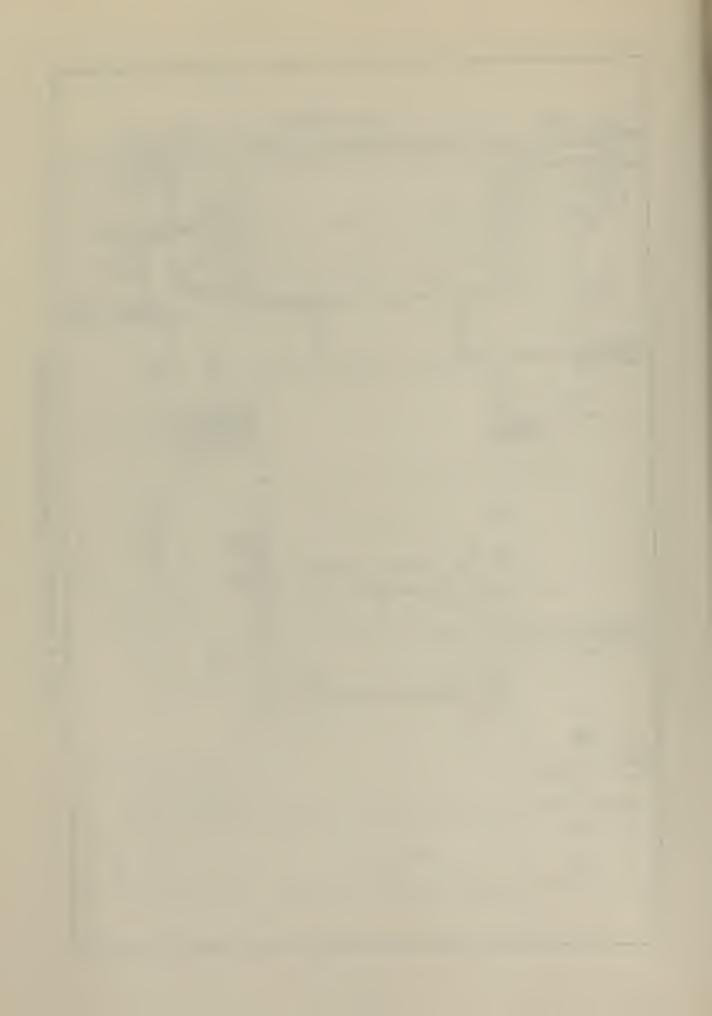
flow through the rotor. More data are needed to confirm the trends in the deviation angles. Agreement with the predicted values was not expected since the blade profiles were unusual, and were operating well away from the design condition.

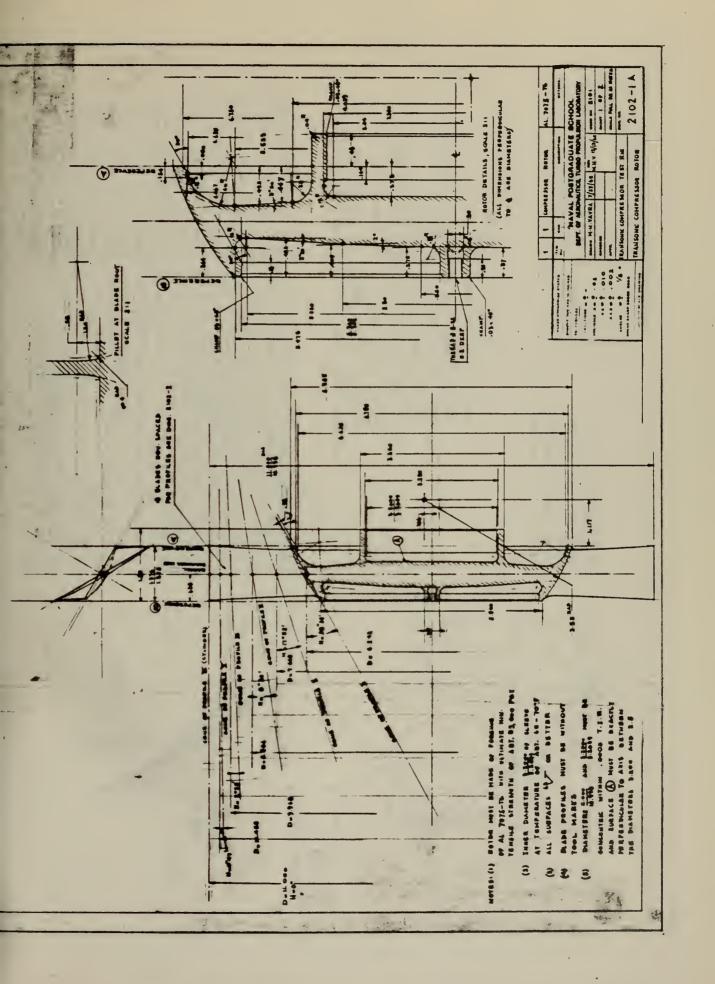




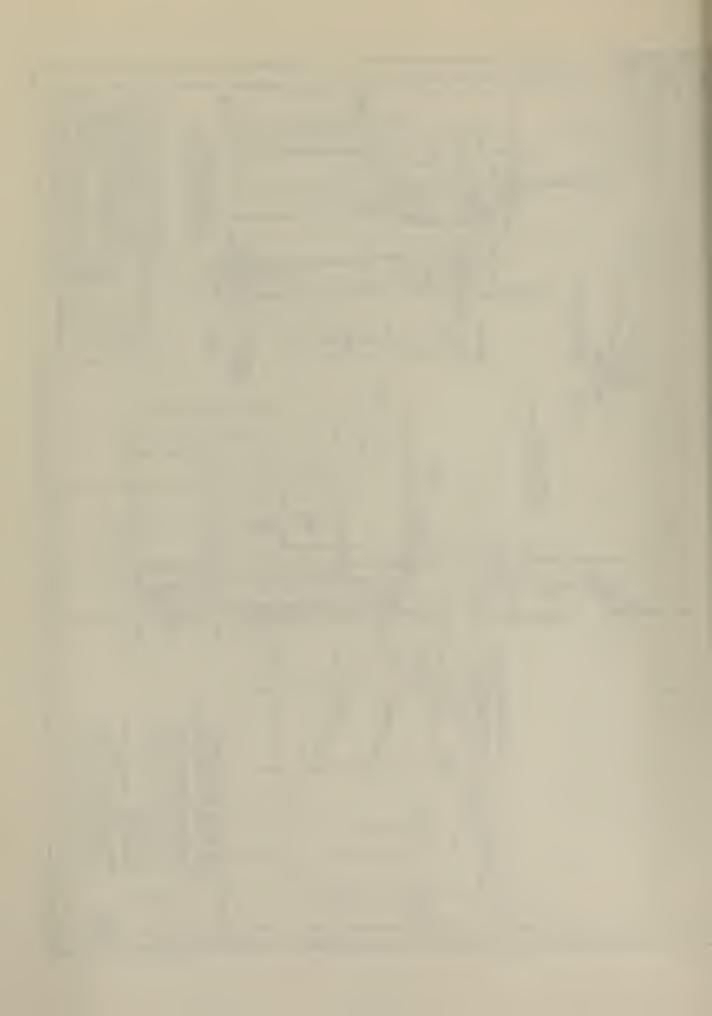


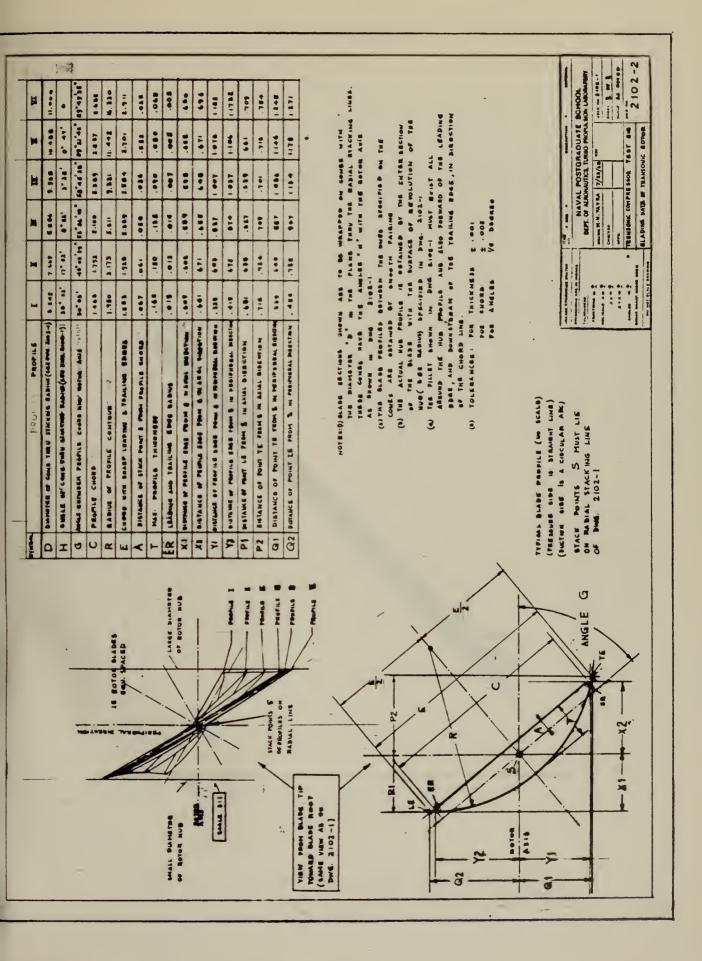


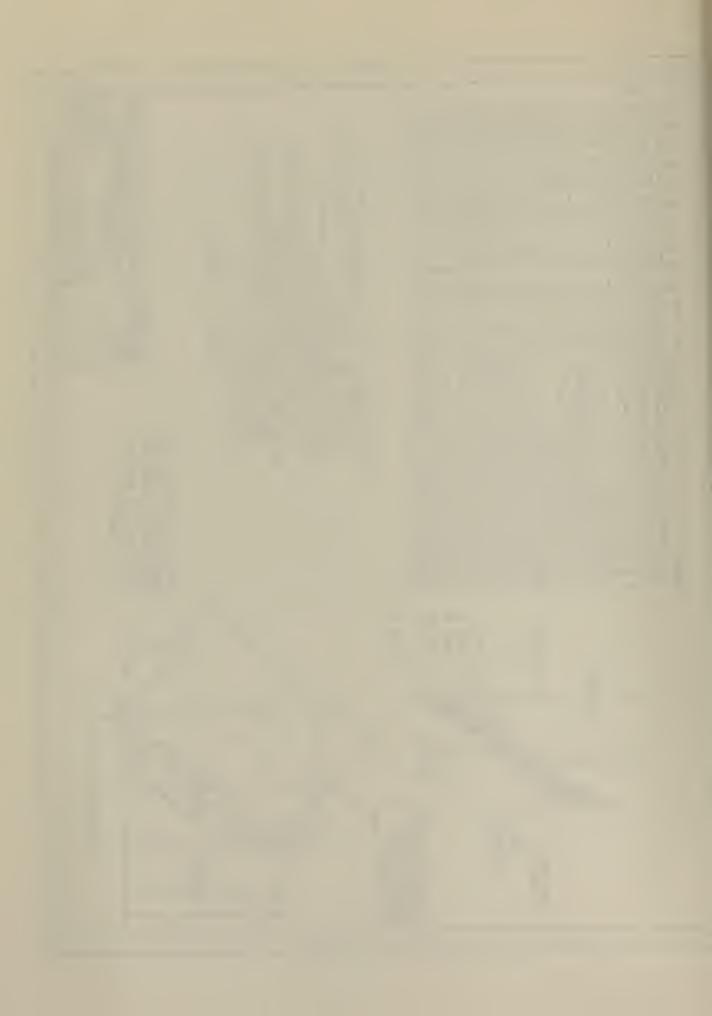




1.







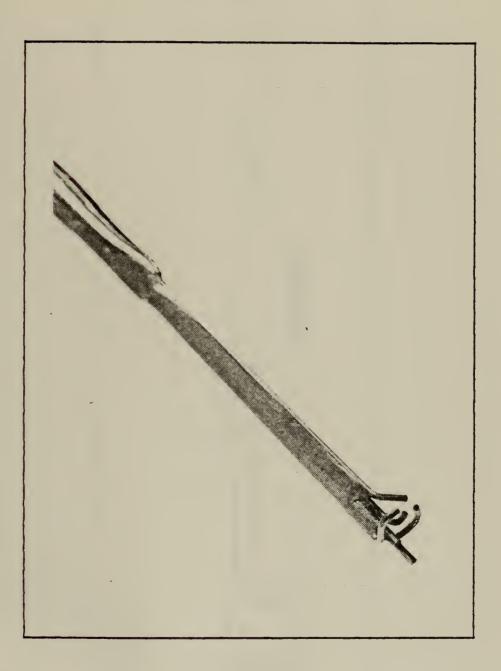


FIG. 4 COMBINATION PROBE (SHOWN WITH THERMO-COUPLE REMOVED)



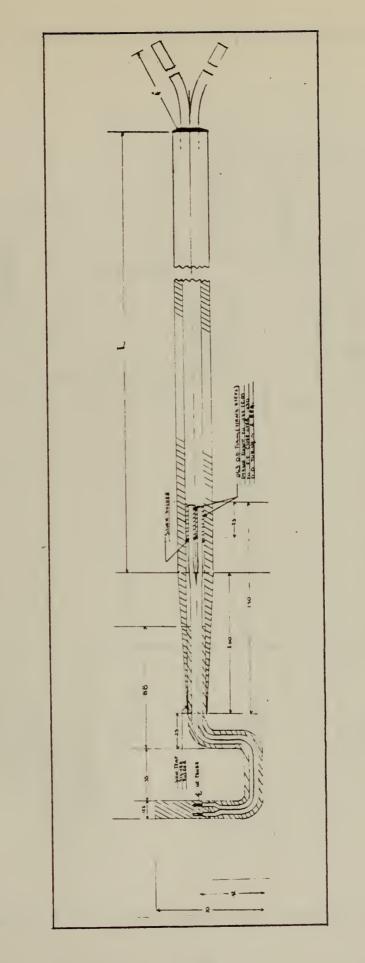
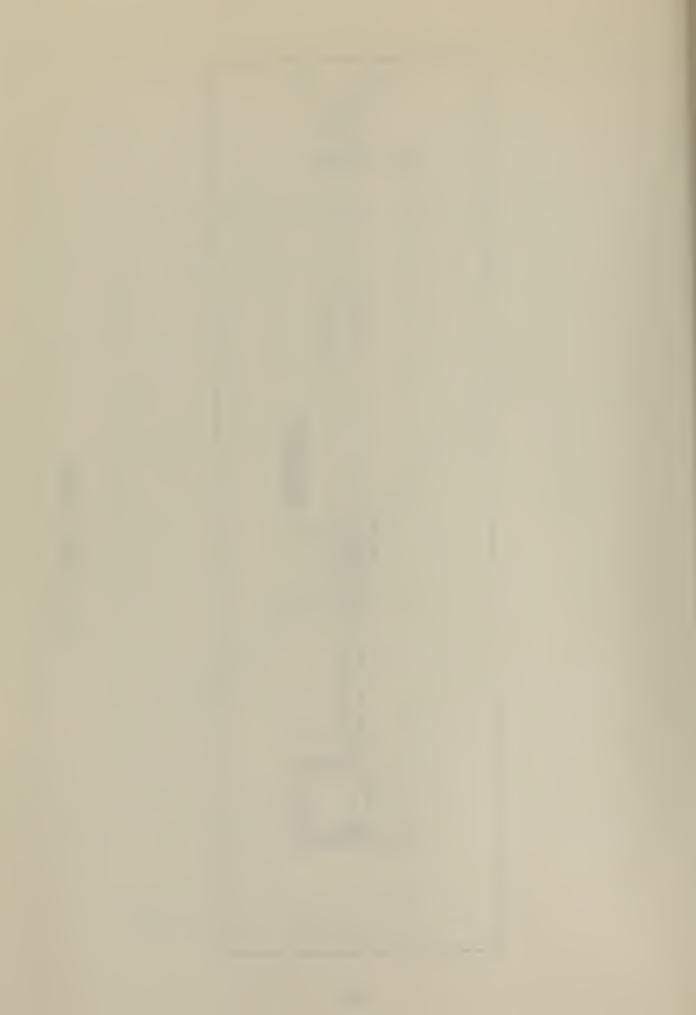
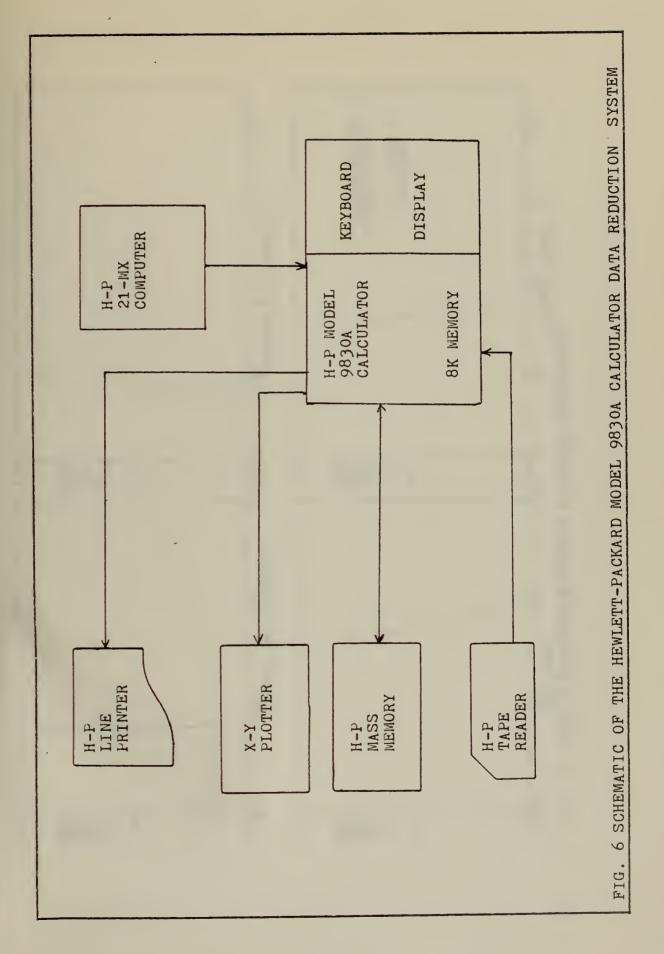
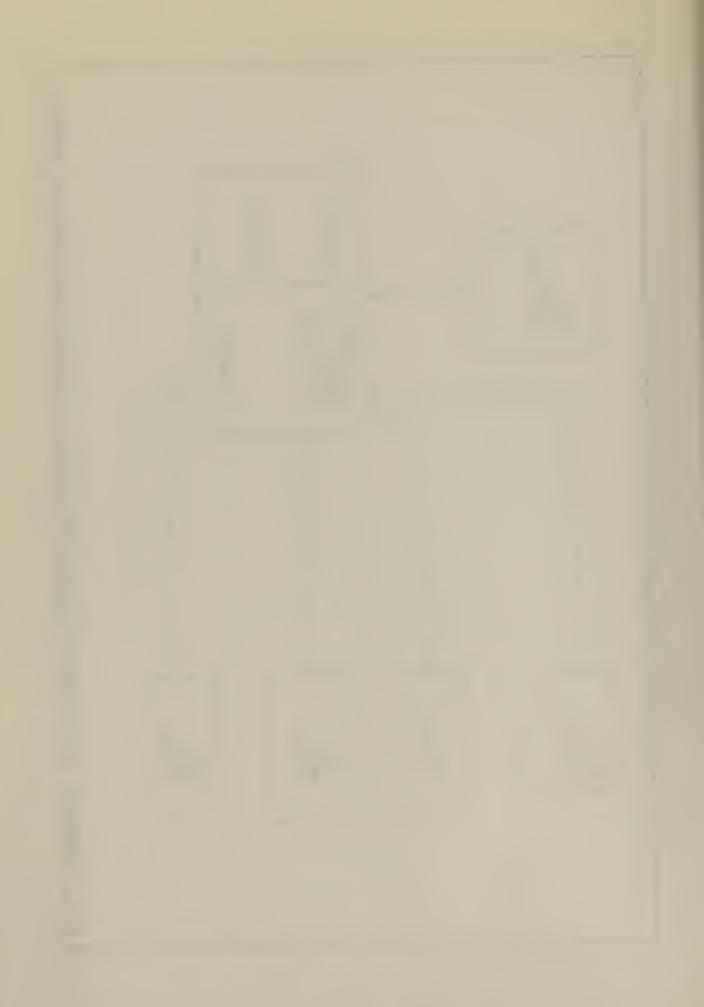
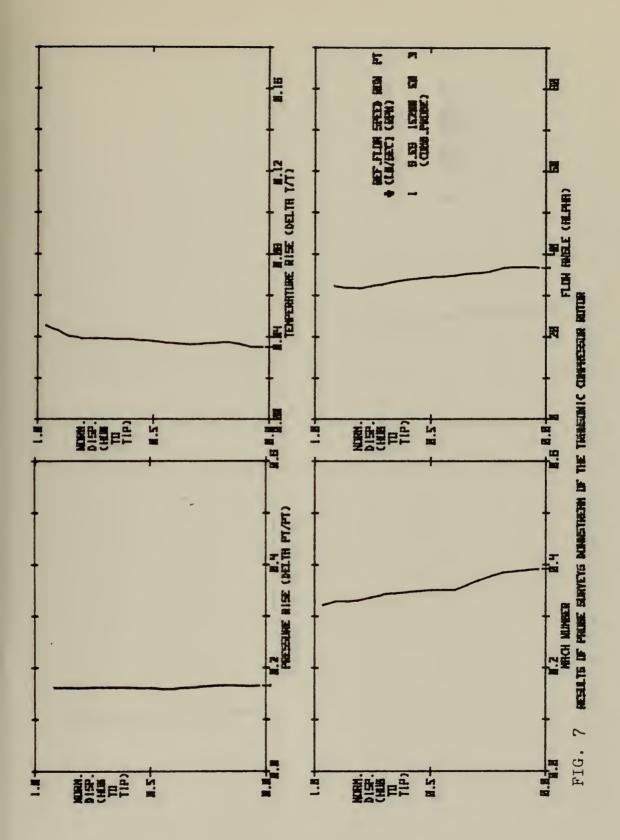


