



Calhoun: The NPS Institutional Archive
DSpace Repository

Theses and Dissertations

1. Thesis and Dissertation Collection, all items

1977-06

Wind tunnel wall corrections for arbitrary planforms and wind tunnel cross-sections.

Heard, Chester Arthur

Monterey, California. Naval Postgraduate School

<https://hdl.handle.net/10945/18328>

This publication is a work of the U.S. Government as defined in Title 17, United States Code, Section 101. Copyright protection is not available for this work in the United States.

Downloaded from NPS Archive: Calhoun



Calhoun is the Naval Postgraduate School's public access digital repository for research materials and institutional publications created by the NPS community. Calhoun is named for Professor of Mathematics Guy K. Calhoun, NPS's first appointed -- and published -- scholarly author.

Dudley Knox Library / Naval Postgraduate School
411 Dyer Road / 1 University Circle
Monterey, California USA 93943

<http://www.nps.edu/library>

WIND TUNNEL WALL CORRECTIONS FOR ARBITRARY
PLANFORMS AND WIND TUNNEL CROSS-SECTIONS

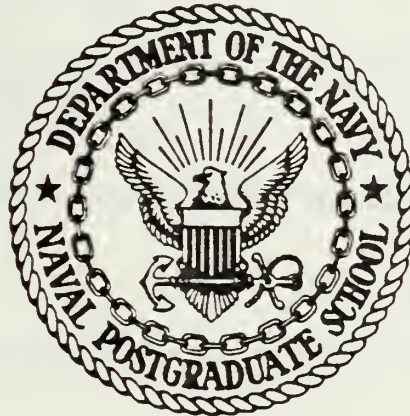
Chester Arthur Heard

BURLEY KNOX LIBRARY
NAVAL POSTGRADUATE SCHOOL

114

NAVAL POSTGRADUATE SCHOOL

Monterey, California



THESIS

WIND TUNNEL WALL CORRECTIONS FOR ARBITRARY
PLANFORMS AND WIND TUNNEL CROSS-SECTIONS

by

Chester Arthur Heard

June 1977

Thesis Advisor:

L.V. Schmidt

Approved for public release; distribution unlimited.

T178648

REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER	2. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER
4. TITLE (and Subtitle) Wind Tunnel Wall Corrections for Arbitrary Planforms and Wind Tunnel Cross-Sections		5. TYPE OF REPORT & PERIOD COVERED Master's Thesis; June 1977
		6. PERFORMING ORG. REPORT NUMBER
7. AUTHOR(s) Chester Arthur Heard		8. CONTRACT OR GRANT NUMBER(s)
9. PERFORMING ORGANIZATION NAME AND ADDRESS Naval Postgraduate School Monterey, California 93940		10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS
11. CONTROLLING OFFICE NAME AND ADDRESS Naval Postgraduate School Monterey, California 93940		12. REPORT DATE June 1977
		13. NUMBER OF PAGES 75
14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office)		15. SECURITY CLASS. (of this report) Unclassified
		15a. DECLASSIFICATION/DOWNGRADING SCHEDULE
16. DISTRIBUTION STATEMENT (of this Report) Approved for public release; distribution unlimited.		
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)		
18. SUPPLEMENTARY NOTES		
19. KEY WORDS (Continue on reverse side if necessary and identify by block number) Wind Tunnel Wall Corrections Vortex Lattice Method		
20. ABSTRACT (Continue on reverse side if necessary and identify by block number) A computer program was developed to obtain the wind tunnel wall corrections for wing angle of attack, induced drag, and pitching moment in incompressible flow. The vortex lattice method is used for computation of these correction		

(20. ABSTRACT Continued)

factors. The program can be applied to wind tunnels of arbitrary cross-sectional shape, and wings of any desired planform, subject to the constraint of straight leading and trailing edges.

Approved for public release; distribution unlimited.

Wind Tunnel Wall Corrections for Arbitrary
Planforms and Wind Tunnel Cross-Sections

by

Chester Arthur Heard
Lieutenant, United States Navy
B.A., Southwestern at Memphis, 1969

Submitted