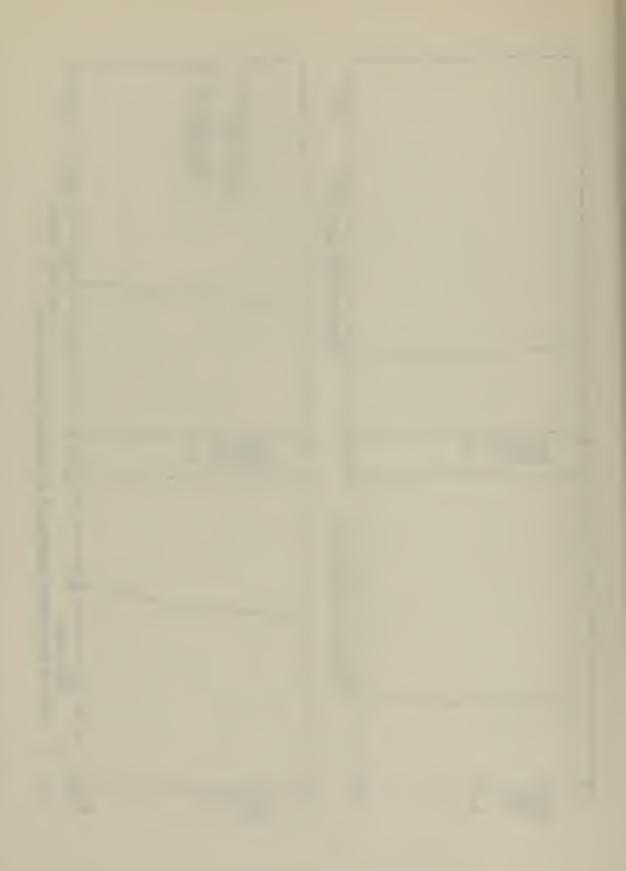
FIG. 5 WEDGE PROBE

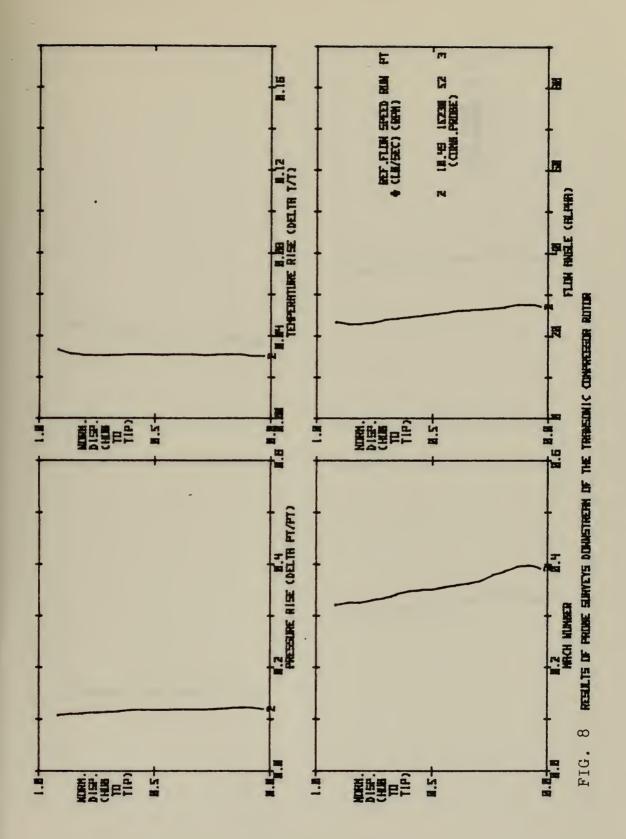


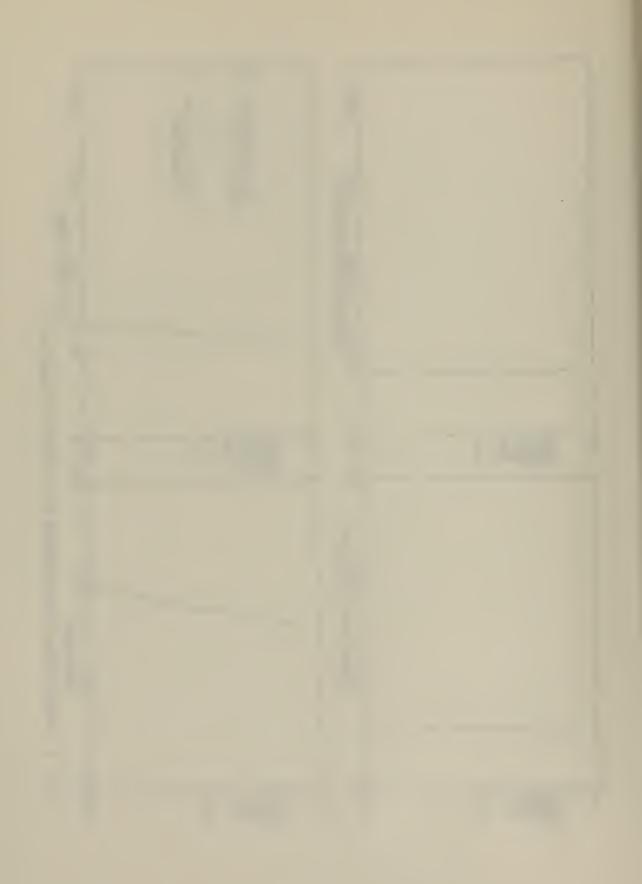


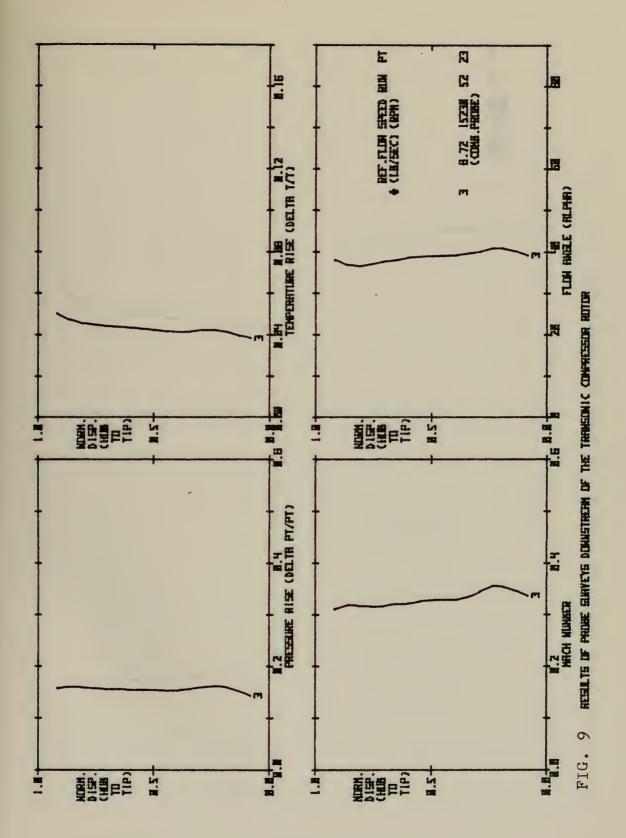


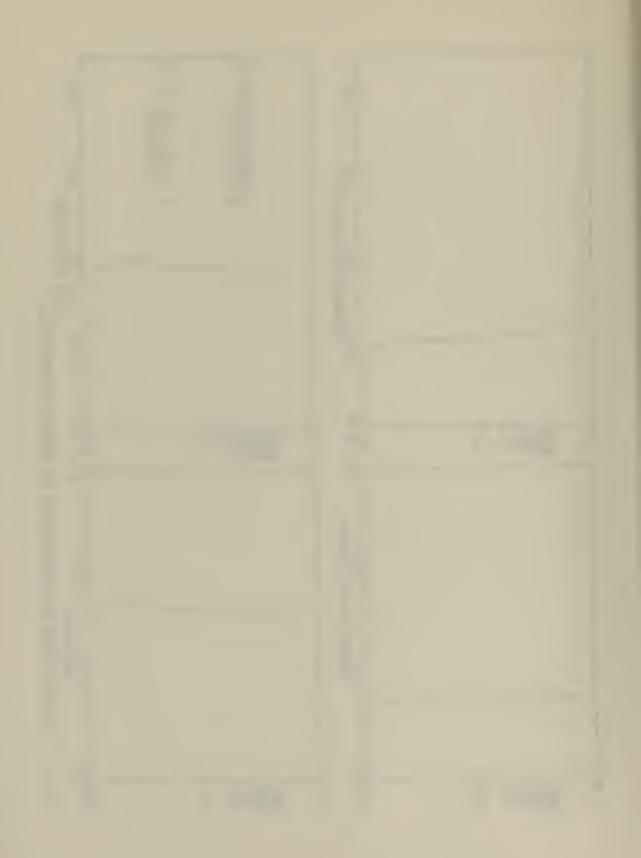


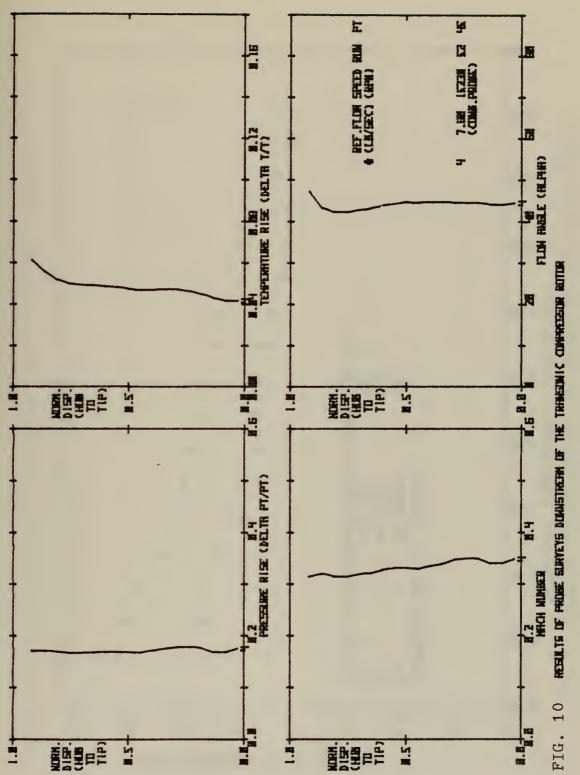


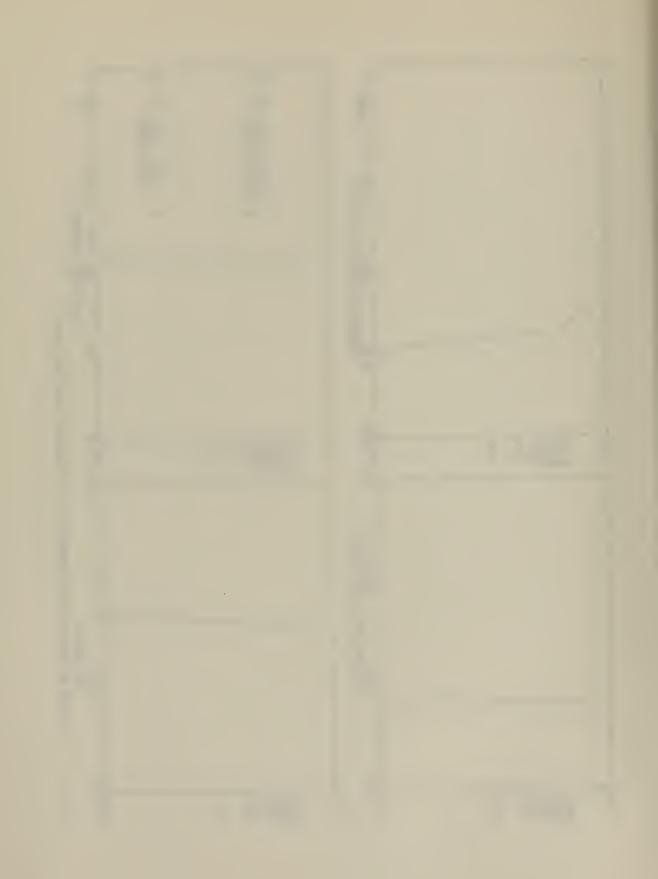


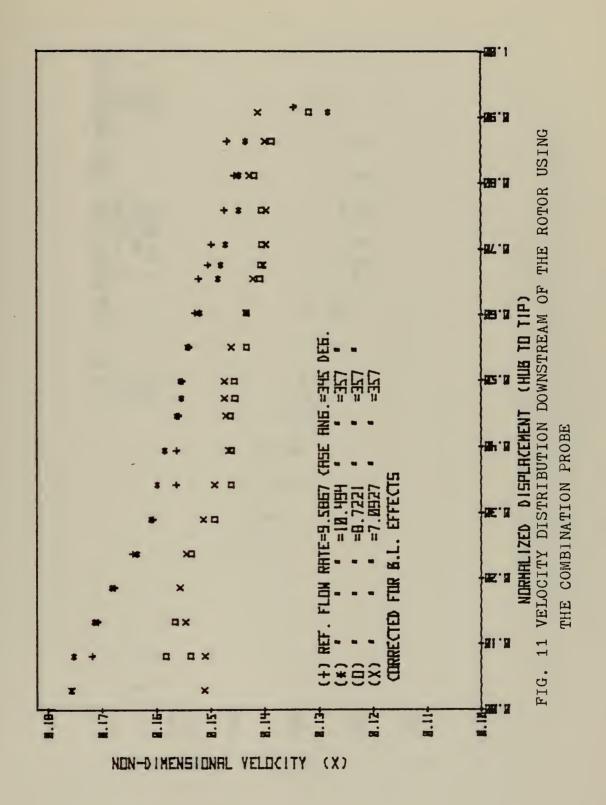




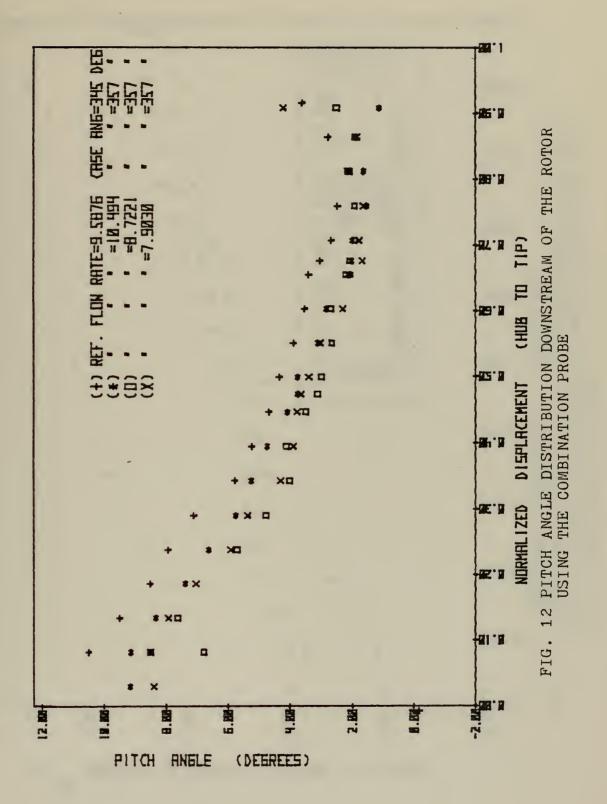


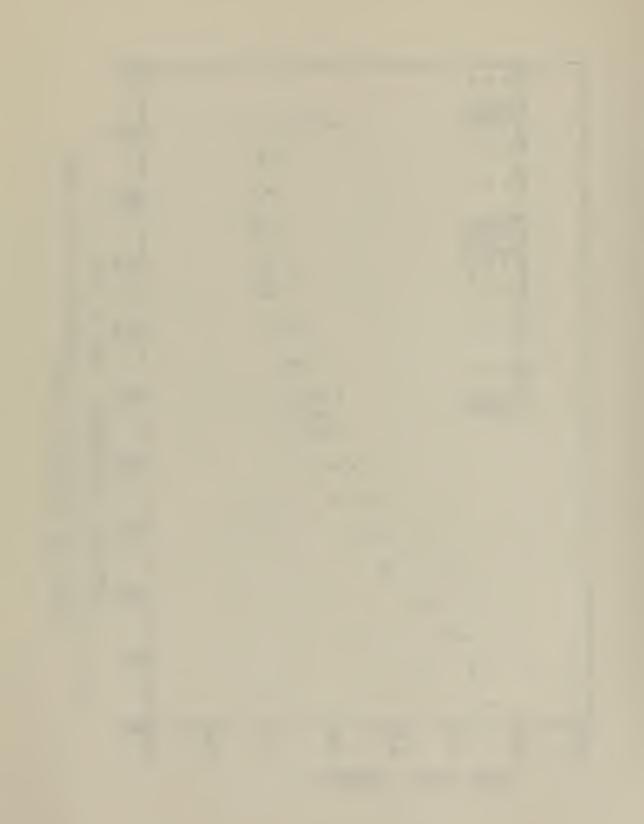


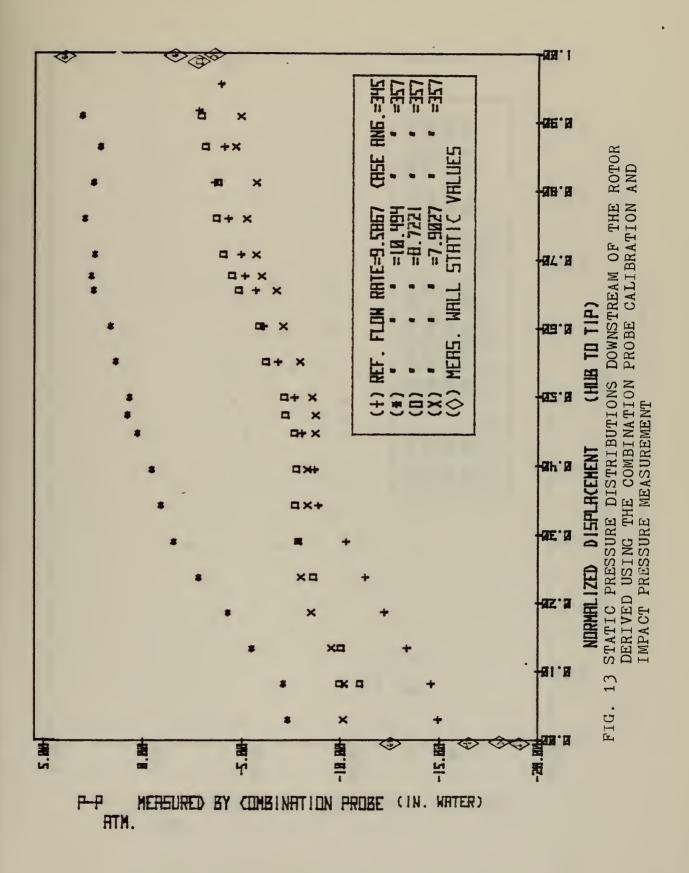


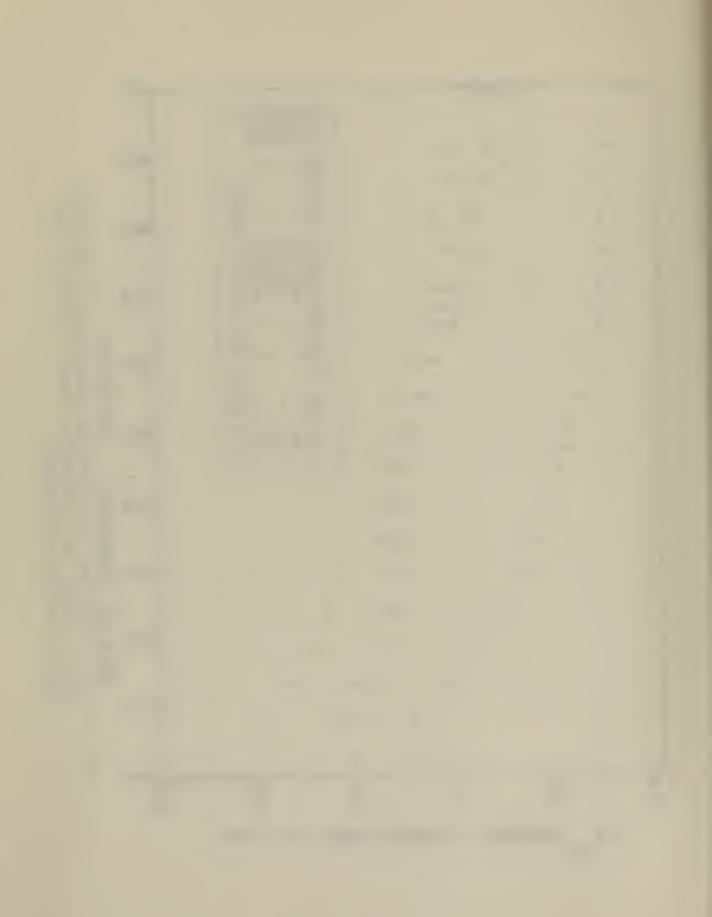


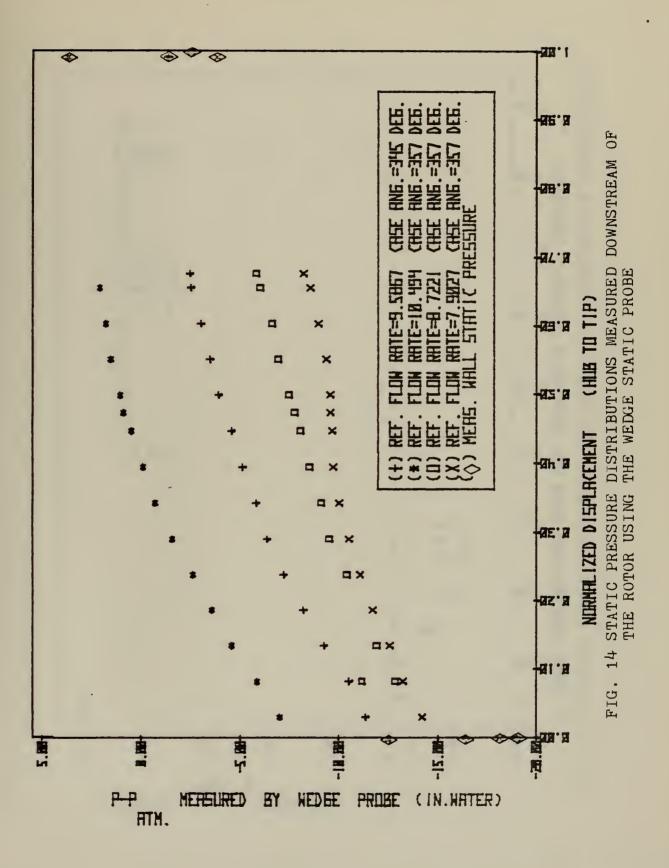


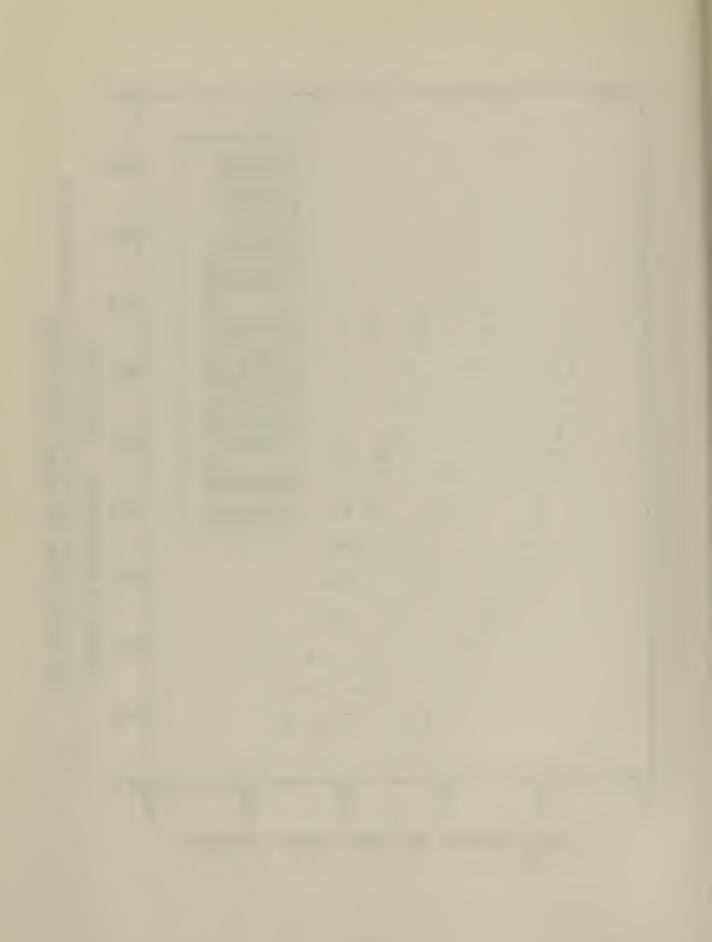


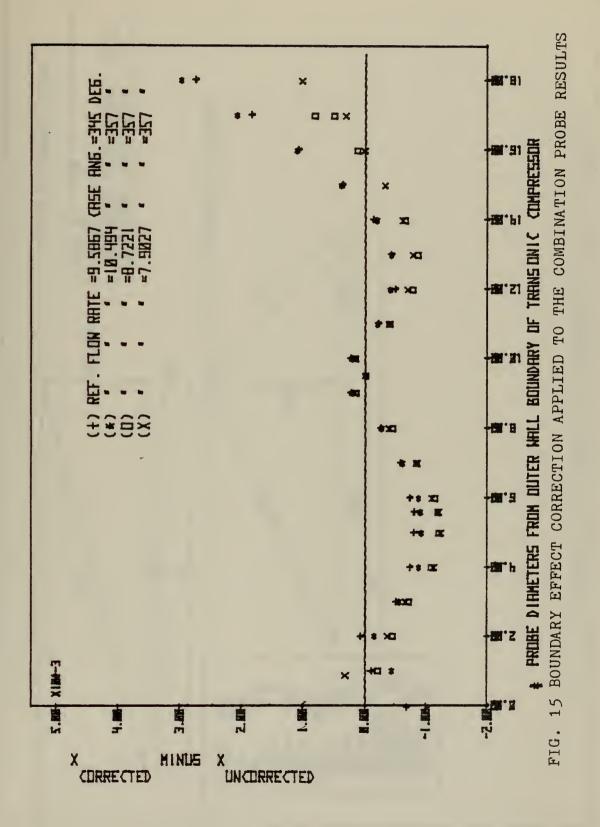


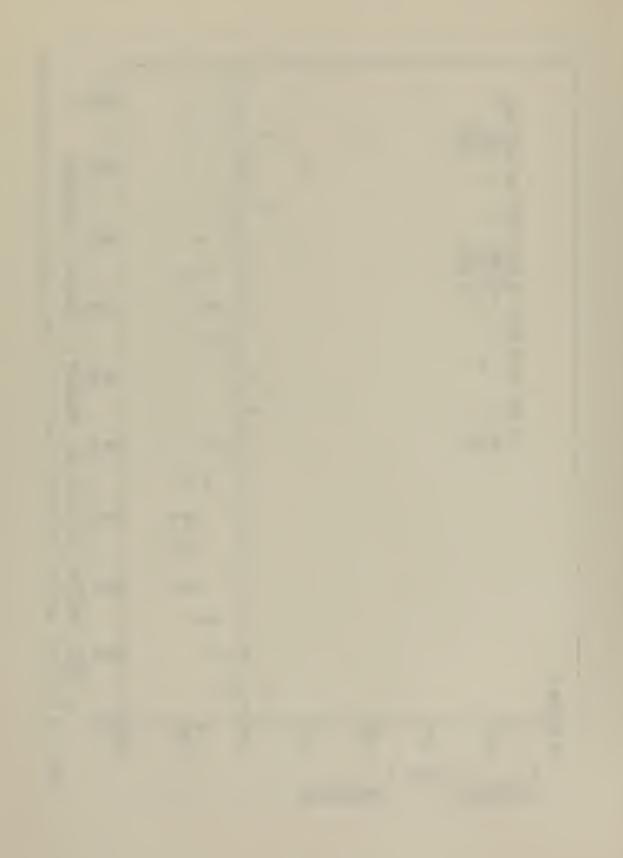


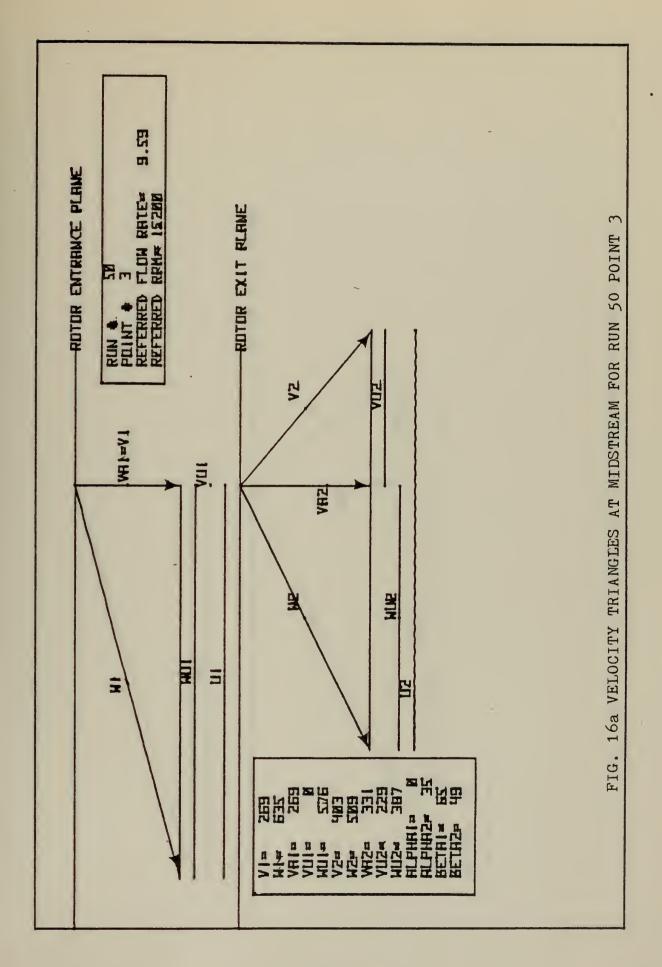


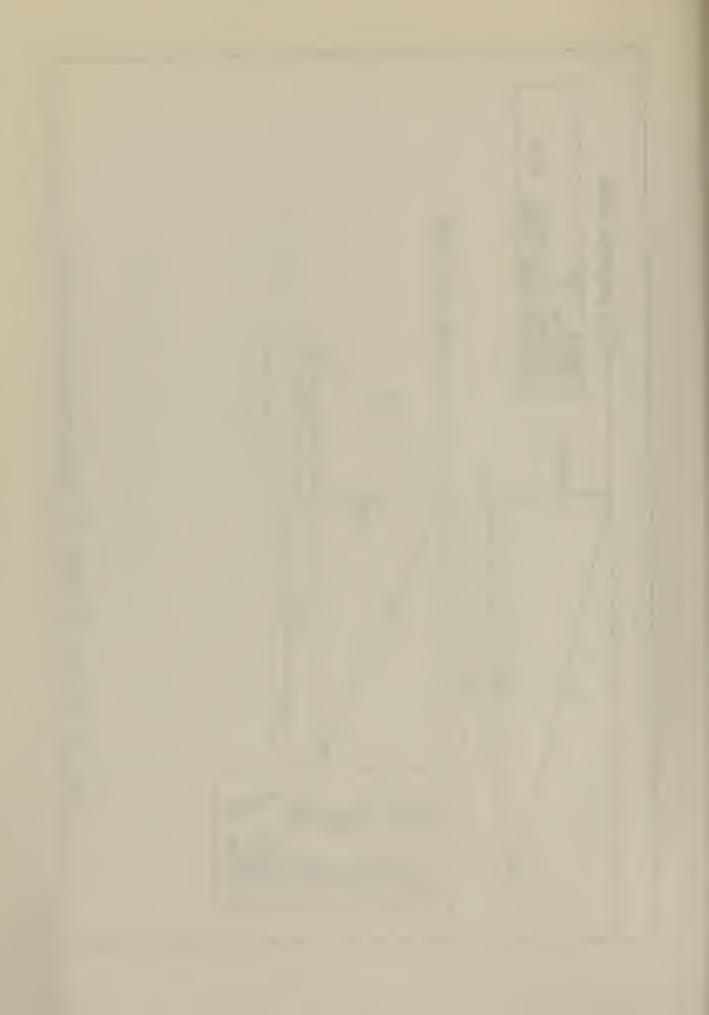


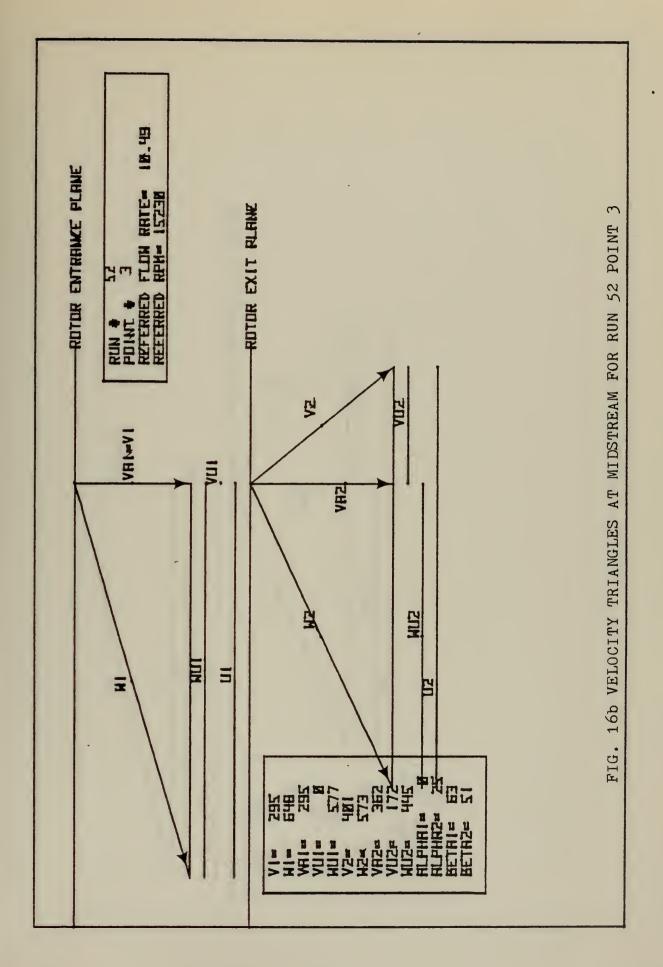


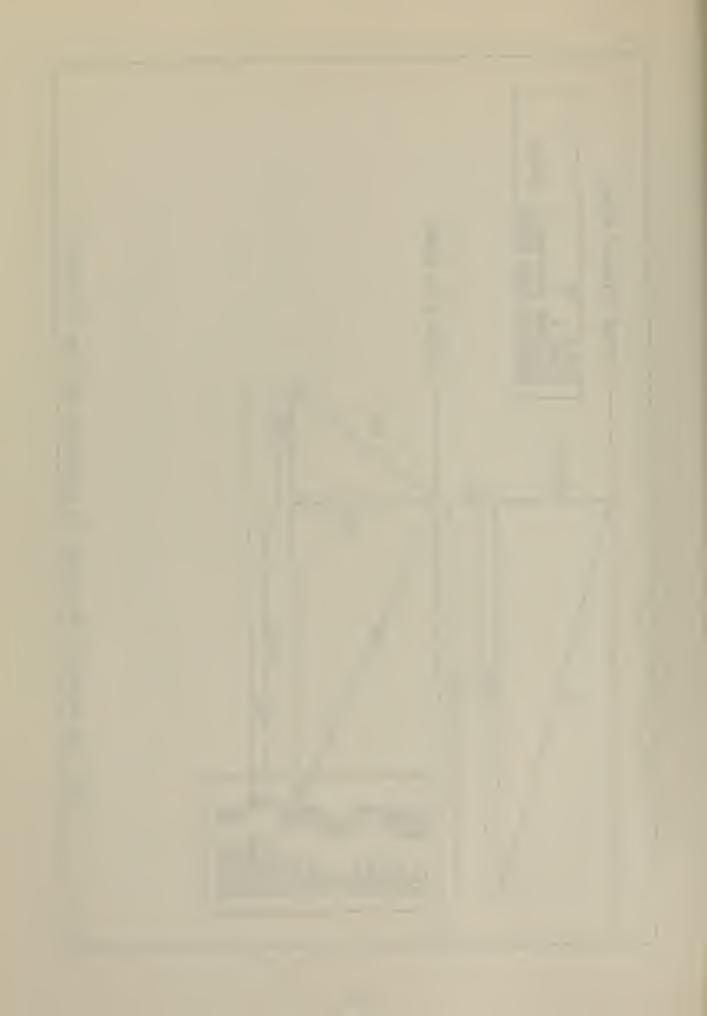


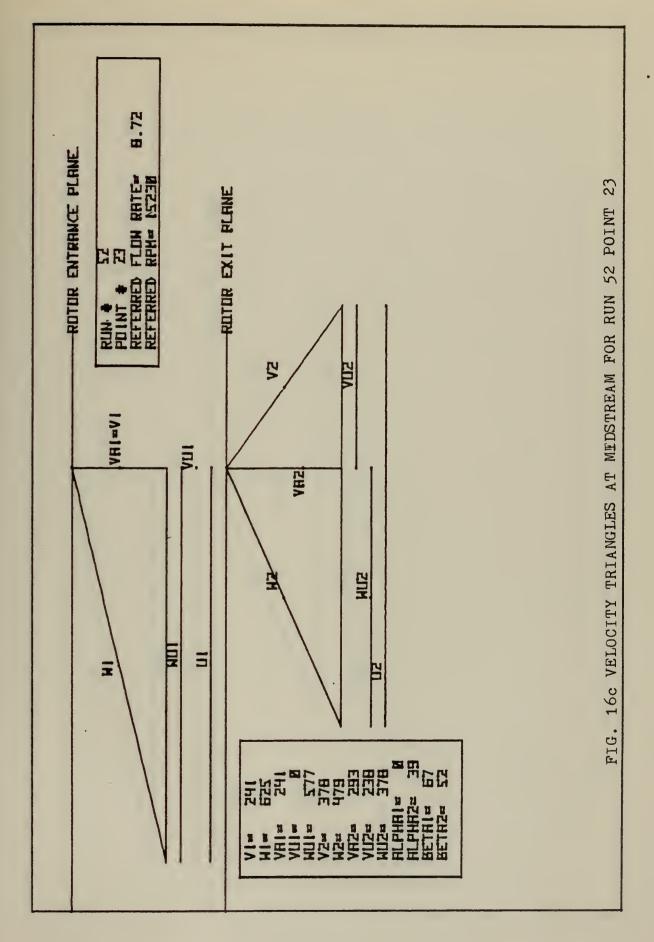


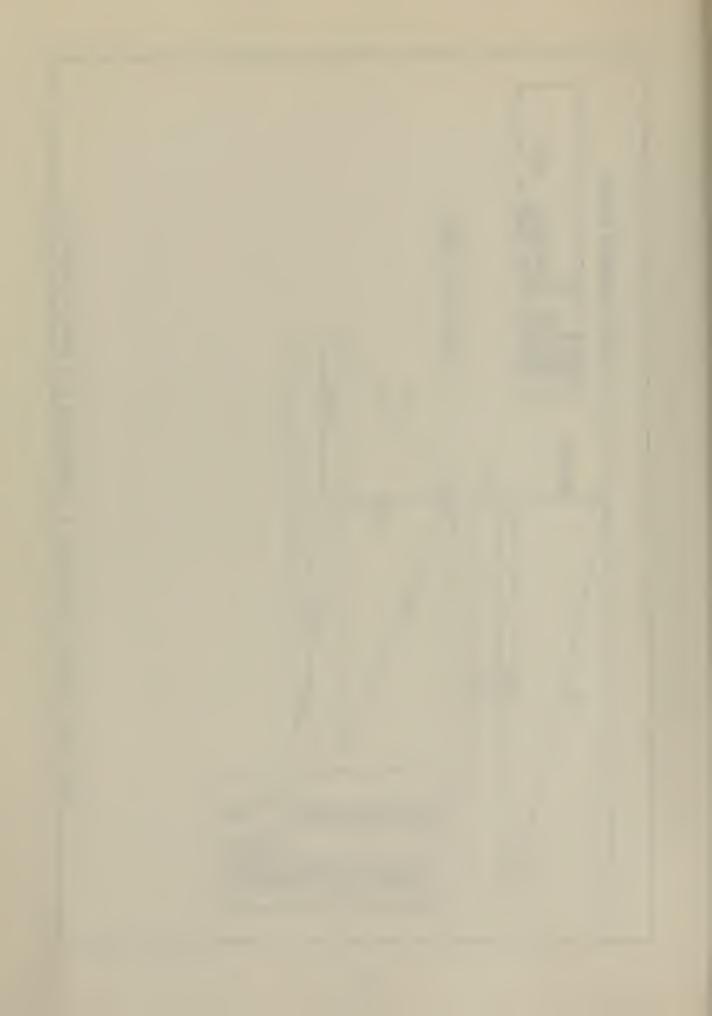


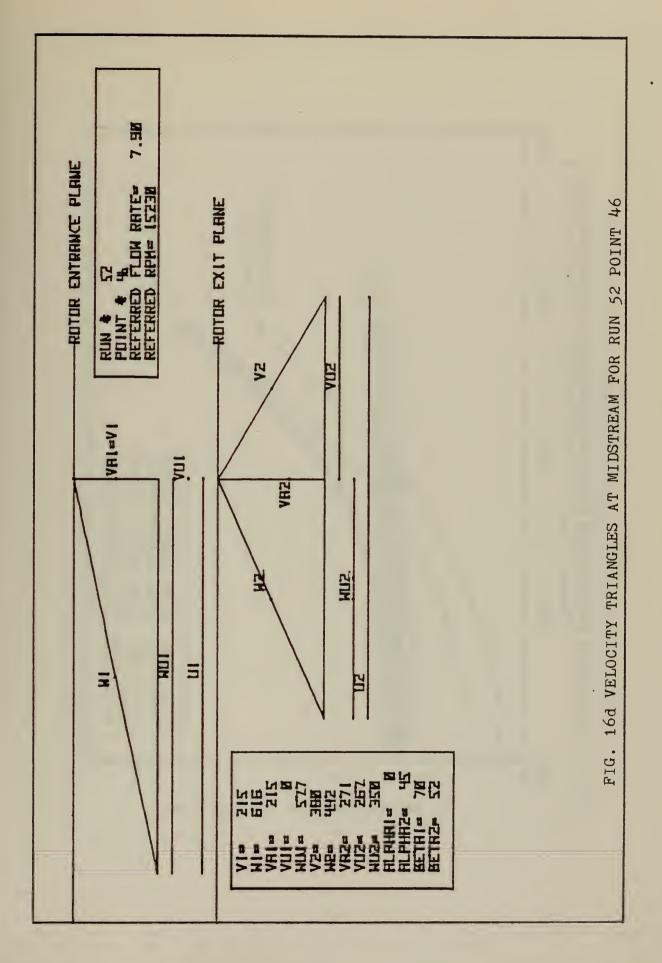


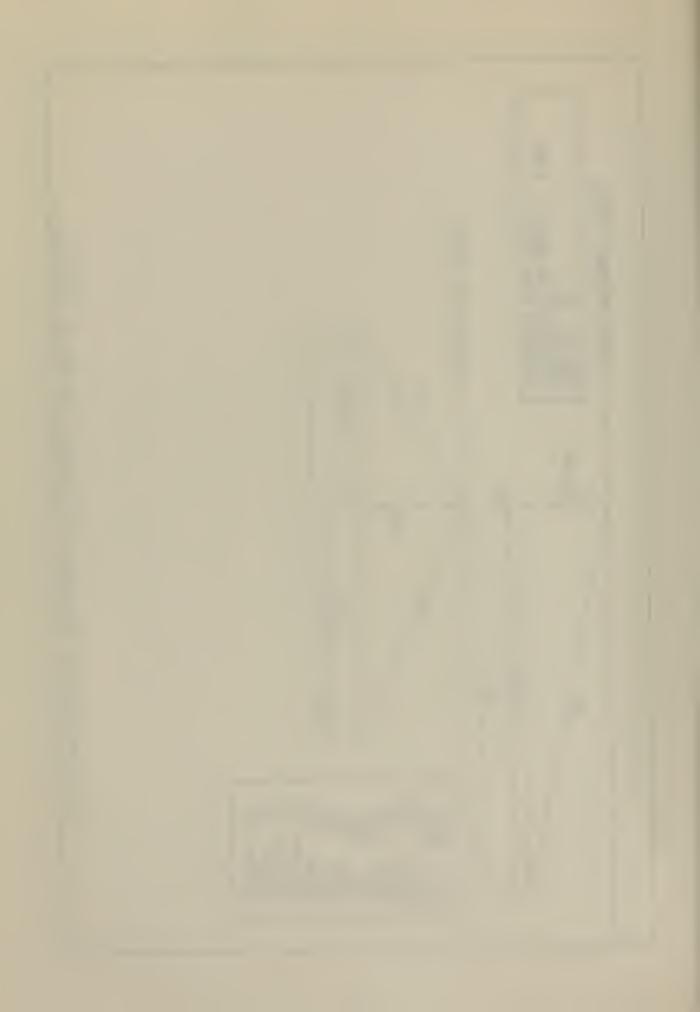


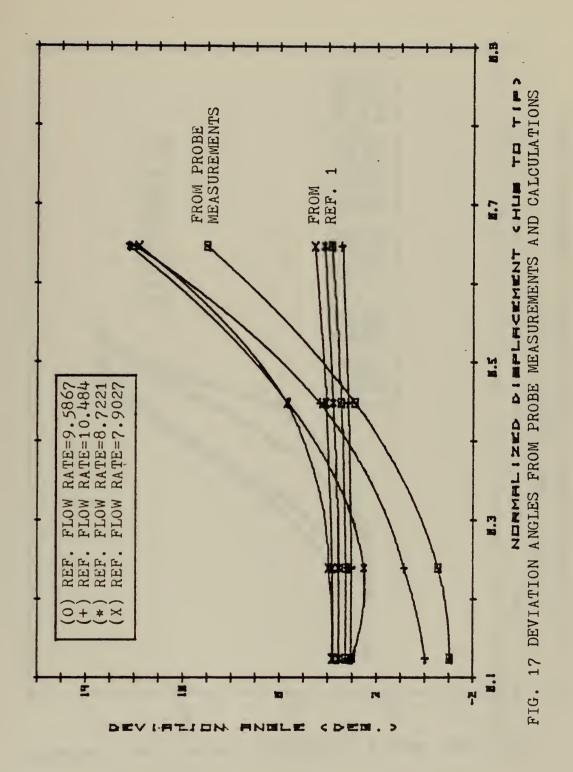




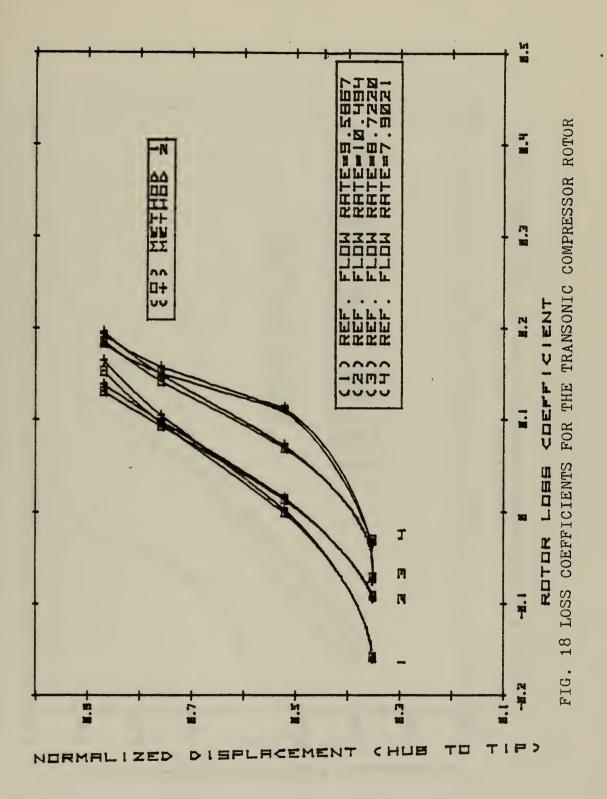




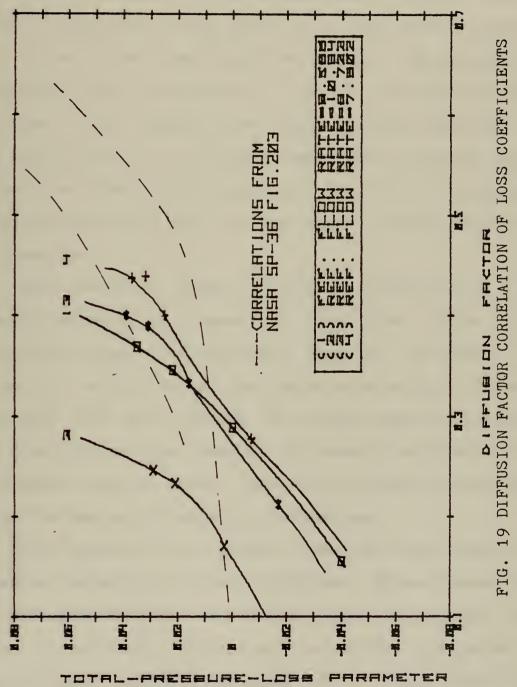














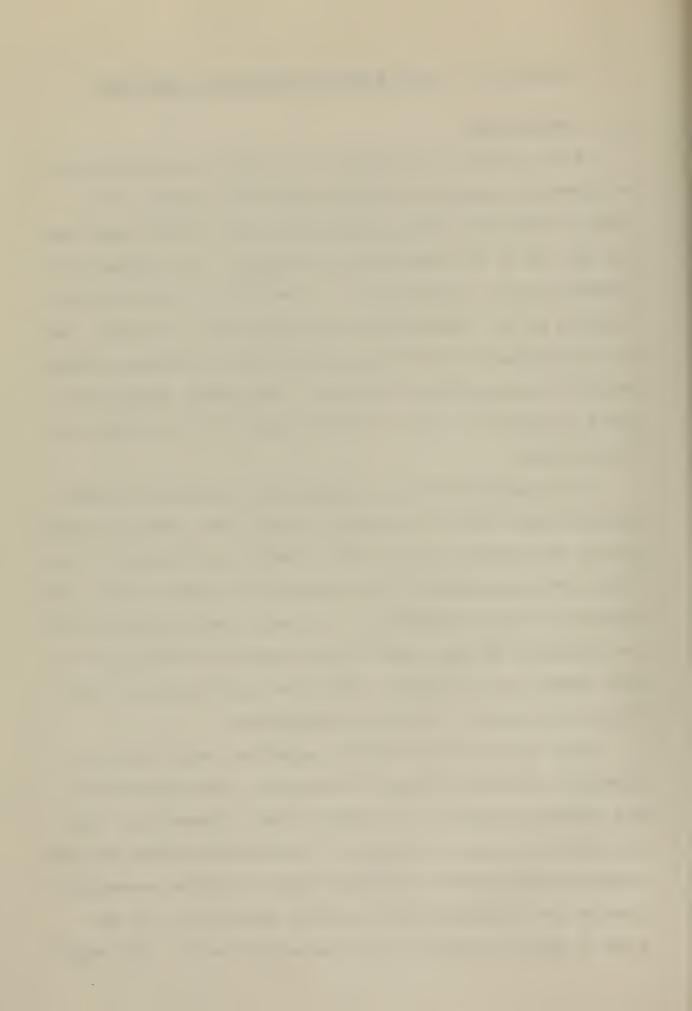
APPENDIX A: BLADE ELEMENT PERFORMANCE PREDICTION

A1. INTRODUCTION

Flow through the blading of an axial-flow compressor is an extremely complicated three-dimensional process. As a result, simplified design models have been devised that permit the use of two-dimensional techniques. The approach is described fully in Reference 1. Involved is first the calculation of the "through-flow" assuming axial symmetry, then the calculation of the "blade-element flow" assuming approximately two-dimensional behaviour. The latter calculation, based on Chapters 6 and 7 of Reference 1, is the subject of this section.

Five quantities shown in Figure A1 determine the aerodynamic behaviour of a cascade in ideal flow. Three of these define the geometry of the blade; they are, the shape of the blade, the orientation of the blades with respect to the cascade axis, and the solidity. The fourth quantity identifies the direction of flow ahead of the cascade and finally, the Mach number must be known. When these quantities are specified, the inviscid flow may be determined.

Real cascade flows however, experience many other influences including friction, turbulence, three-dimensional and unsteady effects, and boundary layer interaction. The procedure outlined in Reference 1 correlates cascade and compressor blade element performance data. Various correction factors are introduced which account empirically for the effects which can not be predicted analytically. The result



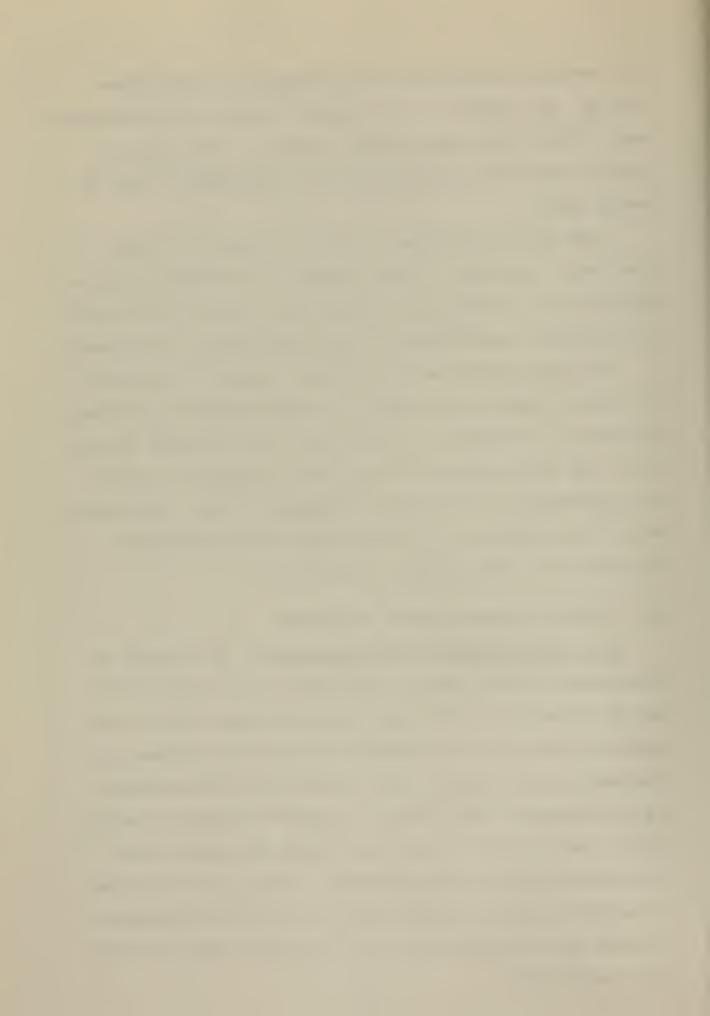
is a method of calculating the performance of compressor blading. The method can be applied to both rotors and stators over a fairly wide range of Mach numbers. The method is limited however to the calculation of performance close to design point.

NASA SP-36 has become a reference text in the axial compressor industry. A brief summary of the method is presented here, followed by a computerized solution which uses the extensive correlations of data presented in this manual.

The main thrust was to develop a program to calculate the blade element performance of a blade design of arbitrary geometry. The program would provide a very powerful design tool, and would provide the basis for a program to predict the performance of a transonic compressor rotor. Reference 6 reports an extension of this was used with considerable success up to a Mach number of about 1.5.

A2. METHOD OF BLADE ELEMENT PREDICTION

A2.1 Two-Dimensional Incidence Angle. Any cascade of aerodynamic blading behaves qualitatively as shown in Figure A2 where \triangle i is the "range" of performance and the midpoint of the curve is defined as the reference minimum loss incidence angle ($i_{ref.}$). For blading with a given camber (ϕ '), thickness. distribution, and maximum thickness ratio (t/c), the solidity (σ) and blade angle (Y) complete the definition of the cascade geometry. Given g_1 and the inlet velocity the method in Reference 1 allows the determination minimum loss incidence angle, the deviation angle, and the loss coefficient.



The reference incidence angle for any blade element can be calculated from correlations of two-dimensional cascade measurements. Two-dimensional reference incidence angle for 10% thick blades is given as

$$i_{2-D} = K_i(i_0)_{10} + n\phi'$$
 A(1)

where K_i is a function of blade thickness distribution and $(i_0)_{10}$ is the zero-camber incidence angle (function of β_1 and σ). n is a slope factor given by

 $n = (i - i_0) / \phi'_{2-D}$ A(2)

which is also a function of β_1 and σ .

In Ref. 1, $(i_0)_{10}$ is given in Fig. 137 and n is given in Fig. 138. K_i has the value 0.7 for double circular-arc aerofoil shapes.

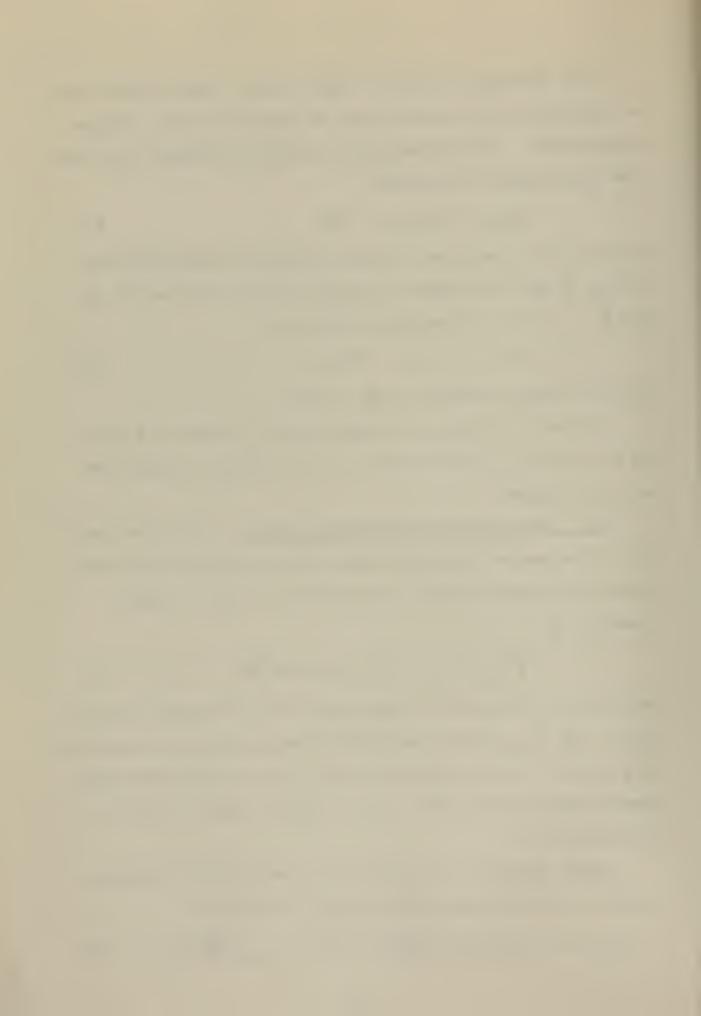
A2.2 Two-Dimensional Deviation Angle. As in the analysis of reference incidence angle, the correlation of bladeelement deviation angle is expressed in terms of blade geometry by

$$S_{2-D}^{\circ} = K_{\xi} (S_{0}^{\circ})_{10} + (m / \sigma^{b}) \not P$$
 A(3)

where K_{s} is a function of blade type (0.7 for double circular arc). $(S_{0}^{\circ})_{10}$ is the zero-camber deviation angle (function of β_{1} and σ), m is a function of β_{1} , for the different basic camber distribution, and b is an exponent that is also a function of β_{1} .

Since deviation angle varies somewhat with incidence angle, a corrected deviation angle is defined as

$$\int_{2-D}^{\circ} = \kappa_{\xi} \left(\int_{0}^{\circ} \right)_{10} + \frac{m}{\sigma^{b}} \not O' + (i_{c} - i_{2-D}) \left(\frac{d\xi^{\circ}}{di} \right)_{2-D} \quad A(4)$$



where $(dS/d_i)_{2-D}$ is the slope of the two-dimensional variation of deviation angle with incidence angle at reference incidence, and i is the actual incidence angle.

Camber and turning angle are related by the equation:

$$\phi' = \beta_1 - \beta_2 + \delta + i$$

or

$$\Delta = \phi + i - S \qquad A(5)$$

Once the two-dimensional deviation and incidence angles have been established, the turning angle can be computed. <u>A2.3 Corrections for Three-Dimensional Effects</u>. The next step in the procedure is to correct reference deviation and reference incidence angles for three-dimensional effects. This is accomplished by defining the three-dimensional reference angles

$$(i_{ref})_{3-D} = i_{2-D} + (i - i_{2-D}) deg$$
 A(6)

and

$$S_{ref}_{3-D} = S_{2-D} + (S - S_{2-D})$$
 A(7)

where $(i - i_{2-D})$ and $(\delta - \delta_{2-D})$ are functions of Mach number.

In summary, the desired turning angle is given by Eq. 288 of Ref. 1.

$$\Delta \varphi = \phi \left[1 - \frac{m}{b} + n\right] - \left[\left(\delta_{c}^{\circ} - \delta_{2-D}\right) - \left(i_{c} - i_{2-D}\right)\right] \\ \left[1.0 - \left(\frac{d\delta^{\circ}}{d_{i}}\right)_{2-D}\right] - K_{i}(i_{0})_{10} + K_{\delta}(\delta_{0}^{\circ})_{10}\right]$$
(8)

A2.4 Loss Coefficient. The loss coefficient for a blade element can be calculated from the correlation given in

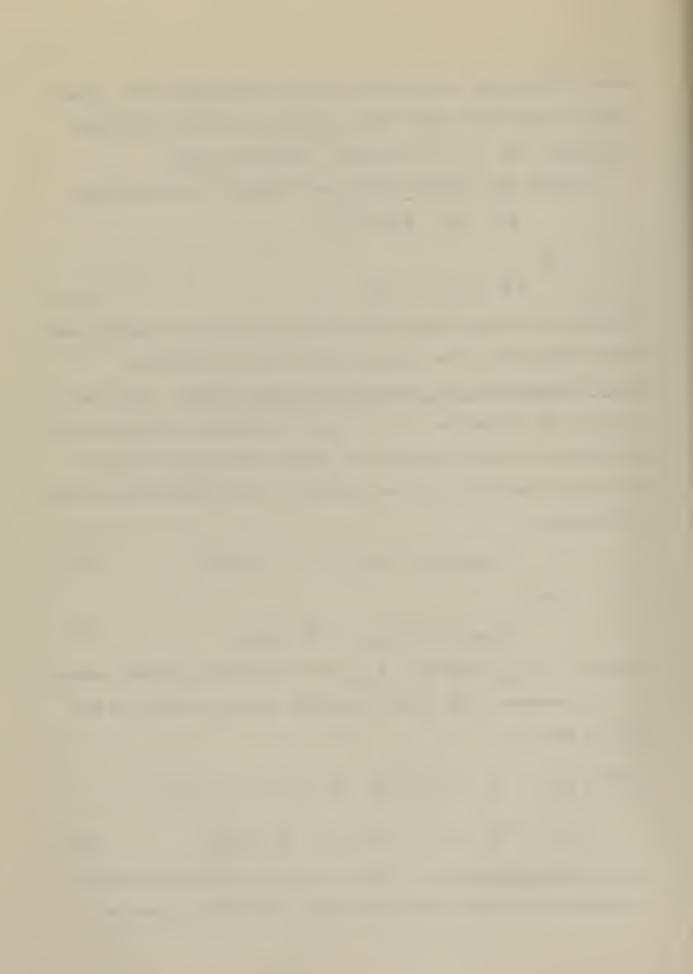


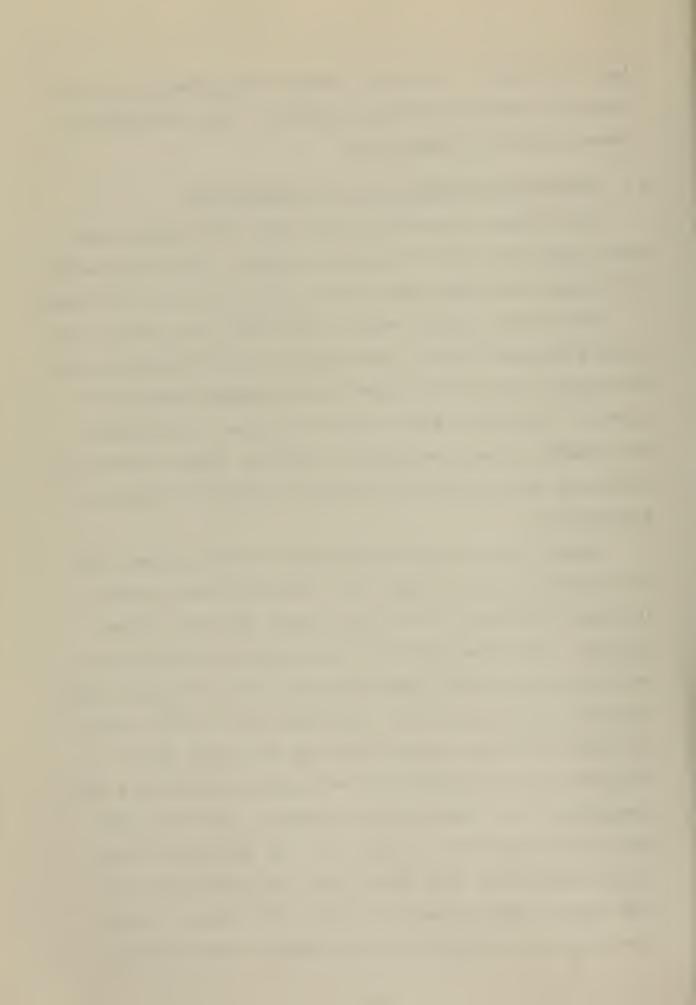
Fig. 203 of Ref. 1. Here the "total loss parameter" is correlated in terms of "Diffusion Factor". The calculation of losses is given in Appendix D.

A3. POLYNOMIAL REPRESENTATION OF CORRELATIONS

All values on the right side of Eq. A(8) may be determined using data given in Figures in Ref. 1 once the geometry of the blade has been given and the inlet velocity calculated.

Each of the unknown values of Eq. A(8) are functions of blading geometry and air inlet angle or blading geometry and Mach number, and are described by well-behaved families of curves. Fig. 168 of Ref. 1 has been chosen to illustrate the process of computerizing the solution, which involved reducing the data correlations given in figures to analytical expressions.

Eleven values of air inlet angle (β_1) were chosen for each solidity given in Fig. 168. The values were plotted as slope factor (m) vs. air inlet angle (β_1) for constant solidity. The data points for each solidity were fit by a third order polynomial curve using the Hewlett-Packard 9830A calculator and X-Y plotter. For simplicity, a fifth order plotting routine was always used with the higher order coefficients equal to zero if a lower order resulted in a more appropriate fit. The plot and polynomial curve fits for each solidity are shown in Fig. A3. The polynomial curve fit for each set of data points gave six soefficients for each curve. Thus for each m vs. β_1 plot, the six coefficients A_0, A_1, \ldots, A_5 were calculated for the polynomial



expression for m as a function of \S_1 :

$$m = A_0 + A_1\beta_1 + A_2\beta_1^2 + A_3\beta_1^3 + A_4\beta_1^4 + A_5\beta_1^5 \qquad A(11)$$

at each value of solidity with β_1 converted to radians to minimize the error in higher order terms. The coefficients A_0, A_1, \ldots, A_5 derived from the curve fits of Fig. A3 were plotted against each of twelve values of solidity as follows:

$$A_{0} (I) vs. \sigma (I) \dots 12 points$$

$$A_{1} (I) vs. \sigma (I) \dots 12 points$$

$$A_{5} (I) vs. \sigma (I) \dots 12 points$$

$$A(12)$$

$$A_{5} (I) vs. \sigma (I) \dots 12 points$$

$$A_{0} = a_{0} + a_{1}\sigma + a_{2}\sigma^{2} + a_{3}\sigma^{3} + a_{4}\sigma^{4} + a_{5}\sigma^{5}$$

$$A_{1} = a_{0}^{1} + a_{1}\sigma^{1} + a_{2}^{1}\sigma^{2} + a_{3}^{1}\sigma^{3} + a_{4}^{1}\sigma^{4} + a_{5}^{1}\sigma^{5}$$

$$A_{1} = a_{0}^{1} + a_{1}\sigma^{1} + a_{2}^{1}\sigma^{2} + a_{3}^{1}\sigma^{3} + a_{4}^{1}\sigma^{4} + a_{5}^{1}\sigma^{5}$$

$$A_{1} = a_{0}^{1} + a_{1}\sigma^{1} + a_{2}^{1}\sigma^{2} + a_{3}^{1}\sigma^{3} + a_{4}^{1}\sigma^{4} + a_{5}^{1}\sigma^{5}$$

$$A_{1} = a_{0}^{1} + a_{1}\sigma^{1} + a_{2}^{1}\sigma^{2} + a_{3}^{1}\sigma^{3} + a_{4}^{1}\sigma^{4} + a_{5}^{1}\sigma^{5}$$

$$A_{1} = a_{0}^{1} + a_{1}\sigma^{1} + a_{2}^{1}\sigma^{2} + a_{3}^{1}\sigma^{3} + a_{4}^{1}\sigma^{4} + a_{5}^{1}\sigma^{5}$$

$$A_{1} = a_{0}^{1} + a_{1}\sigma^{1} + a_{2}^{1}\sigma^{2} + a_{3}^{1}\sigma^{3} + a_{4}^{1}\sigma^{4} + a_{5}^{1}\sigma^{5}$$

which resulted in polynomial curve fits shown in Fig. A4. In this case the higher order coefficients A_4 and A_5 are set equal to zero. When all the coefficients in Eq. A(13) are known, the slope factor m, for any given σ and β_1 can be calculated from:

$$m = (a_{0} + a_{1}\sigma + a_{2}\sigma^{2} + a_{3}\sigma^{3} + a_{4}\sigma^{4} + a_{5}\sigma^{5})$$

$$+ (a_{0}^{1} + a_{1}^{1}\sigma + a_{2}^{1}\sigma^{2} + a_{3}^{1}\sigma^{3} + a_{4}^{1}\sigma^{4} + a_{5}^{1}\sigma^{5})\beta_{1...+}$$

$$::+(a_{0}^{5} + a_{1}^{5}\sigma + a_{2}^{5}\sigma^{2} + a_{3}^{5}\sigma^{3} + a_{4}^{5}\sigma^{4} + a_{5}^{5}\sigma^{5})\beta_{1}^{5}$$

This procedure resulted in a single equation (Eq. A(14))for m in which the coefficients were analytic functions of β_1 .

.

The coefficients are given in Tables A1 and A2. Due to the well-behaved nature of the curves, the slope factor m could be calculated to well within the accuracy of the original data contained in Ref. 1.

All data necessary to predict performance for circulararc blading was reduced to polynomials using a similar procedure. The polynomials were included in a computer program to calculate blade element performance for specified input geometry and flow conditions.

A4. COMPUTER PROGRAM

<u>A4.1 Description</u>. Program "NASA36" was written for the Hewlett-Packard 9830A calculator to calculate the incidence and deviation angles for a rotor with meridional inlet velocity. The program follows the method of Ref. 1 through the equations given in Section A2. Where a value from a Figure in Ref. 1 is required, it is calculated using a polynomial approximation to the data as described in Section A3.

The program is self-explanatory through the listing given in Table A3. The symbols are defined in Table A4. The program performs the blade element calculations for a specified compressor operating condition. The inputs are referred flow rate and speed, and temperatures upstream and downstream of the rotor. Through the method given in Appendix C, these inputs define the inlet velocity as a function of the radial position. It should be noted therefore that the present version of the program includes a description

of the transonic compressor inlet flow-field, while it allows changes in blading geometry to be input.

<u>A4.2 Operation</u>. Detailed information on the operating procedures for the HP-9830 calculator, mass memory and associated equipment are found in Ref. 9 and Ref. 10. The following is a step-by-step operating procedure for the program called "NASA36".

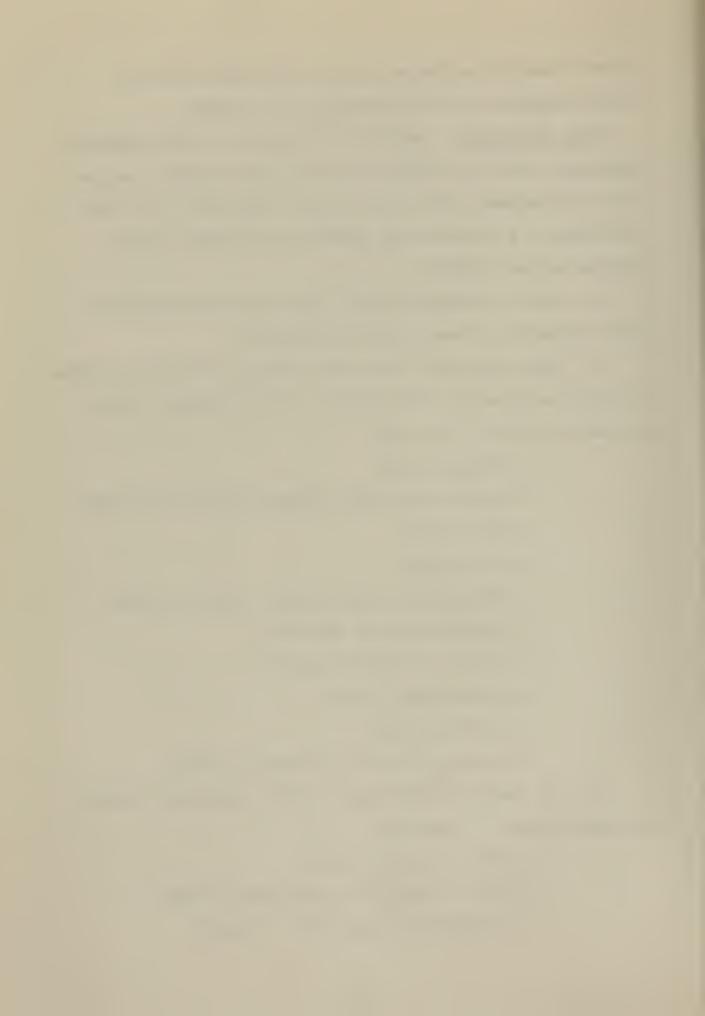
1. After loading "NASA36" into the Hewlett-Packard 9830A calculator press "Run" and "Execute".

2. The calculator will then display a series of inputs required to determine the geometry of the blading. These are shown in Fig. 3 and are:

- a) Stagger angle
- b) Chord with sharp leading and trailing edges
- c) Tip radius
- d)-Hub radius
- e) Diameter of cone through stacking radius
- f) Maximum Profile Thickness
- g) Radius of Profile Contour
- h) Blade camber angle
- i) Profile chord
- j) Angle of cone thru stacking radius

3. The operating parameters of the compressor rotor are now required. These are:

- a) Revolutions per minute
- b) Total temperature upstream of rotor
- c) Temperature downstream of rotor



d) Referred flow rate

Outputs include deviation and incidence angles, Mach number before and after the rotor, and referred flow function (Φ) .



Table A1

Coefficients for Eq. A(11)

A 5	0	0	0	0	0	0	0	0	0	0	0	0
A4	0	0	0	0	0	0	0	0	0	0	0	0
A ₃	0686459	05157576	0072702	00063945	.0243992	.03103606	.043310059	.05919224	.0626165	.056440537	.0715060	.0655224
A2	.05745331	.07365157	.024863524	.02439882	00434522	0005187	0253336	040108605	03145125	013581617	0389736	0346697
A'1	00172689	002457967	.01587984	.025196542	.03080154	.02295859	.03885258	.04138388	.02853839	.013581617	.02473965	.02868824
AO	.60422074	.48957429	.40879632	.349811725	.30978144	.280292	.24934145	.2093762	.181571948	.160653459	.14262652	.12848536
Value of Solidity	t1.	• 5	• 6	2.	8.	6.	1.0	1.2	1.4	1.6	1.8	2.0

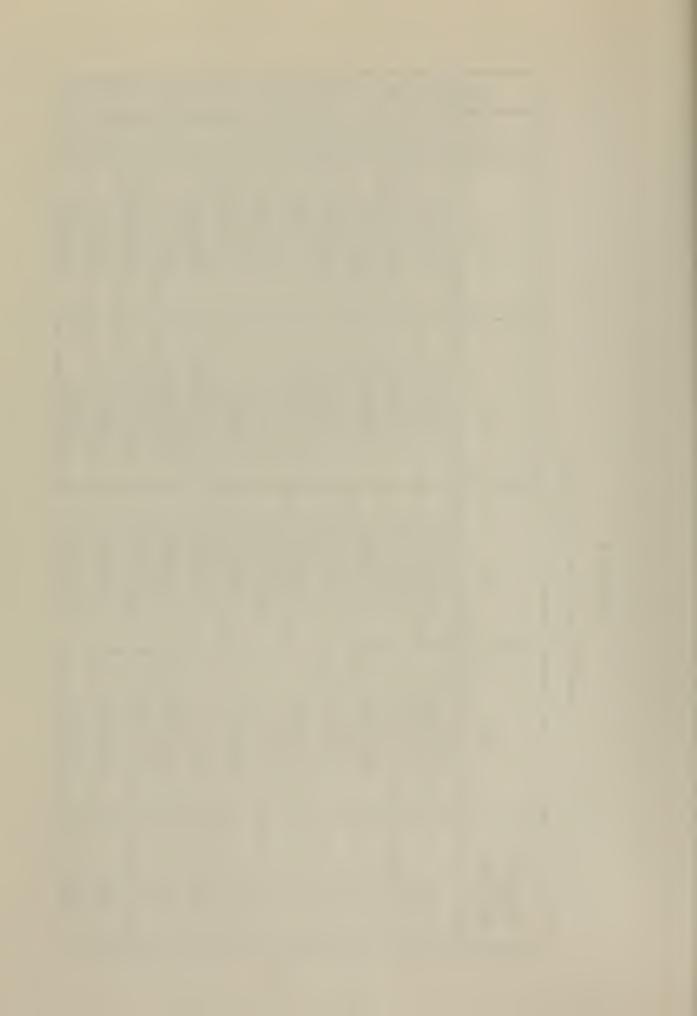
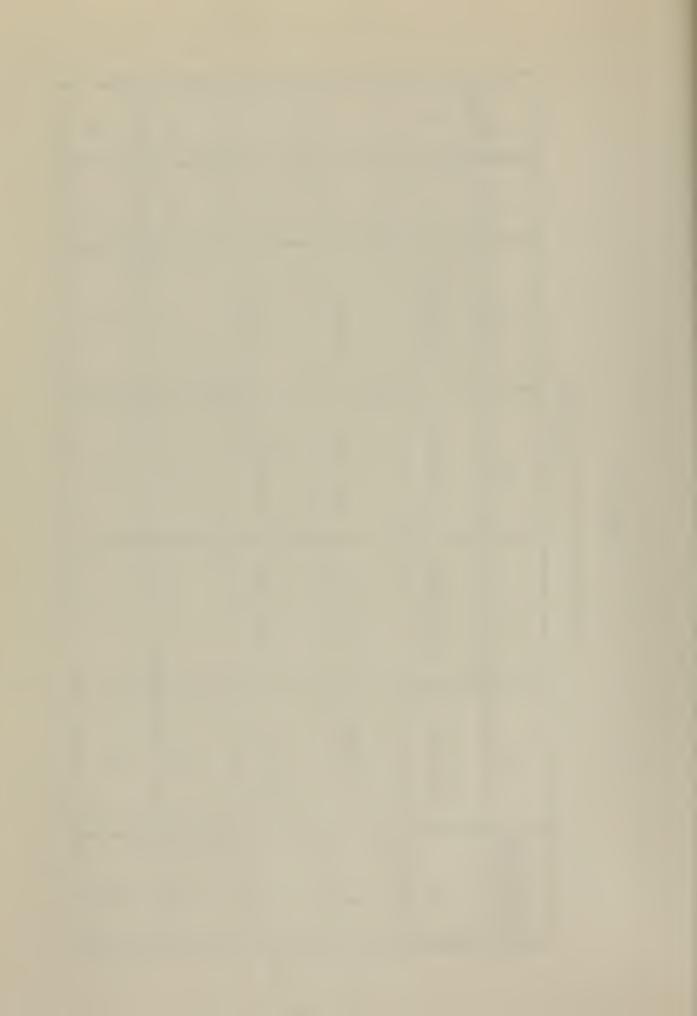


Table A2

Coefficients for Eq. A(13)

Coefficient	c B	5	50	d d		
		T 1	2	5	4	5
AO	1.1078294	-1.70264568	1.070834595	23258418	0	0
A1	.12218714	18703165	.06354814	0044876	0	0
A2	25565987	.628179584	38691079	.08008022	0	0
A ₃	0	0	0	0	0	0
A ₁	0	0	0	0	0	· 0



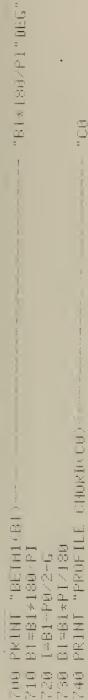
5		.e.nee.	-LLi -			: : : 881 8	1.
ROGRAM - ******HASA35***** - M.P.HAMIJHS - 1/7/76 -PROGRAM TO CALCULATE CUMPRESSOR BLADING PERFORMANCE -BASED UPON EMPIRICALLY DERIVED DATA (REFERENCED BY - "AEFOUYNHMIC DESIGN OF AXIAL CUMPRESSORS"*NASA.1965, -INPUTS REQUIRED ARE AIR IM ET ANGLEYBICHORD LENGTH, -CANBER ANGLE,THICKNESS CHORD RATIO.STAGGER ANGLE.& SOLIDITY.	учырыкино имырылын рырыбыры 24.60 STAGGEM ANGLERGуRUÈG, китыраар	GER ANGLEKGUMMAN MANANANANANANANANANANANANANANANANAN	D WITH SHARP LEAD.&TRAILING EDGESCE/ DIA. OF CONE THRU STACK RADIUS";	105 R9 5		S AT ROTOR INLET(RI)	NESS(T)
		HT "STAGGER ANGLE(G) P "ENTER E"; JT E	FRINT "CHORD MITH SHARP LE DISP "ENTER DIA, OF CONE T INPUT DØ RI=DØ/2	"INPUT TIP R0 "Thour And	INPUT 58	RADIU "RADIU "RADIU "RADIU "ENTER" T	L "THICK "ENTER F R9
KKKKKK Padada EEEEE	<pre></pre>		0000 N 0000		000: tuvu		320 PRIN ⁻ 330 DISP 340 INPU ⁻

TABLE A3 PROGRAM LISTING



"Pel" DEG 1. 1. 1. 1. 20 00 : 14 17 mm DISP "ENTER ANGLE OF COME THRU STACK, RADODE."" PETHI TENTER REPEAS OF PROFILE CONTOUR (\$5) ELCOPTRONC BUILDER ABINE. ASIO H2=(10+2.624*TAN(H)-7.16)/3.84 PRINT "BLADE CHARER ANGLE-PO-H1=((D0-1,376*[ARCH))/5,5)+1 D3=(D0/2-0.688*TAN(H))*2 04=(D0/2+1.312*TAN(H))*2 DISP "ENTER T(TOTAL)2"; ---U2=(P1*R*D4)/(30*24) PUPPER SURVEY STREET U1=(P1*R*D3)>(30*24) PRINT "SOUIDITYERD DISP "INPUT TI TOTAL PRINT "SPACTAGES ----V8#109.62*(50R(T8)) DISP "ENTER APR": --- (A) MGAT INTRA 3年(F1424K1)(13 [S=(1-\112)*T2 []=T1+459.688 [2=12+459,688 BI=PIN(UL/V3) [4~08]*04=04 H=H*P1×130 X=Ex+2+R11 50808 3430 G0808 3150 INPUT T2 THPUT CO IHPUT T1 V3=Y1*V8 H TUAHI INPUT R 50=08×8 993 H H H 12.1 (1) 065 100 000 말는 995 비가는 ा ् जि S S T 598 200 10 00 00 00 949 949 이 나 다 아이 다 0 1 0 300 999 0 N 0 800 619 600 628 000 010 000 66.8 0 74 10 00 0 0 0

TABLE A3 (CONTINUED)



T Restriction

[]]], [] PRINT "THICKNESS CHORD RATIO-760

PRINF PRINT 977 279

PRINT 962

010

DATA 8.000636.-0.001466.0.000087.0.0.0 000

0.000671.0.086416.0.000831.0.0.0 DATA

-0.002147,-0.008859,-0.000475,0,0,0 DATA 0008

0,0,0,0,0,0,0 DATA 10 10 00

0.01.0 0,0,0,0,0,0 020

DATA 0.0.0.0.0.0.0.0 000

(18)2N3=01 ා ල රා

988

I9~180*10/PI

"TO"DEG" ----FIGURE 137---PRINT "ZERO CAMBER INCLDENCE ANGLE Ξ = FRINT 99 ତ | ତ 900 00

000

REM----CALCULATE SLOPE FACTOP(N) FROM FIGURE 138

89-1X 000

REM----COEFFICIENTS FIG. 138 000

DATA 0.013041, -0.376566, 0.774974, -0.768297, 0.306622, -0.050579
DATA -0.879264, 3.402177, -5.761135, 4.962011, -2.053883, 0.325004
DATA 0.384817, -2.637453, 4.778125, -4.148041, 1.706835, -0.267415 990 DATA 0.0.0.0.0.0.0 969 000

(800 DATA 8,8,8,8,8,8,8

DATA 0.0.0.0.0.0.0 010

1020 N=FNZ(B1)

PRINT "SLOPE FACTOR(A) ---- FIGURE 138--PRINT 040

<u>-</u>:



<pre>KENCHLCULATE CORRECTION FACTORCTID FRUN FLUNKE 142 DATN -0.000137.19.136403.125.755414.243.82285.0.0 MAT READ A V1=FNP(T0) PRINT "CORRECTION FACTORATEFIGHRE 142 **** PRINT "CORRECTION FACTORATEFIGHRE 142 **** PRINT "****2-01N. KEFERENCE ANGLE*** PRINT "****2-01N. KEFERENCE ANGLE*** PRINT "****2-01N. KEFERENCE ANGLE*** PRINT "****2-01N. KEFERENCE ANGLE*11).*** "II"DEG" PRINT "****2-01N. KEFERENCE INCIDENCE ANGLE*11).*** "II"DEG" PRINT "****2-01N. KEFERENCE ANGLE*** PRINT "****2-01N. KEFERENCE ANGLE*11).*** "II"DEG"</pre>	u XI=SU 0 REMCOEFFICIENTS FIG. 168 0 DATH 1.6515028+-4.463623015.6.1054043694.416738437.1.610496857.0.2327375 0 DATH 0.182868+-0.428030048.0.3399643750.060885158,-0.059347634.0.02260378 0 DATH 0.182868+-0.428030048.0.3399643750.060885158,-0.051968577634.0.02260378 0 DATH 0.559236.2.18965113+-3.158964364.2.3046766,-0.819050758.0.111924774 0 DATH 0.000.0.0 0 DATH 0.000.0.0 0 DATH 0.000.0 0 DATH 0.000.0 0 PATH 0.000.0 0 PATH 1.5LOFE FACTOR.N)FIGURE 168
1050 1050 1050 1110 1120 1120 1120 1120	

REM----CHLOULATE VARIATION OF AVERAGE REF. INCIDENCE ANGLE MINUS LOM-REM----SPEED 2-DIM.-CASCADE-RULE REF. INCIDENCE ANGLE(19)--FIG.201--КЕМ----САНСИНАТЕ ЗНОРЕ АТ КЕРЕКЦИСЕ ТИСТИНОЕССЭЭ ЕКОМ FIG. 177 " D2" DEG" "D-DEG" 5 기 :: Z=DIM REFERENCE DEVIATION ANGLE(D2)**** -0.477233144,-0.10769486,0.33398654,0.02129055,0.0 DATA -2.30672898.-0.3060019.1.03794405.-0.16526256.0.0 1.83879369.8.31632269.-1.05934646,-0.86984133.0.8 DATA 0.96354267.0.11284222.-0.29730246.0.19355914.0.0 REM----CHLOULHTE CORRECTION FACTOR(N-> FROM FIG. 172 "***2*DIM. REFERENCE DEVIATION ANGLE(D2)**** "SLOPE AT REF. INCIDENCE ANG. (M9) -- FIGURE 177 DHTH ~0.001662.8.248814. 6.181318.231.64355.0.0 REM---BEGIN CRECKLATIONS FOR S-DIM. EFFECTS "CORRECTION FROTOR(K2)----FIGHRE 13. "****2~DIM.DEVIATION ANGLE(D) **** REM****CALCULATE DEVIATION ANGLE(D) **** A0=50R(1.402*32.174*53.35*T8) A1=S0R(V3*2+U1*2) REMARACHLOULHTE D2=K0*K2*D1+M*P0 DATA 0,0,0,0,0,0,8 0ATA 0,0,0,0,0,0,0 D=D2+(I-II)*K9-K9=FNZ(80) HAT READ A K2=FNP(T0) = -= M1=43×60 : MS=W1/A0 . = PRINT PRINT PRINT Set PRINT PRINT PRINT PRINT PRINT TNI 94 PRINT DATA PRINT DATE: 방방 ा ् च 00 7 7 90 7 919 218 8 04 17 20 00 10 949 949 900 10 10 10 10 ି ବିତ୍ର 619 ୍ ଅତ୍ରତ୍ର 648 0000 000 3 0 0 788 20 04 N-999 ی م 912

TABLE A3 (CONTINUED)



TABLE A3(CONTINUED)



-'UI'FT. ZEE.' "U2"FT. /SEC. DEVIBIION ANGLE AT . D30. 60. "luc"lec" PRINT "--MINUS LON SPEED 2-DIN. CASCADE-RULE PRINT "****S-DIN. DEVINTION ANGLECDG)+*** "COMPRESSOR REFERENCE THUTDENCE AND E REM----CAL. 3-DIM. REF. DEVIATION ANGLE---19.081*18° Ē 22 月日年50月(11年9月年30日。17年4月9日。30日年19月) V.L=SQR(V5*2+V3*2) V9=109.62*80R(T2) B2=B1-(P0+76-D6) V2=V4×(COS(A2)) -TUHUTU. M2=44/(005(B2)) []=(]-Y2*2)+[]=0] R2=ATH(V6/V4) "UI -----A1=A14(45-43) NG=N1+SIN(B1) N4=N2+SIN(B2) 11 1 1 1 million and a second second B1=B1×P1×180 B2=B2*P1 /180 A1=A1+180.771 "BETAL B1=B1*180 P1 ---- [UA ... 44 44 -11 11 NZ=VZZAB - 64×34=34 16=1+19 = ¥6=U≳-M4 0A=+A FIR NI LHT 광리 PRINT PRINT PRINT PRINT PRINT PRINT PR PRINT PRINT PRINT 0-58 BCCC 2120 2130 9000 0000 0900 2300 2310 2340 2190 0923 0022 Baco Soco 9343 944 2160 2170 2130 2200 0100 0222 0000 0000 0000 0000 2110 ୍ୟ ୧୦ ୧୦ 0000 S N S 01-1 7 2150 යා ගා ලා 문수입법 00000

TABLE A3 (CONTINUED)

YU1 WI WI WI WI WI WI WI WI WI WI
PRINT PRINT
88888888888888888888888888888888888888

F 19=0 THE HATN "BPLOT RTNT TOP TOP AT READ 6 AT READ 7 AT A=6 AT A=7 AT A=6 AT A=7 AT A=6 AT A=7 AT A=6 AT A=7 AT A=7	

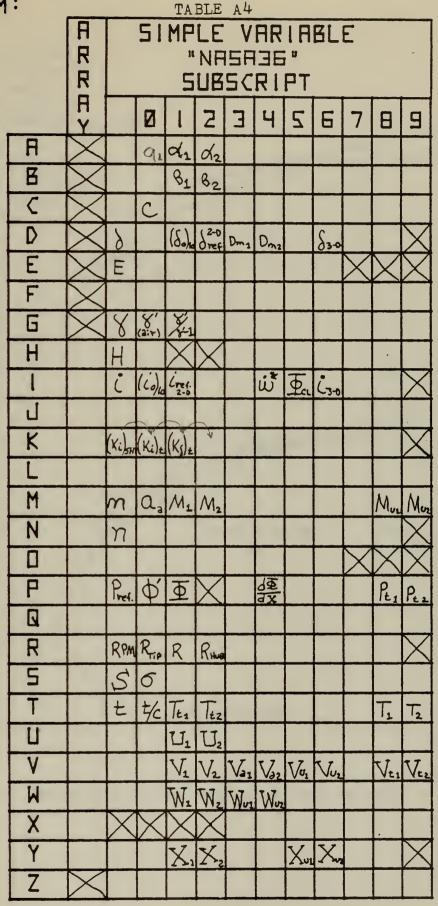
TABLE A3 (CONTINUED)

P1=(0.954823+0.082347*(H1)+0.163275*(H1)+2.0.255 Ple(0.896413+0.3472218H1 0.220228*4H1 12-0.19712*4H1 233)*15 P1=(0.9205345.299223541.40.299226441.40.25823644(H1)*24240.0447488(H1)*8)*15 P1=(0.857467+0.496997*(H1)+0.40696*(H1)+2-0.85361*(H1)+3)*15 Р1=(1,009099-ы,088129тН1+0,290343*(Н1)+2-0,300944*(Н1)+8)*15 P1=(0.964092+0.(19941*H1-0.0189?*(H1)+2-0.154942*(H1)+3)*15 P1=(0.98905-0.017937*H1+0.219834*(H1)+2-0.28032*(H1)+3)*15 -THIS SCHEME THES THE VALUE OF REFERRED FLOW RATE P4#P4+(-2*Y1*2)*(1×(G0+1))*(1+Y1*2)*(1>(G0+1)+1) AND OBTATING THE CLOSEST CURVE HEPROX. FIT REM---SUBROUTINE TO CAL NOM-DIM VELOCITY(S)-[4>10.135 AHD 14 -= 11.035 THEN 3030 14>11.035 AHD 14 -= 11.3 THEN 3050 14>11.3 AHD 14 -= 12.625 THEN 3070 14>12.625 AND 14 -= 14.065 THEN 3070 LF 14×9.165 THEN 3290 LF 14>9.165 AND 14 <= 10.135 THEN 3310 CONFETCIENTS FOR FLOW CURPE. IF ABS(P2-P1)(0.000001 THEN 3520 -P2=Y1*(1-Y1*2)*(1/(G0-1)) 14-14.065 THEN 3410 P4=(1-Y1+2)+(1/(G0-1)) Y1=Y1+(P1-P2)>P4 GOTU 3420 GOTO 3420 GOTO 3420 GOTO 3420 1010 3420 G0T0 3420 GOTO 3460 60=1.402 41=0**.**15 RETURN NEM - --RETHRN REP R I I 00000 0400 3346 3350 3366 3478 3488 0000 0000 332B 332B 8888 8888 8888 00000 3310 3400 0410 0410 0400 9788 2370 09220 0000 00000 3430 3440 3450 3460 0000 301 B

TABLE A3 (CONTINUED)



PROGRAM:



SCORE SHEET: RECORD OF VARIABLES USED.



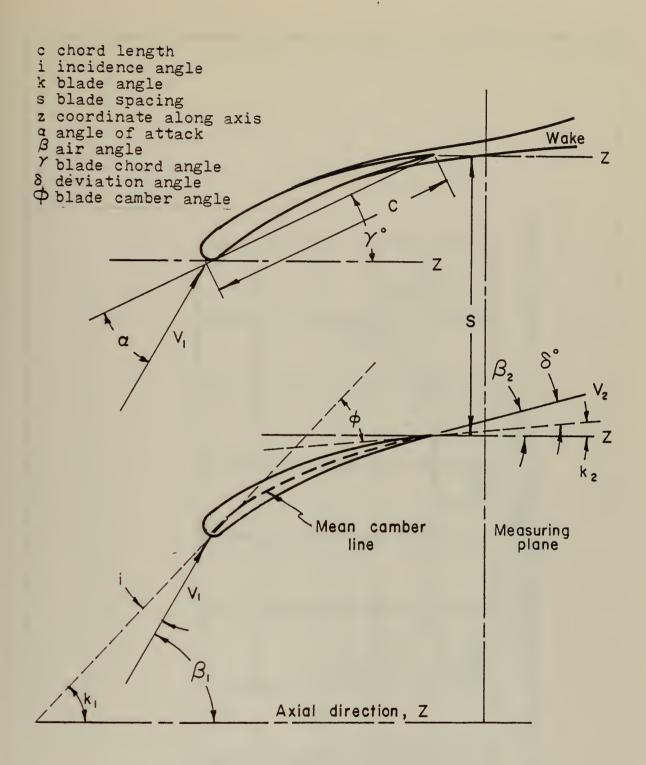
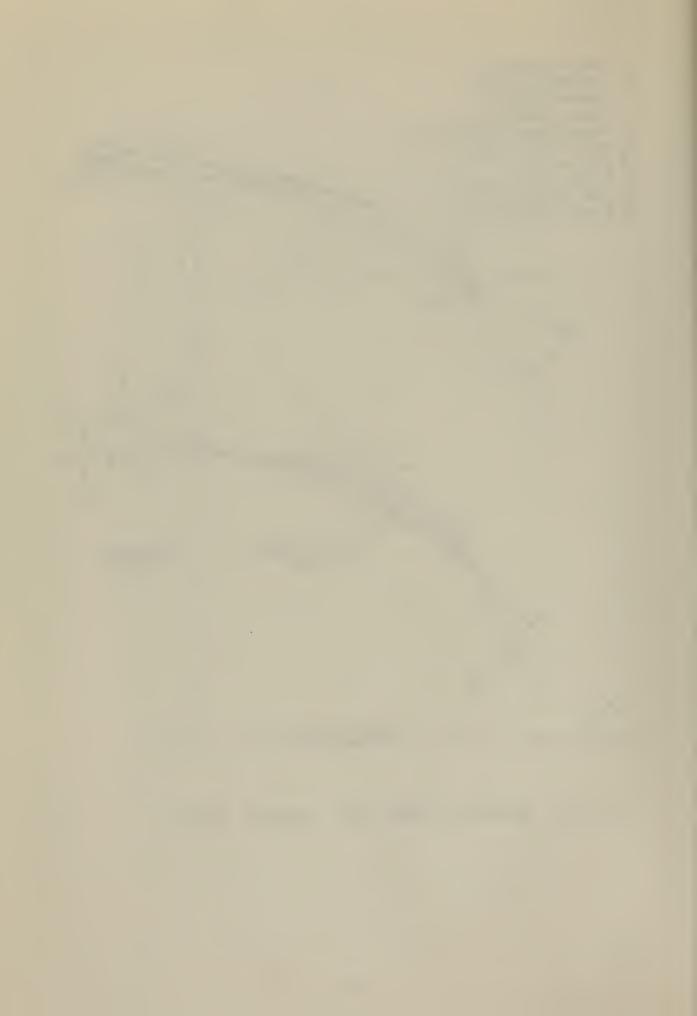
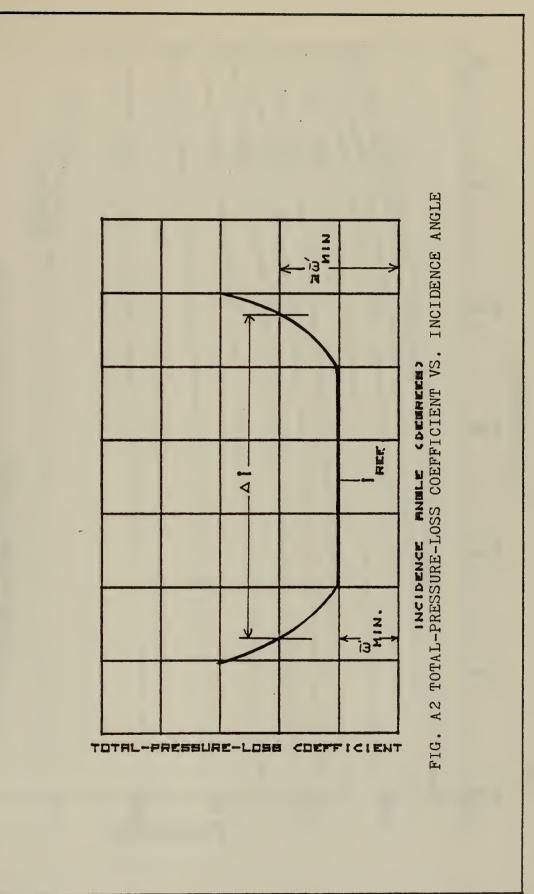


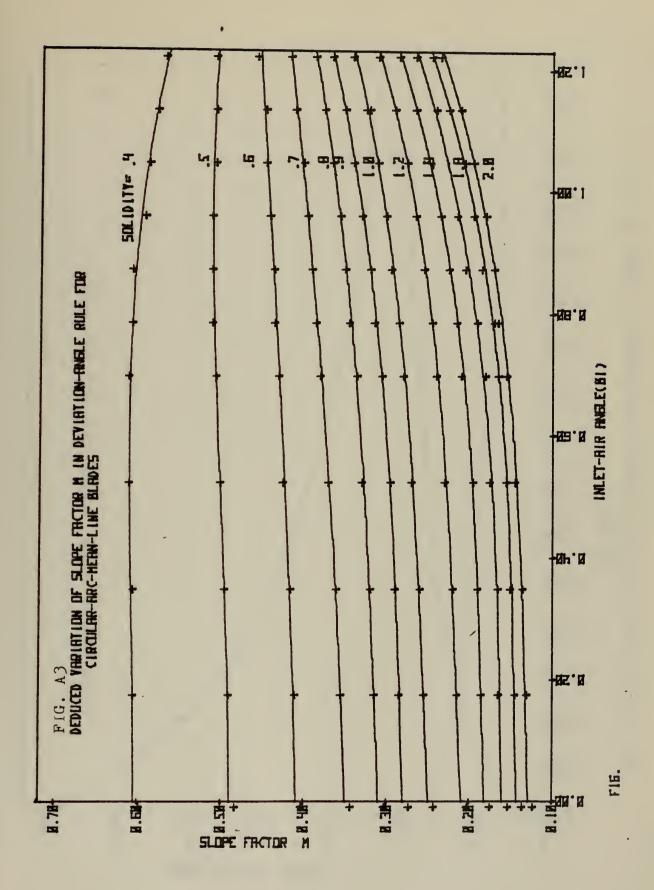
FIG. A1 NOMENCLATURE FOR CASCADE BLADE





. 79

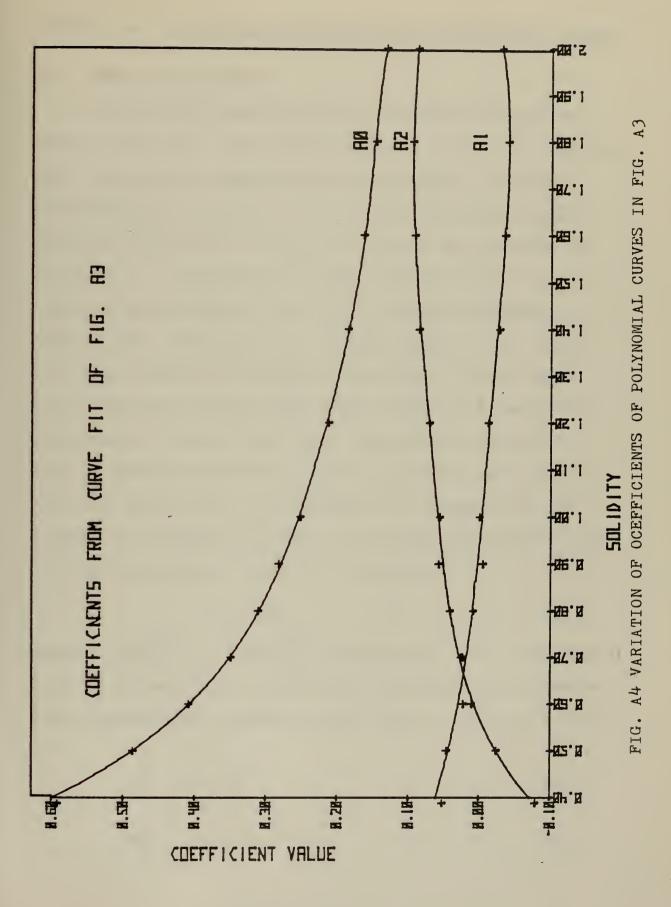


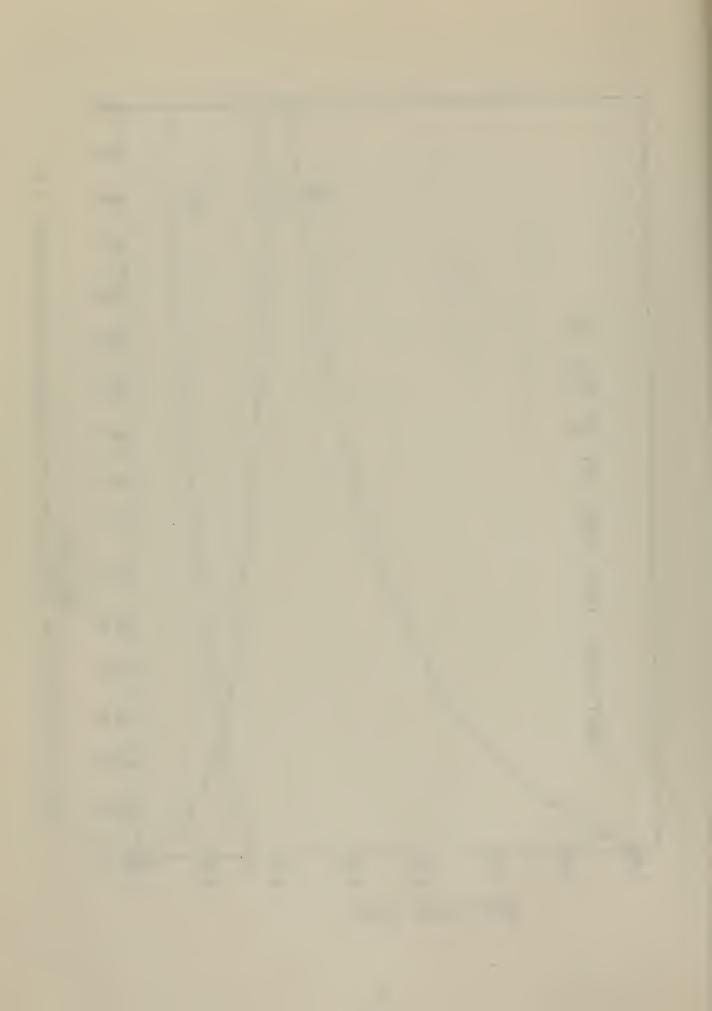


80

•

-





APPENDIX B: CALIBRATION AND CORRECTION OF PNEUMATIC PROBES

B1. FREE-JET APPARATUS

The free-jet apparatus used to calibrate probes is shown in Fig. B1. The device consisted of a 8 inch diameter pipe with the air supplied by the laboratory's central Allis-Chalmers Compressor. A 4.2 inch converging nozzle was used to increase velocity and attain Mach numbers up to about .9. To determine if the exiting velocity was uniform and undisturbed by the probe mounting arrangement, surveys were conducted with a Prandtl probe over a range of 5 Mach numbers at two axial locations. Surveys were also conducted with the same probe mounted and traversed from opposite sides of the jet. The results shown in Fig. B2 indicated that the velocity profiles were uniform over the core of the jet extending to a diameter of 3.8 inches. As suggested in Ref. 11, the non-dimensional velocity (X) appearing in Fig. B2 is defined by

$$X = V/V_t \qquad B(1)$$

where $V_t = \sqrt{2C_p T_t} = 10\%.62\sqrt{T_t}$ when T_t is in ^oR. Following Ref. 11 further, the relationships for stagnation pressure, total temperature, and Mach number are, in terms of X given by

$$\frac{T}{T_{t}} = 1 - X^{2}$$
 B(2)

$$\frac{P}{P_{t}} = (1 - X^{2})^{\frac{6}{7}} / (\frac{6}{1})$$
 B(3)

$$M = \frac{V}{\sqrt{3}RT} = \frac{2}{\sqrt{3}-1} \cdot \frac{X}{\sqrt{1-X^2}} B(4)$$

The values of X in Fig. B2 were calculated using the measurement of stagnation pressure and the assumption of atmospheric static pressure in Eq. B(3).

B2. CALIBRATION OF THE COMBINATION PROBE

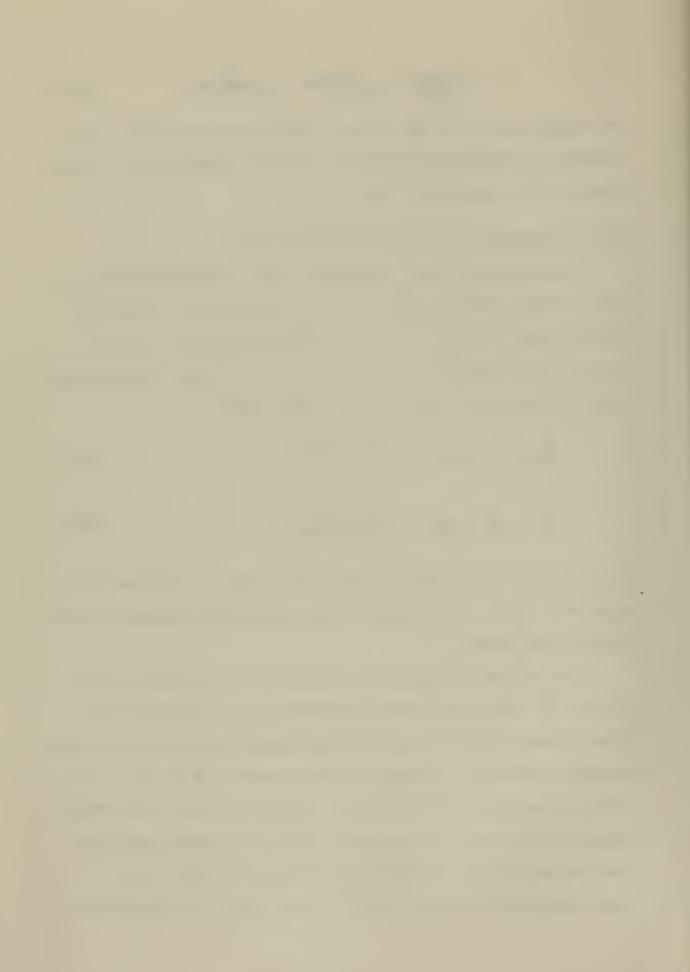
Calibration of the pneumatic probe reported in Ref. 2 can be represented by defining two functions of the nondimensional velocity, X, and the pitch angle, ϕ . If P₁ and P_{2/3} are indicated stagnation and indicated static pressure of the probe respectively, then define

$$F_{\Theta} = F_{\Theta} (X, \phi) = \frac{P_1 - P_2/3}{P_1} B(5)$$

$$F_{\phi} = F_{\phi} (X, \phi) = \frac{P_1 - P_4}{P_1} B(6)$$

to be calibration functions when the probe is rotated to balance $P_2 = P_3$. P_4 is the fourth, off axis pressure measured by the probe.

The complete calibration procedure is given in detail in Ref. 3. The probe was recalibrated to confirm the results given in Ref. 2 before investigating corrections for boundary effects. A range of Mach numbers (X = .13 to .4)and pitch angles $(-20^{\circ} \text{ to } 20^{\circ})$ were used. With true static pressure taken to be atmospheric and true impact pressure that measured by a reference Prandtl probe, the value of X was calculated from Eq. B(3). As in Ref. 2, polynomial



representations were found for the calibration equations written in the form

$$X = X(F_{\boldsymbol{\theta}}, \boldsymbol{\phi})$$
 B(7)

and

$$F_{\phi} = F_{\phi} (X, \phi) \qquad B(8)$$

where F_{θ} , and F_{ϕ} are the ratios of probe pressure measurements defined in Eq. B(5) and Eq. B(6). It is noted that Eq. B(6) departs from the definition used by D₀dge in Ref. 2. The present method was found to give more accurate results. The coefficients in Eq. B(7) and Eq. B(8) derived from the calibration test results are given in Table B1.

As a test of the analytical representation of the calibration, the calibration data were used to calculate values of X and ϕ to compare with the actual values. Table B2 shows the results of this comparison for the velocity. The error in X is generally less than 1% and only reaches higher values at high positive or negative pitch angles (16° or -8°) or at higher Mach numbers (.88). At this point the error increases to about 2%.

Fig. B3 shows the error in the pitch angle in the range of pitch angle from -4° to $\pm 12^{\circ}$. The error is seen to be $\pm 1\frac{1}{2}^{\circ}$ and is not a simple function of either pitch angle or Mach number (or X). There appears to be a limit to the capability of resolving ϕ . The error was larger at high negative and positive values of pitch angles but these were outside the intended range of use.



B3. BOUNDARY EFFECT ON COMBINATION PROBE MEASUREMENTS

In application, the probe is not in plane flow away from all boundaries. The indicated velocity and pitch angle will depend upon several factors including boundary layer and stem immersion effects. The method of approach assumed here was that the probe always obeys the calibrations established and that errors are induced due to the perturbation of the probe itself on the flow near the boundary. Thus, in any flow the probe measures a velocity, X, and a pitch angle, ϕ , which are the sum of the actual and an "induced" component.

Three surveys were conducted in a 10 inch pipe up to the maximum attainable Mach number of .55. The results of calculating velocity applying the free jet calibration given above are shown in Fig. B4.

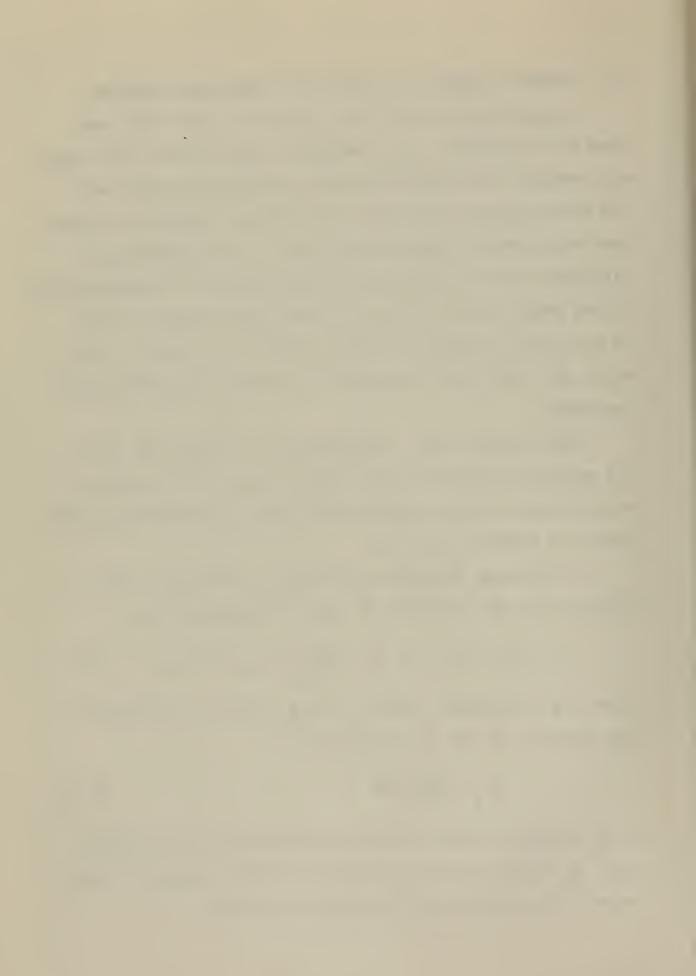
Introducing subscripts a(actual), i(induced), and m(measured), the velocity, X, may be represented by

$$X_{m} = X_{a} + X_{i} = X_{a} \left[1 + \frac{X_{i}}{X_{a}} \right] = X_{a} \left(1 + \epsilon_{x} \right) \qquad B(9)$$

where the fractional 'error' in X, ϵ_x , which is induced by the presence of the wall, is given by

$$E_{x} = \frac{X_{m} - X_{a}}{X_{a}}$$
 B(10)

 $X_{\rm m}$ is determined from the probe calibration in the usual way. $X_{\rm a}$ is the required, correct velocity, and $\epsilon_{\rm X}$ is the error to be established by calibration tests.



The measured velocity is corrected using

$$X_{a} = \frac{X_{m}}{1 + \epsilon_{x}} B(11)$$

when the error \in_{x} is known.

In the same manner actual pitch angle may be represented by

$$\phi_a = \phi - \epsilon_{\phi} \qquad B(12)$$

In the 10 inch pipe tests, the actual velocity was calculated from the probe impact pressure and pipe wall static pressure using Eq. B(3) and the actual pitch angle was zero. Thus the "induced" error in X was calculated using Eq. B(10) and the "induced" error in ϕ was calculated using Eq. B(12). The two errors, ϵ_x and ϵ_{ϕ} , were then examined as a function of distance from the pipe walls expressed as a number of probe diameters; (the characteristic dimension of the probe was taken to be 0.1 inches). It was found that the errors became negligible at about 9.5 probe diameters from the boundary. In order to derive an expression of a suitable form, the errors were plotted as a function of (9.5-D), where D is the displacement as a number of probe diameters. The velocity error was then approximated by a polynomial of the form

$$\epsilon_{x} = A_{0} + A_{1} (9.5 - D) + A_{2} (9.5 - D)^{2} B(13)$$

where D is measured from the wall through which the probe was inserted. The result is shown in Fig. B5. The error was less than 2% at distances greater the 0.25 inches from



the wall. In order to extrapolate the correction to larger values of velocity, the error was represented as a function of X. The coefficients in Eq. B(13) were plotted as a function of X, and the result is shown in Fig. B6. A_0 , A_1 and A_2 were seen to be almost linear functions of X and were therefore approximated by

 $A_{0}^{'} = B_{0} + B_{1}X_{.95} + B_{2}X_{.95}^{2}$ $A_{1} = C_{0} + C_{1}X_{.95} + C_{2}X_{.95}^{2}$ $A_{2} = D_{0} + D_{1}X_{.95} + D_{2}X_{.95}^{2}$

where X.95 was the value of X at D = 9.5. Values of X(corrected) minus X(uncorrected) verses immersion depth are shown in Fig. B7. Because of the aerodynamic design of the probe, the corrections necessary for boundary effects are small.

Results for the induced pitch angle error are shown in Fig. B8. Since these errors were within the resolution capability of the probe $(1\frac{1}{2}^{0})$, no correction was made.

B4. COMBINATION PROBE MEASUREMENTS IN STEADY SWIRLING FLOW Additional errors may be present when a pneumatic probe is immersed in a swirling flow. Fig. B9 shows the apparatus which was constructed to investigate this possibility. The apparatus consisted of an annulus with a channel height of $1\frac{1}{2}$ inches (10 inches in outer diameter). A total of 40 static wall readings were available and a provision was made for probe surveys at different axial stations. The

swirl velocity was generated by a single stage of stator blading at the entrance to the annulus. Initial measurements suggested the possibility of boundary layer separation and reverse flow near the hub. In an effort to correct this problem, a plate was constructed to decrease the channel height at the exit, isolating the pressure at the hub wall from the surrounding atmosphere, and blocking backflow.

Results are given in Fig. B10 which shows the static pressure derived from the probe calibration. Agreement is very close near the hub with a moderate departure near the tip at the highest Mach number.

B5. CALIBRATION OF THE WEDGE PROBE

A type of probe which is reported to give a good indication of static pressure over a wide range of Mach number is the wedge static probe illustrated in Fig. 5. The probe has a hatchet-shaped head with small pressure taps in each face of the wedge. In principle, if the leading edge is sharp and the wedge angle is small, the flow past the sensing orifice will be almost unperturbed, and the measured pressure will be close to the static pressure in the undisturbed flow.

The static pressure may thus be determined by

$$P_{s} = (P_{2/3} - P_{A}) + P_{A} = B(11)$$

where it is assumed the probe is aligned in the flow with P_2 and P_3 equal, and P_A is the reference atmospheric pressure.



The wedge probe shown in Fig. 5 was traversed in both the free jet and the swirling annular flows through the same range of Mach numbers reported for the combination probe. However, the characteristics of the probe in swirling flow were not fully determined. It was found in analyzing the results of the tests in the swirl annulus that the radial gradient in the flow angle gave rise to probe readings which were in error when the probe was rotated to balance. This was explained by the difference in the radial position of the sensors on the two faces of the wedge. It was therefore necessary to use the combination probe to sense flow direction in the compressor measurements and to set the wedge to the measured angle.

	$(X) = a_i^5(X)$	0	0	0	0	0	C		$p_j^{(\phi)}$	0	0	0	0	The state of the second se
()	$a_{i}^{4}(x)$	0	0	0	0	0	0		$p_{i}^{t}(\phi)$. 0	0	0	0	
Fφ(X,9	$a_i^3(x)$	0	0	0	0	0	0	(Fe, Ø)						
for $F\phi =]$	(X)	.430296	223	9	328			for X = X	$b_i^3(\phi)$	64.17796	377.5630	578.1631	-187.416	
fficients	$a_i^2(x)$.430	-5.78223	29.28679	-31.33828	0	0	fficients	$b_{i}^{2}(\phi)$	-16.7985	-76.79957 377.5630	-73.94789 578.1631	138.16714 -187.4164	
Probe Calibration Coefficients for $F\phi = F\phi(X,\phi)$	$a_{j}^{1}(X)$.007201	.0241'52	-7.67746	5.75709	0	0	Probe Calibration Coefficients for X = X(Fe, Ø)	$b_{i}^{1}(\phi)$	3.060194	5.92345	.43807	-17.54476	
Probe Ca	a ⁰ _i (X)	-,031966	.356675	1.065658	6217505	0	0	Probe Ca	$b_{i}(\phi)$.049479	096216	023244	.465854 -	
	Order of Coefficient	Zeroth	First	Second	Third	Fourth	Fifth		Order of Coefficient	Zeroth	First	Second	Third	

Table B1

00

00

00

00

0 0

00

Fourth

Fifth



Table B2

Error Analysis of Limiting Velocity From Combination Probe Calibration

φ	%E	X	X ₁	%E	X	X ₁
-8	1.240859	.131396	.133026	1.294396	.164529	.166658
-4	179254	.131396	.131631			
0	.278352	.131396	.131761	.500537	.164718	.165542
4	-1.363128	.131396	.129604	1.408336	.164718	.016703
8	-1.530939	.131396	.129384	.203496	.164718	.165053
12	-0.680858	.131396	.130501	.651461	.164718	.165791
-8	1.000402	.19477	.196718	.233878	.220488	.221003
-4	-0.117261	.194314	.194086	.152853	.220744	.221081
0	.169147	.104618	.194947	114982	.220616	.220362
4	-0.214012	.194161	.193745	092819	.221253	.221047
8	-0.358790	.194466	.193768	-1.029916	.220871	.218596
12	.376707	.19477	.195503	646592	.220616	.219189
-8	-1.239331	.246923	.243862	.237152	.287457	.288138
-4	-0.034597	.247245	.247159	1.076403	.287457	.290551
0	-0.146786	.247138	.246775	1.024665	.28754	.290486
4	-0.515128	.24703	.245757-	.471649	.287872	.289229
8	-1.285034	.24703	.243855	-1.434447	.287872	.283742
12	-1.132503	.246923	.244126	.699168	.287872	.289884
-8	4.327326	.330596	.344901	.274718	.342723	.343664
-4	-3.051296	.330723	.340814	-1.857185	• 342664	.33630q
0	1.741821	.329579	.335319	-1.009610	.34284	•339378
4	2.010646	•330343		969406	.342488	.339167
8	2.250762	.330089	.337518	-1.002690	.342488	.339053
12	-0.449206	.330089	, 328606	-1,115949	.342547	.338724
	$\phi = F$	oitch Angl	.e	. X = A	ctual Val	ue
	$X_1 = 0$	computed V	alue	%E = %	Error	



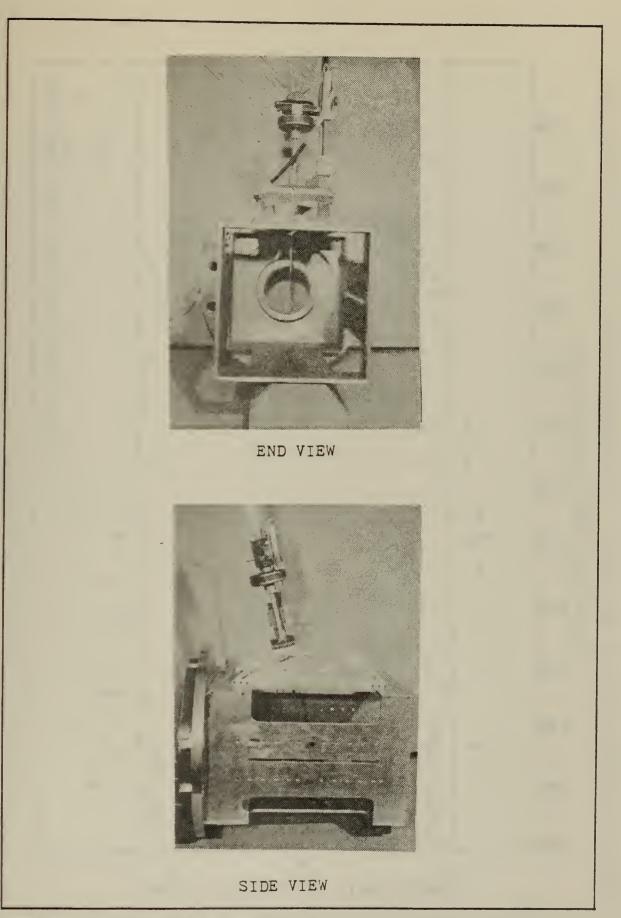
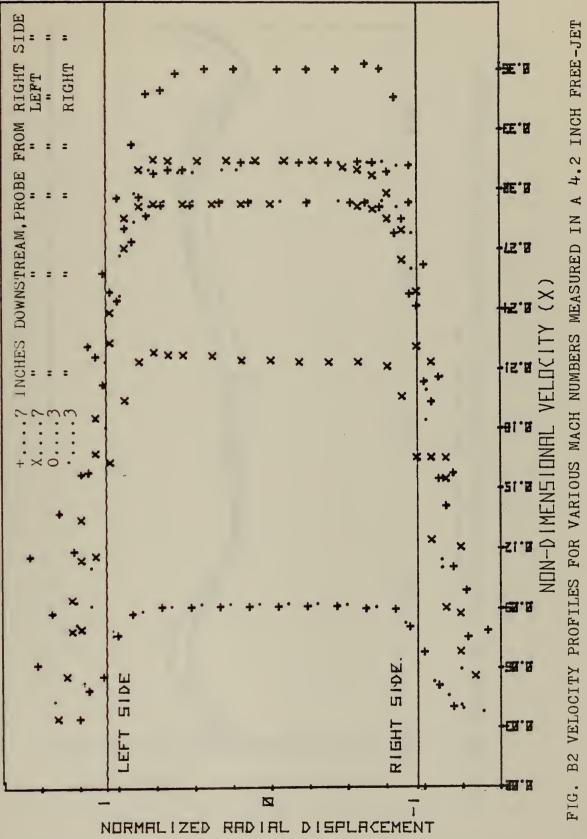
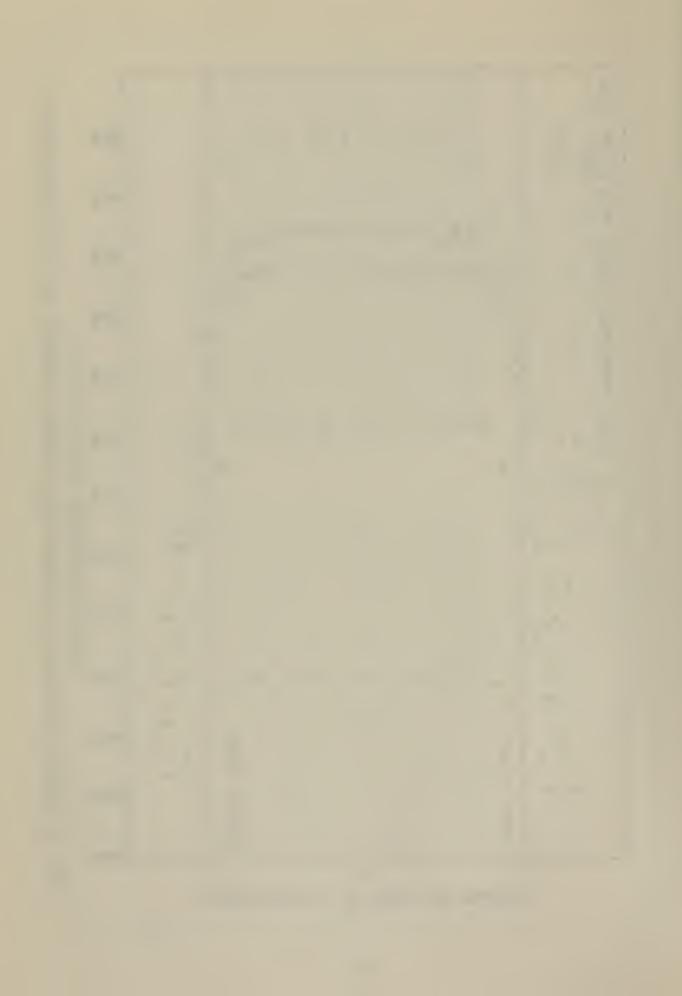
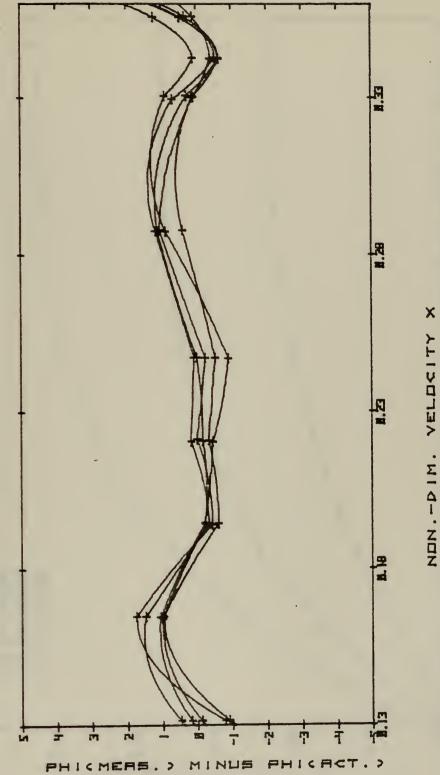


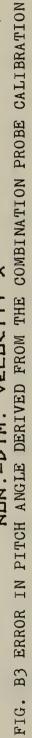
FIG. B1 FREE-JET APPARATUS USED TO CALIBRATE PROBES

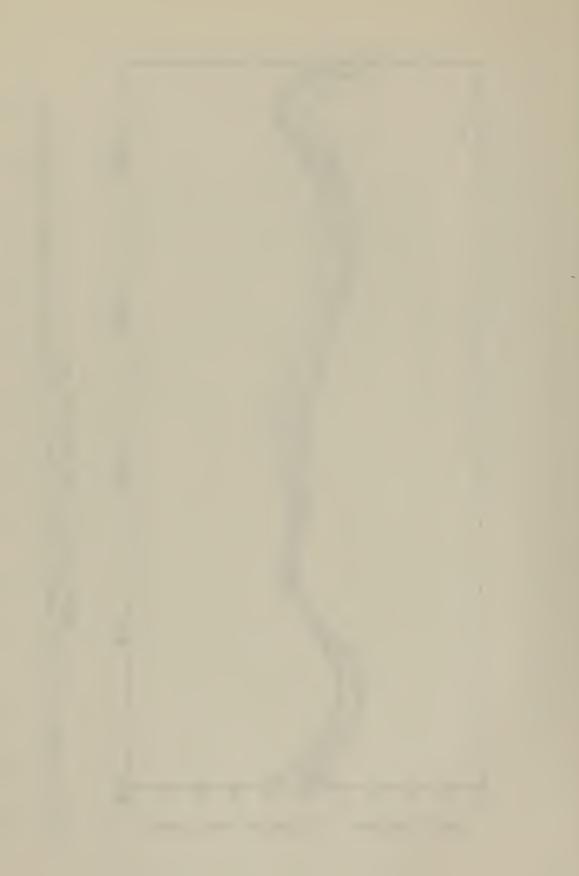


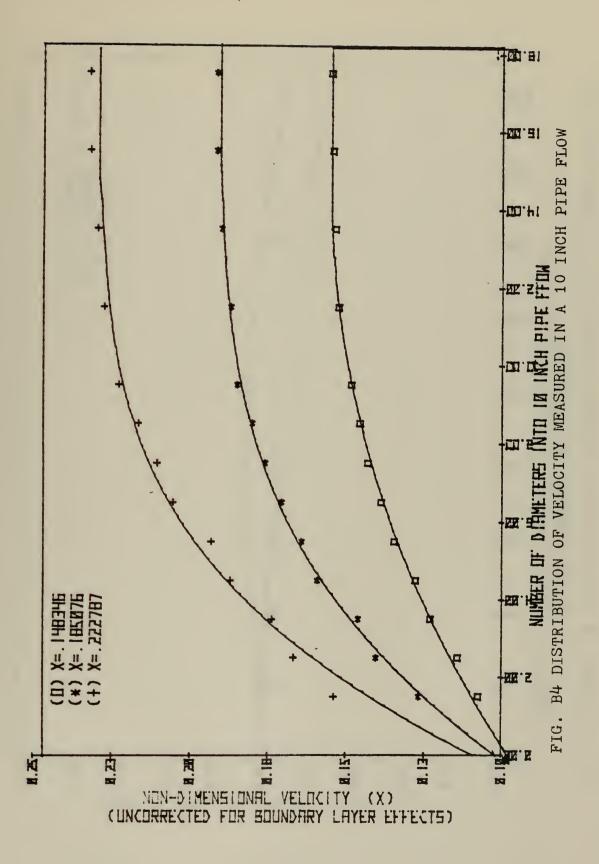




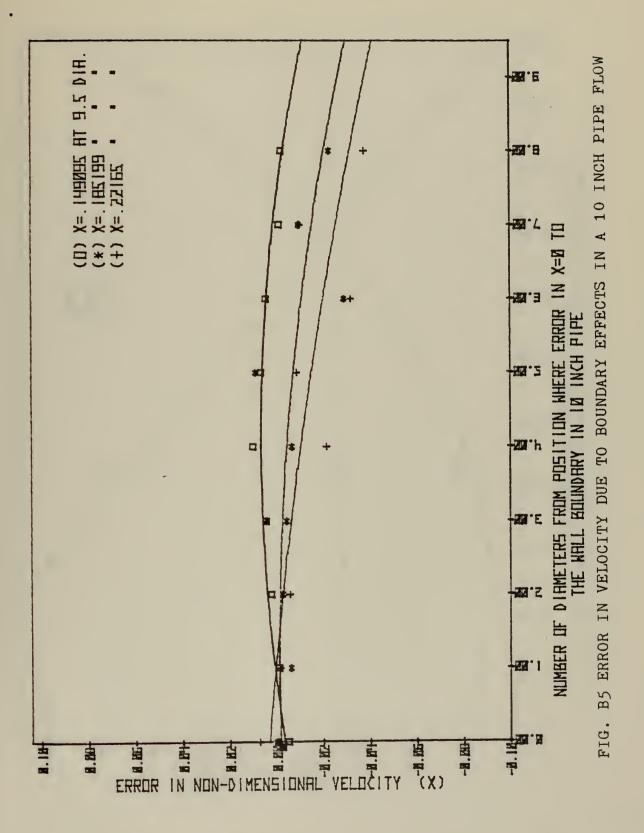


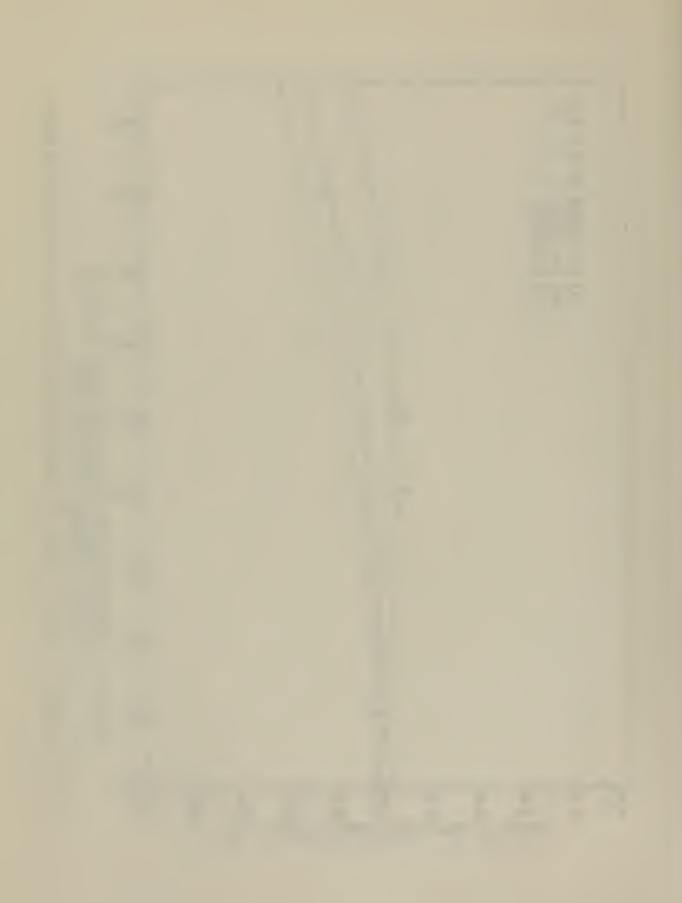


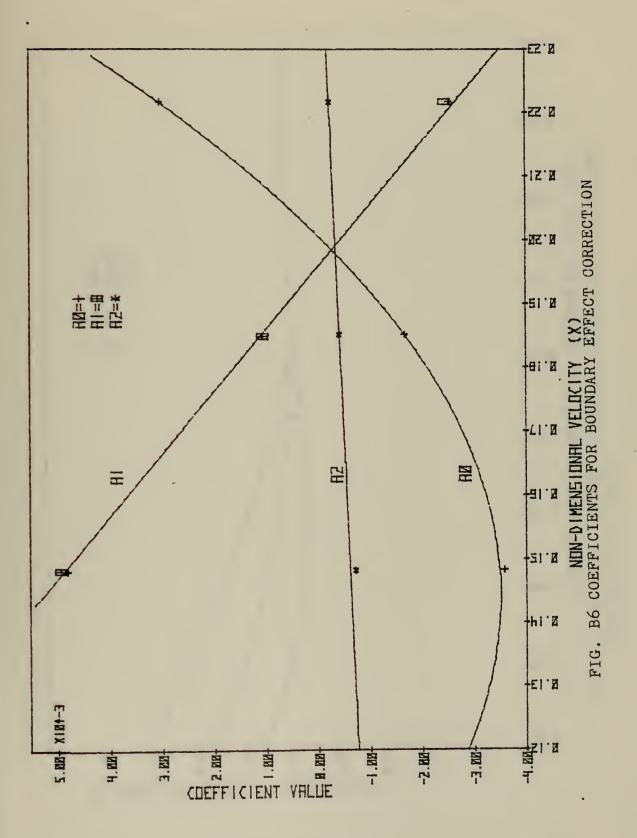


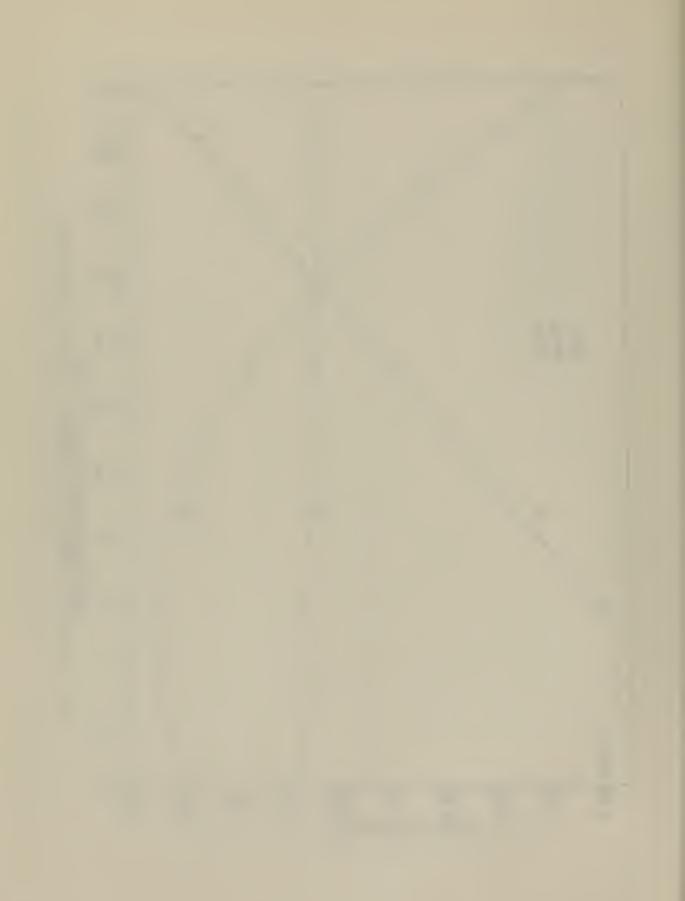


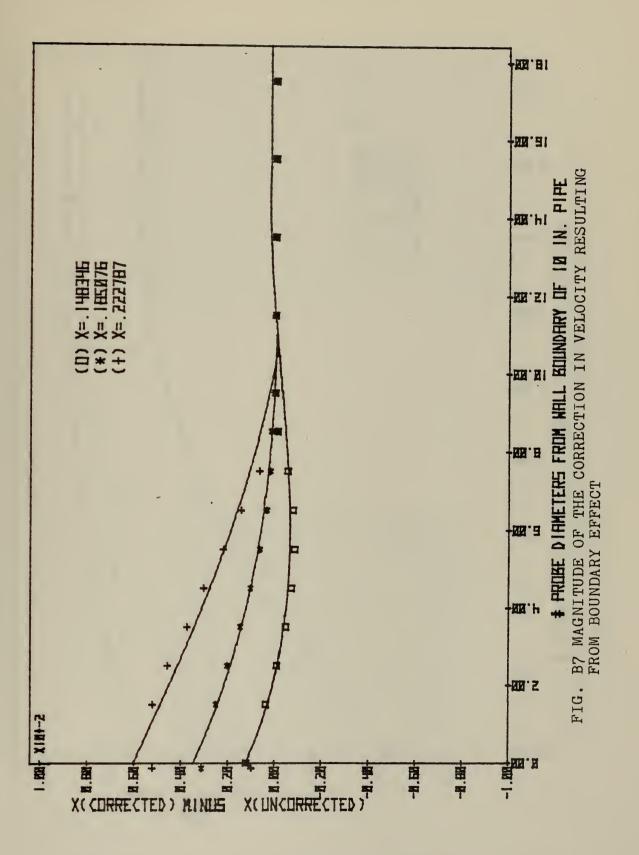


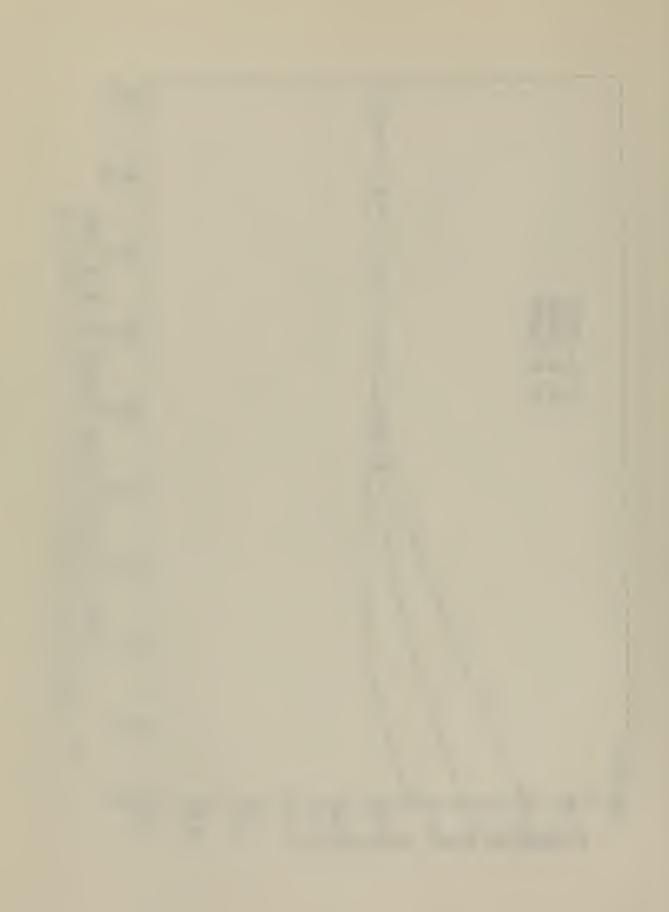


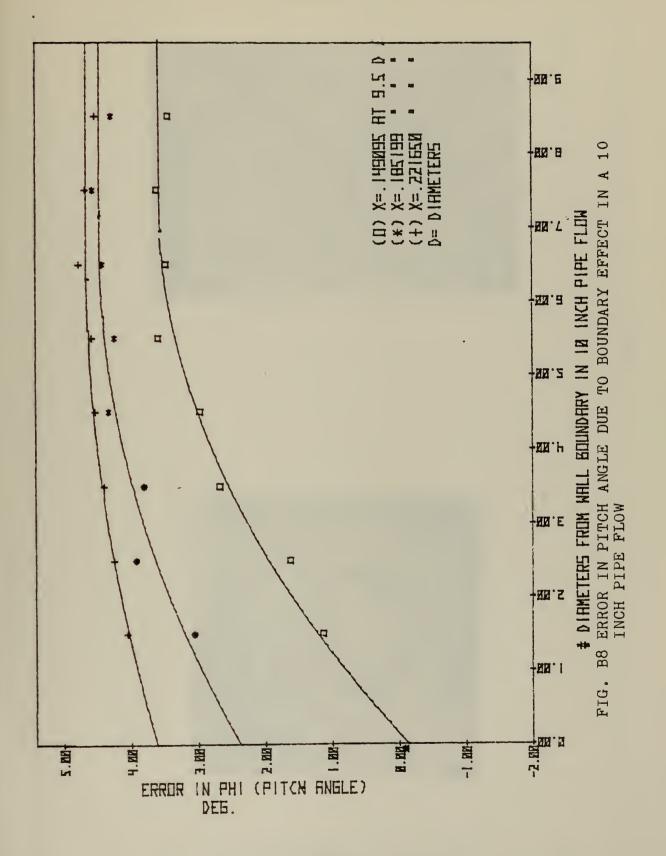


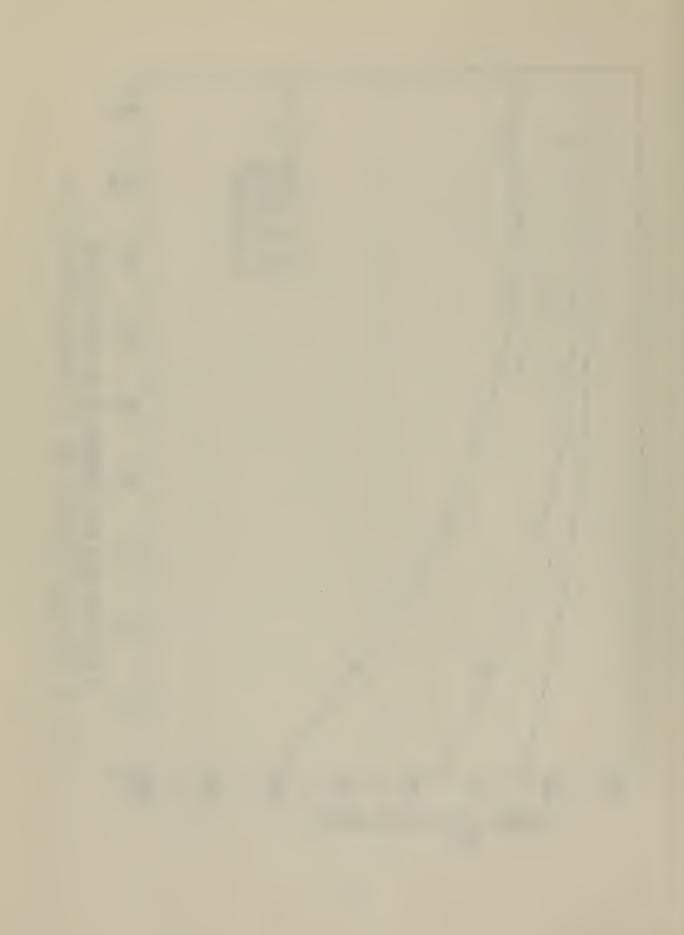


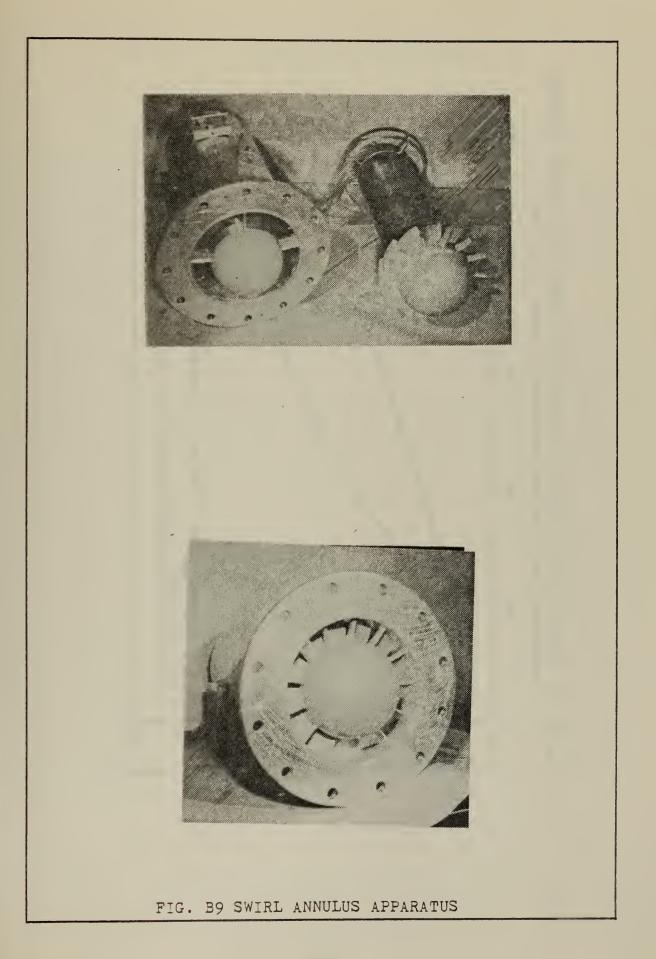




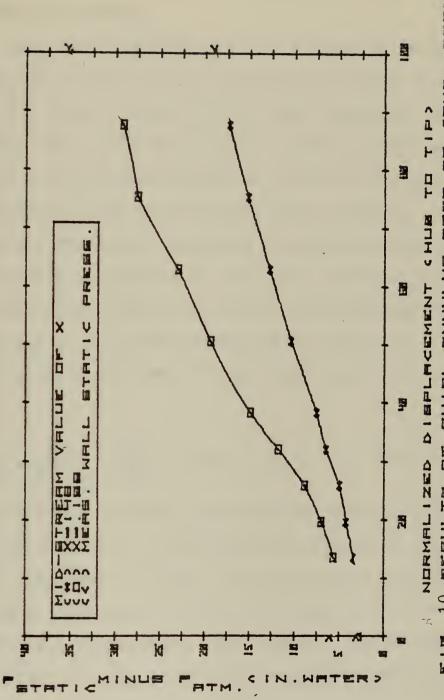


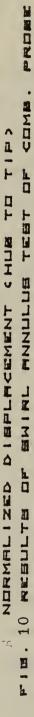


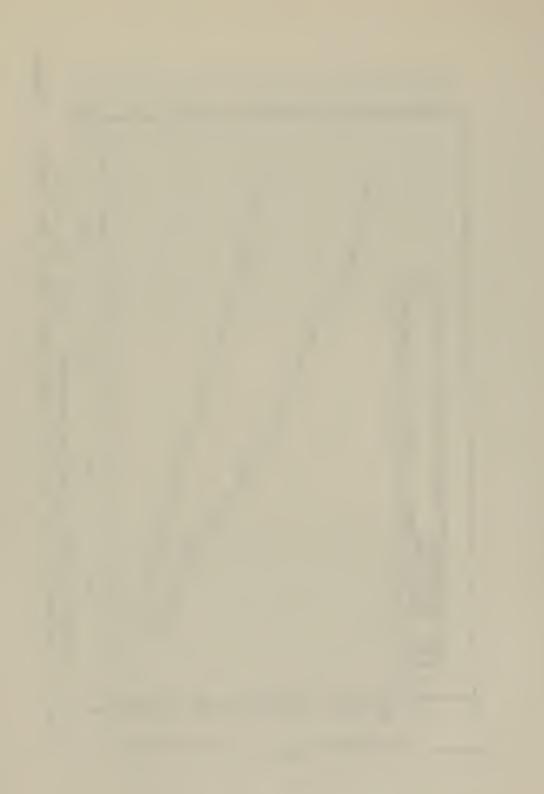












APPENDIX C: INLET FLOW FIELD DETERMINATION

C1. METHOD OF APPROACH

An important consideration in a transonic compressor installation is the velocity profile at the face of the rotor. The profile depends on the inlet shape and the mass flow rate. The following analysis is based on the assumption that a close approximation to the true velocity may be calculated if the referred flow rate is known.

Seven surveys were conducted by Anderson (Ref. 3) in which accurate calculation of the inlet velocity profiles was accomplished using a calibrated United Sensor Probe over a range of flow rates tabulated in Table C1.

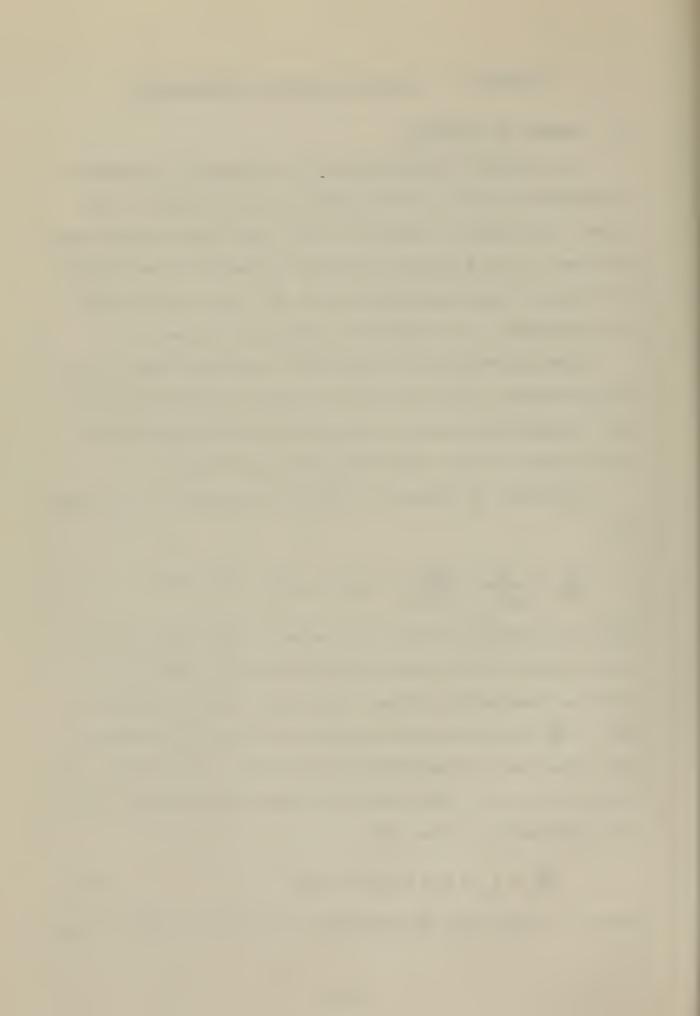
Reference 11 defines a "total flow function," , given by

$$\Phi = \frac{\hat{q}_{V}}{\hat{q}_{t}^{V}t} = \frac{\hat{w}_{A}}{\hat{q}_{t}^{V}t} = F(X) = X(1 - X^{2})^{1/(v-1)} C(1)$$

The flow function provides the means of replacing density in the equation with the non-dimensional velocity (X) for internal compressible flows. For each survey conducted in Ref. 3, Φ was calculated at each point and plotted versus the normalized displacement (hub to tip). The results are shown in Fig. C1. Each curve was then fitted with a suitable polynomial of the form

$$\Phi = a_0 + a_1 H + a_2 H^2 + a_3 H^3 + \dots C(2)$$

where H = normalized displacement (hub to tip) and $a_1, a_2, ...$



are determined by a polynomial regression curve fitting routine. The value of the total flow function at the centerline (Φ_{cL}) was evaluated for each case. Values of Φ/Φ_{cL} for each survey were then calculated and plotted against H. The resulting curves shown in Fig. C2 were then approximated by a family of polynomials having the form

$$\overline{\Phi} = \frac{\Phi}{\Phi_{cL}} = A_0 + A_1 H + A_2 H^2 \dots C(3)$$

which is then called the normalized flow function.

The referred flow rate is defined as

$$N^* = \frac{\omega \sqrt{\Theta}}{\delta'} C(4)$$

where

$$\Theta = \frac{T_{t_0}}{T_{ref}}$$
 C(5)

and

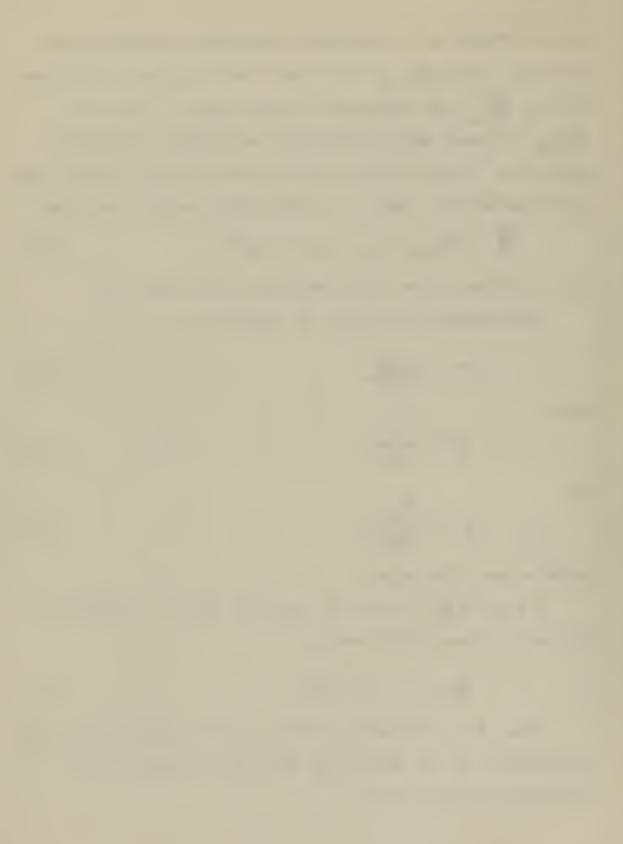
$$\int_{c}^{t} = \frac{P_{t_0}}{P_{ref}} \qquad C(6)$$

and $\dot{\omega}$ = mass flow rate.

A plot of $\overline{\Phi}_{CL}$ versus \dot{W}^* shown in Fig. C3 yielded the following linear relationship:

$$\overline{\Phi} c_{L} \neq b_{0} + b_{1} \dot{W}^{*} \qquad C(7)$$

Thus, Eq. C(3) and Eq. C(7) provide an analytical representation of the inlet flow profile in terms of the referred flow rate only.



C2. APPLICATION

For each run of the transonic compressor, \dot{W}^* is calculated and $\overline{\Phi}_{cL}$ is then evaluated from Eq. C(7). $\overline{\Phi}$ can then be evaluated from Eq. C(3).

X is then evaluated as the subsonic solution of the flow function given by Eq. C(1) using Newton's method as follows:

- 1) Guess $X = X_0$
- 2) Calculate

$$\Phi_2 = X (1 - X^2)^{1/(Y-1)}$$
 C(8)

$$\frac{d\Phi}{dX} = \Phi_2 \left[\frac{1}{X} - \frac{2}{(Y-1)} \left(\frac{X}{1-X^2} \right) \right] \qquad C(9)$$

$$X = X + \frac{\overline{\Phi_1} - \overline{\Phi_2}}{\frac{d\overline{\Phi}}{d\overline{X}}} C(10)$$

3) Now test for convergence of $\overline{\Phi}$.

If $|\Phi_2 - \Phi_1| < .00001$ then the calculation is complete. If this requirement is not satisfied then the new $\overline{\Phi}_2$ in Eq. C(8) is calculated using the new X in Eq. C(10).

4) Mach number is calculated using Eq. B(4).

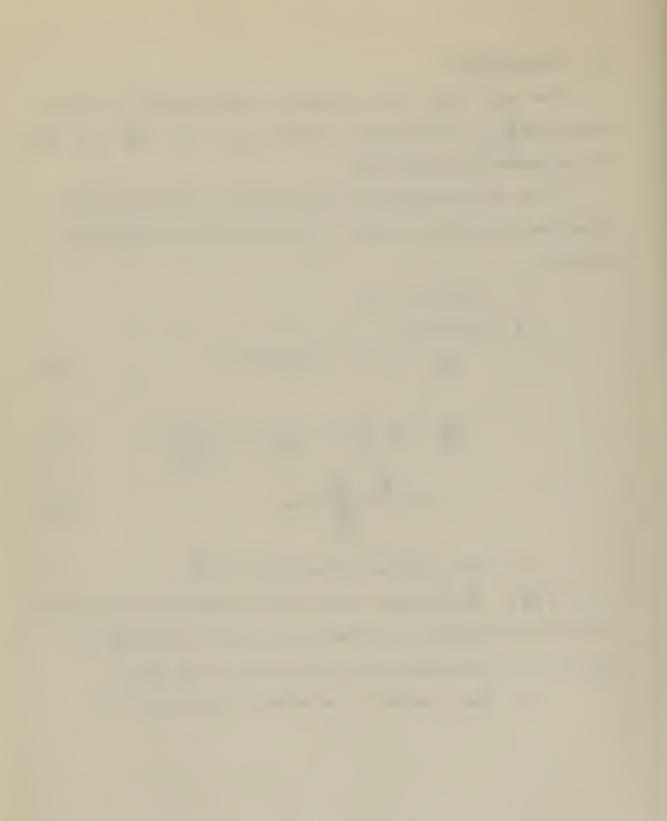
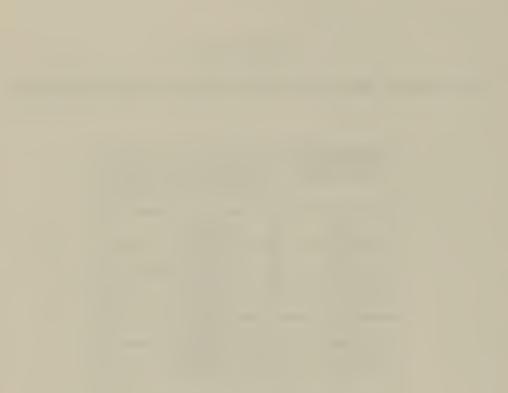
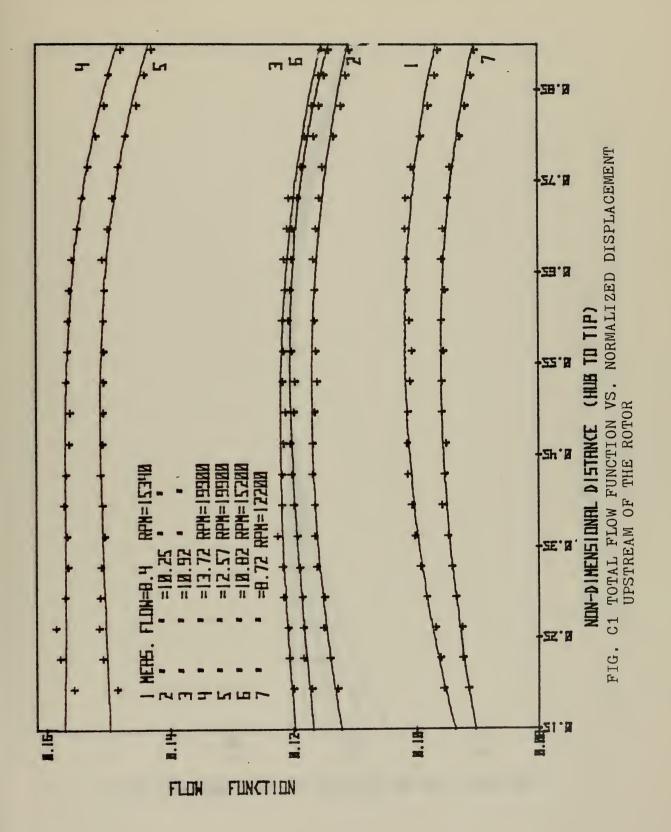


Table C1

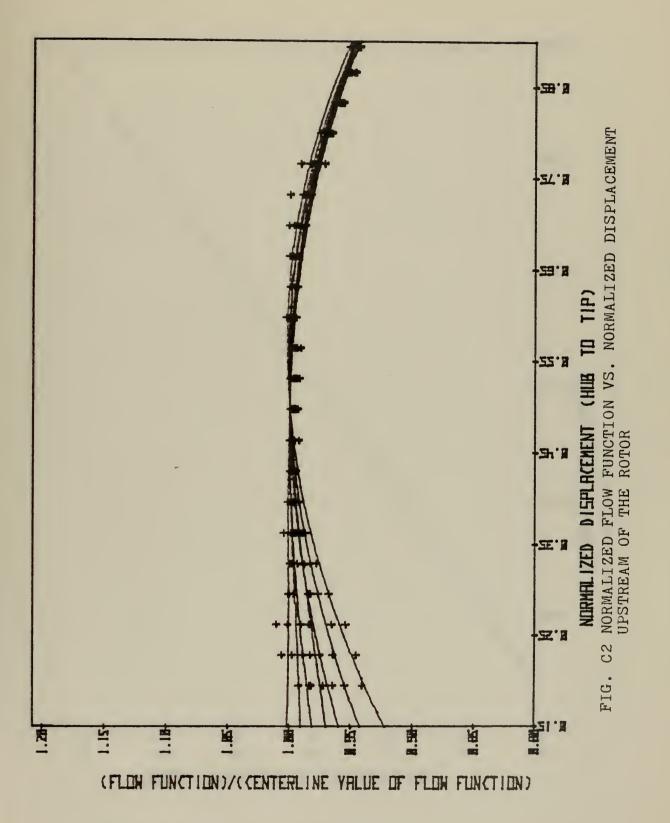
Flow Rates Used for Inlet Velocity Determination

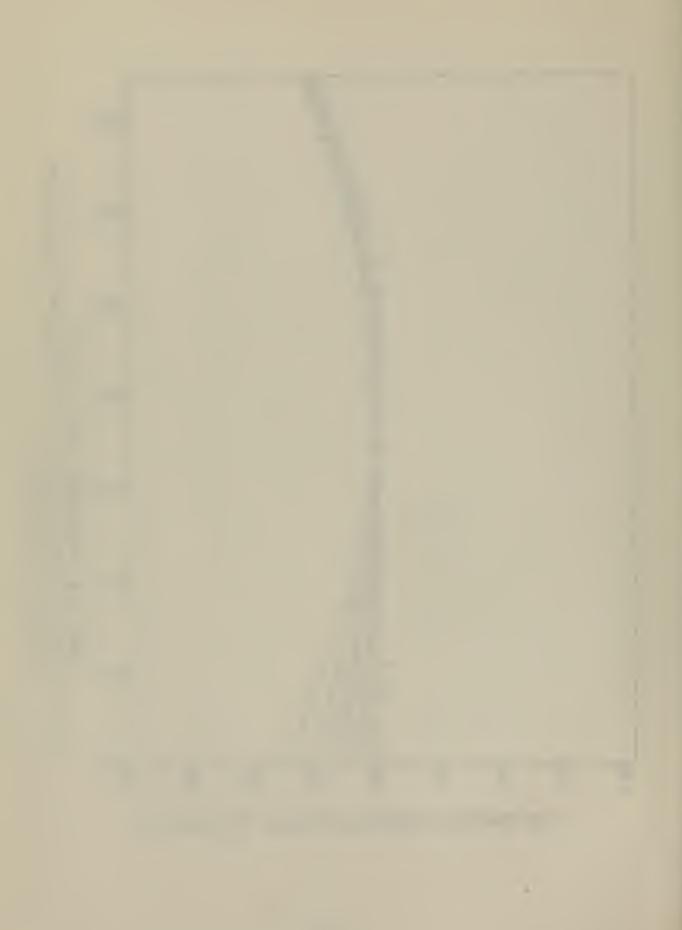
Referred Flow Rate	Centerline Value of Flow Function
8.95	.09589
9.38	.101607
10.89	.11693
11.18	.12039
11.42	.122025
13.83	.151239
14.30	.156789

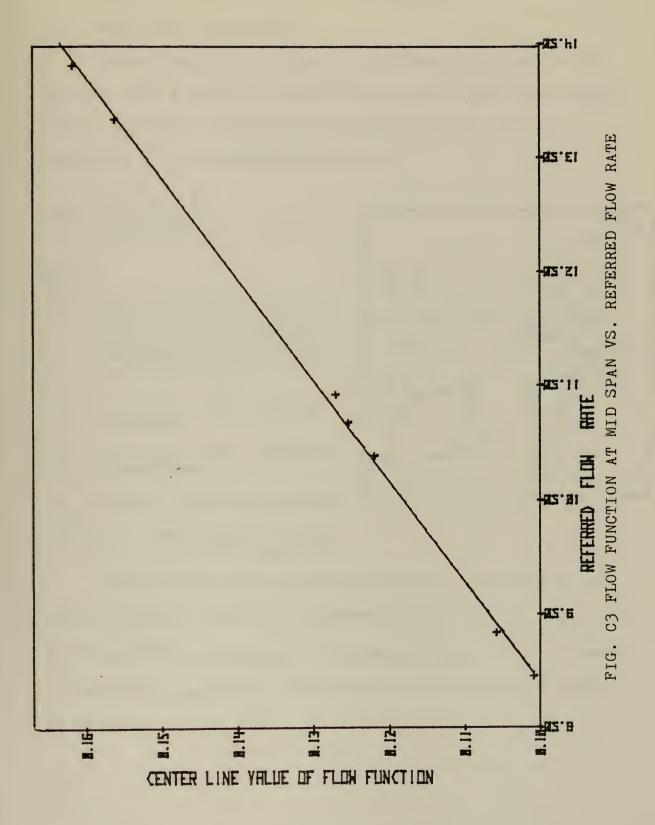


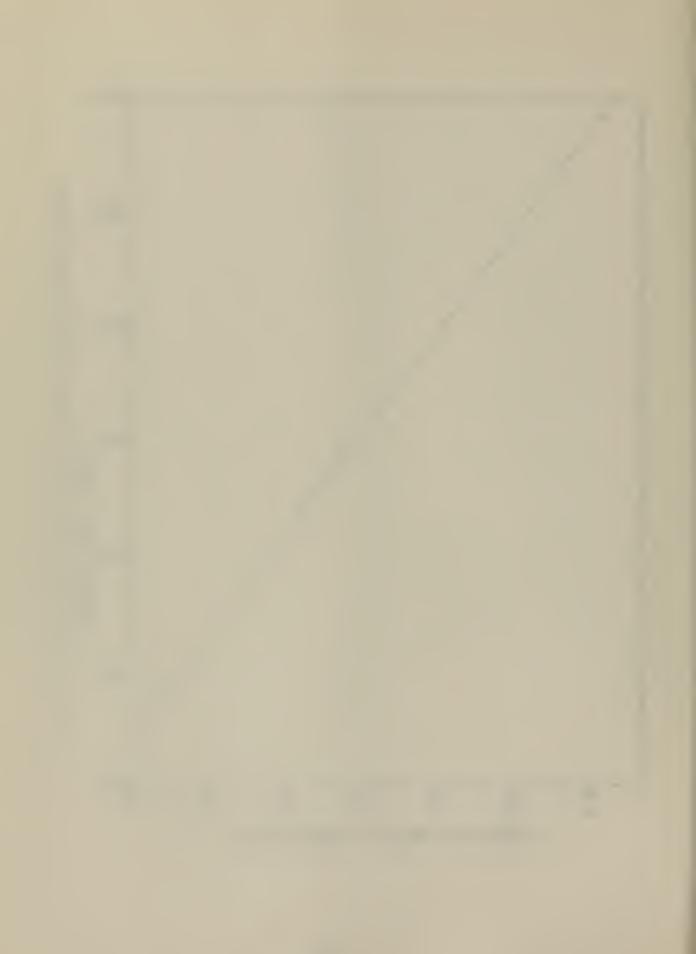












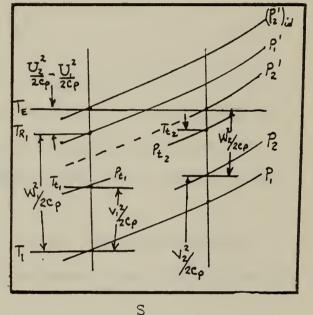
APPENDIX D: ROTOR LOSSES

D1. NASA LOSS COEFFICIENT

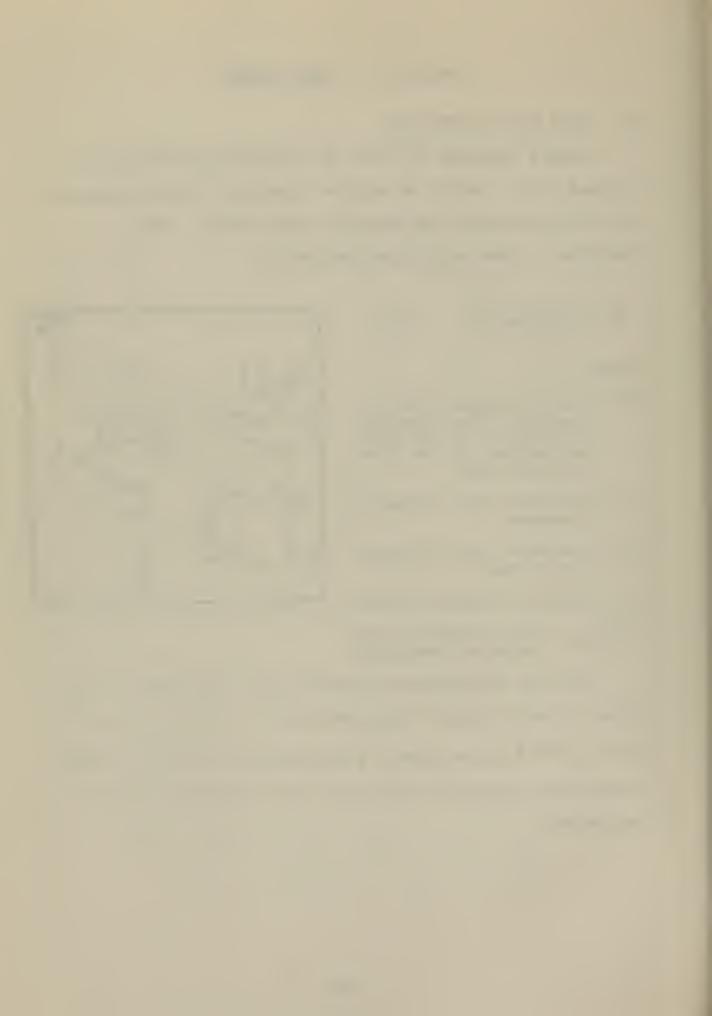
Losses incurred in flows in turbomachinery may be described with a varity of methods depending upon the measurements available and the specific application. Ref. 1 describes a loss coefficient defined by

$$\overline{\omega}' = \frac{(P_2')_{id} - P_2'}{P_1' - P_1} \qquad D(1)$$

where



From the measurements obtained and a knowledge of the inlet velocity profile the parameters P_1 , P_2 , P_{t1} , P_{t2} , X_1 , X_2 , T_{t1} , and T_{t2} are known. A representation of $\bar{\omega}'$ in terms of measured stagnation conditions and velocities (X or M) is desired.



D1.1 Upstream of the Rotor. The following relations may be written:

$$(P_2)_{id} = P_{t_1} \left(\frac{T_E}{T_{t_1}}\right)^{\frac{3}{2}} = P_{t_1} \left[1 - X_{U_2}^2\right]^{\frac{3}{2}} = D(2)$$

$$T_{E} = T_{1} + \frac{W_{1}^{2}}{2C_{P}} + \frac{U_{2}^{2} - U_{1}^{2}}{2C_{P}} D(3)$$

$$\frac{T_{\rm E}}{T_{\rm t_1}} = 1 - X_1^2 + X_{\rm W_1}^2 + X_{\rm U_2}^2 - X_{\rm U_1}^2 \qquad D(4)$$

where X is a velocity non-dimensionalized as in Eq. B(1), subscript denotes the relative velocity, and subscript W denotes the wheel speed. The other notation is given in the T-S diagram for the flow through the rotor shown in the above sketch.

Using the above equations, for an "impulse" machine for which there is a meridional entrance flow, the following relations result:

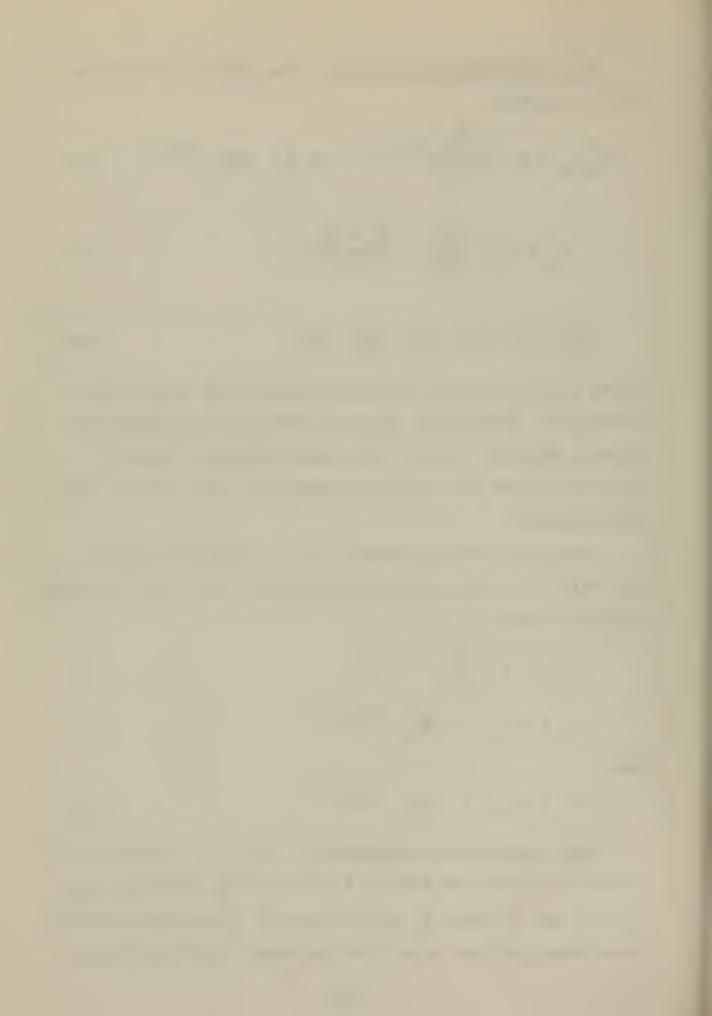
$$\frac{T_{\rm E}}{T_{\rm t1}} = 1 + X_{\rm U2}^2 \qquad D(5)$$

$$P_{1} = P_{t_{1}} \left(1 + X_{U_{1}}^{2} \right)^{\frac{3}{2}} (3-1)$$
 D(6)

and

$$P_{1} = P_{t_{1}} (1 - X_{1}^{2}) \frac{\delta}{(x-1)} D(7)$$

<u>D1.2 Downstream of the Rotor</u>. Sufficient measurements exist at the machine station 2 to derive \mathbb{P}_2 using \mathbb{T}_{t_2} , \mathbb{T}_{t_2} , $\overline{X}_2, \propto_2$, and \mathbb{U}_2 where \overline{X}_2 is the measured downstream velocity, non-dimensionalized using the downstream limiting velocity



 (V_{t_2}) in Eq. B(1). Alternatively, since T_E = constant for the flow through the rotor (see diagram), then one of the separate measurements is not needed. Two methods were therefore used. Method 1 used all measurements at station 2. Method 2 did not use the temperature rise at station 2, and thus served as a check on the accuracy of the temperature measurement.

(i) <u>Method I</u> (all measurements at station 2)

$$P_{2} = P_{t2} \left(\frac{T_{E}}{T_{t2}}\right) \frac{\sqrt[4]{(\gamma-1)}}{D(8)}$$

where $\frac{T_{E}}{T_{t_{2}}}$ is given by

$$\frac{T_{E}}{T_{t_{2}}} = 1 - X_{U_{2}}^{2} \left(\frac{T_{t_{1}}}{T_{t_{2}}}\right) - 2\bar{X}_{2} X_{U_{2}} \sqrt{\frac{T_{t_{1}}}{T_{t_{2}}}} \sin \alpha_{2} \qquad D(9)$$

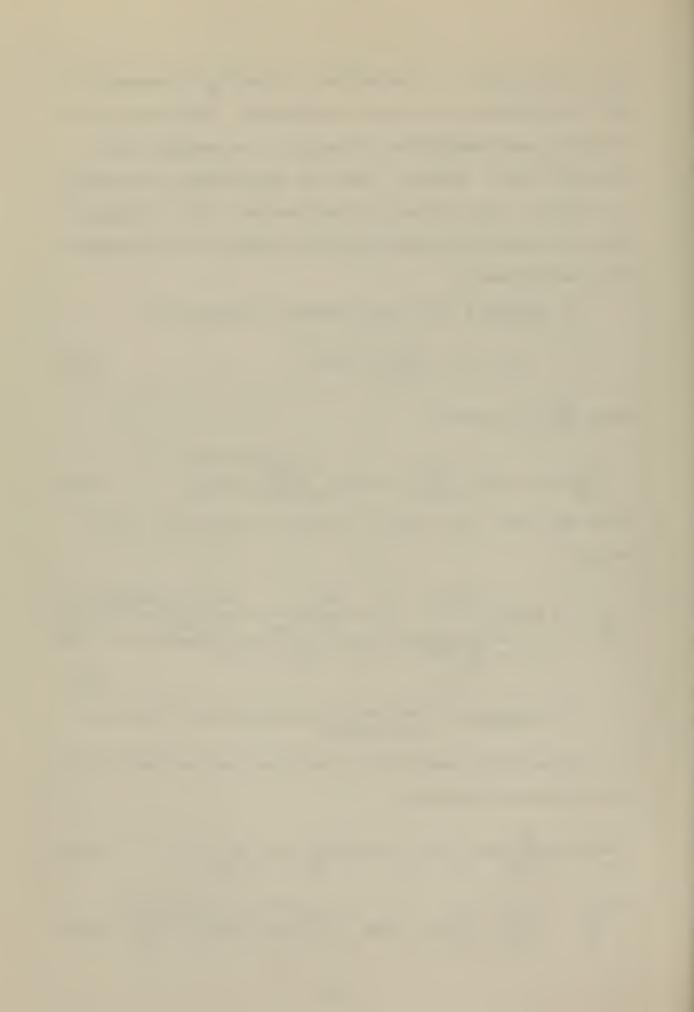
Using Eq. D(6), D(7), D(8), and D(9) in Eq. D(1), there results

$$\overline{\omega}' = \frac{\left[1 + X_{U_2}^2\right]^{\frac{1}{2}} \left[1 + X_{U_1}^2\right]^{\frac{1}{2}} - \left[1 + \frac{X_{U_2}^2}{(T_{t_1}/T_{t_2})} - \frac{2X_2X_{U_2}\sin\alpha_2}{T_{t_2}/T_{t_1}}\right]^{\frac{1}{2}} - \frac{1}{P_{t_2}}}{\left[1 + X_{U_1}^2\right]^{\frac{1}{2}} \left[1 - X_1^2\right]^{\frac{1}{2}} \left[1 - X_1^2\right]^{\frac{1}{2}}}$$

·(ii) <u>Method II</u> (Temperature measurement at station 2 not needed)

Temperature measurement downstream may be found using the following relation.

$$\frac{T_{E}}{T_{t_{2}}} = \left(\frac{T_{E}}{T_{t_{1}}}\right) / \left(T_{t_{2}}/T_{t_{1}}\right) = \left(1 + X_{U_{2}}^{2}\right) / \left(T_{t_{2}}/T_{t_{1}}\right) \qquad D(11)$$



Using Eq. D(6), D(7), D(11), and D(12) in Eq. D(1), the loss coefficient is given by

$$\bar{w}' = \frac{\left[1 + x_{U_2}^2\right]^{\frac{9}{7}(\frac{9}{4} - 1)} - \left[(1 + x_{U_2}^2)/\Psi^2\right]^{\frac{9}{7}(\frac{9}{4} - 1)} (\frac{P_{t_2}}{P_{t_1}})}{\left[1 + x_{U_1}^2\right]^{\frac{9}{7}(\frac{9}{4} - 1)} - \left[1 - x_1^2\right]^{\frac{9}{7}(\frac{9}{4} - 1)}} D(13)$$

D2.. DIFFUSION FACTOR

Ref. 1 reports results of correlating compressor losses in terms of the "diffusion factor". This approach results from the argument that the loss in stagnation pressure depends largely on the suction-surface adverse pressure gradient, of which the diffusion factor can be shown to be an approximate measure. The diffusion factor of Ref. 1 is defined by

$$D = 1 - \frac{W_2}{W_1} + \frac{R_1 W_{U_1} - R_2 W_{U_2}}{\sigma(R_1 + R_2) W_1} D(14)$$

In this form, changes in axial velocity and radius through the blade row are accounted for.

It is concluded in Ref. 1 that the total-pressure-loss parameter $(\varpi' \frac{\cos \theta}{2\sigma})$ can be correlated in terms of the above diffusion factor. Each family of blade shapes has a somewhat different correlation curve, however, this presents no real problem as the total number of shapes is limited. The correlation for several types of blading is shown in Fig. 203 of Ref. 1.



BIBLIOGRAPHY

2.5

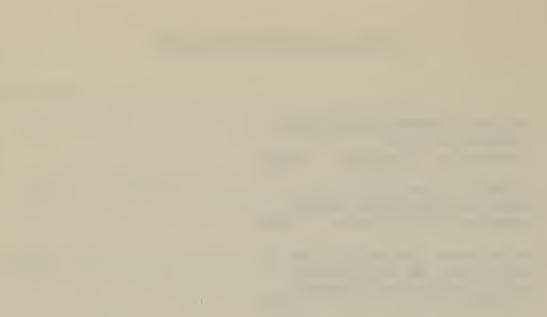
- National Aeronautics and Space Administration Special Report NASA SP-36, <u>Aerodynamic Design of Axial Flow</u> <u>Compressors (NASA SP-36)</u>, Edited by Irving A. Johnson and Robert O. Bullock, 1965
- 2. Naval Postgraduate School Thesis, <u>Development of a</u> <u>Temperature-Pneumatic Probe and Application at the</u> <u>Rotor Exit in A Transonic Compressor</u>, by F. J. Dødge, June 1976.
- 3. Naval Postgraduate School Thesis, <u>Velocity Measurements</u> <u>in a Transonic Compressor Using a Calibrated Pressure</u> <u>Probe</u>, by D. S. Anderson, March 1975.
- 4. Naval Postgraduate School Report NPS-57va72091A, <u>A De-</u> scription of the Turbopropulsion Laboratory in the <u>Aeronautics Department at the Naval Postgraduate</u> <u>School</u>, by M. H. Vavra and R. P. Shreeve, September 1973.
- 5. Naval Postgraduate School Thesis, <u>Microprogrammable Data</u> <u>Acquisition and Probe Control System (MIDAS IV) With</u> <u>Application to Compressor Testing</u>, by D. D. Patton, March 1976.
- Naval Postgraduate School Report NPS-57sf74081, <u>Flow</u> <u>Into a Transonic Compressor Rotor Part 1-Analysis</u>, by R. P. Shreeve, August 1974.
- 7. Bryer, D. W. and Pankhurst, R. C., <u>Pressure-Probe Methods</u> for Determining Wind Speed and Flow Direction, Her Majesty's Stationary Office, 1971.
- 8. North Atlantic Treaty Organization Advisory Group for Aerospace Research and Development Report AGARD-LS-83, <u>Modern Prediction Methods for Turbomachine Performance</u>, June 1976.
- 9. <u>Hewlett-Packard 9830A Calculator: Operating and Pro-</u> gramming Manual.
- 10. <u>Hewlett-Packard 9830A Calculator: 9830A/B Mass Memory</u> Operating Manual.
- Naval Postgraduate School Report NPS-57sf73072A, <u>Cali-bration of Flow Nozzles Using Traversing Pitot-Static Probes</u>, by R. P. Shreeve, July 1973.



INITIAL DISTRIBUTION LIST

.

		No. Copies
1.	Defense Documentation Center Cameron Station Alexandria, Virginia 22314	2
2.	Library, Code 0142 Naval Postgraduate School Monterey, California 93940	2
3.	Department Chairman, Code 67 Department of Aeronautics Naval Postgraduate School Monterey, California 93940	1
4.	Assoc. Professor R.P. Shreeve, Code 67Sf Department of Aeronautics Naval Postgraduate School Monterey, California 93940	1
5.	LT W.R. Hawkins 77 Truex Place Middletown, New Jersey 07748	1
6.	Mr. J.E. Hammer, Code 67 Department of Aeronautics Naval Postgrauate School Monterey, California 93940	1
7.	Turbo-Propulsion Laboratory, Code 67 Naval Postgraduate School Monterey, California 93940	8
8.	Mr. H.J. Mueller Code 310A, Naval Air Systems Command Navy Department Washington, D.C. 20360	1
9.	Mr. Karl H. Guttman Code 330C, Naval Air Systems Command Navy Department Washington D.C. 20360	1
LO.	Mr. Eric Lister R & T Division Naval Air Propulsion Test Center Trenton, New Jersey 08628	1



-

-

ъ

.

۰.

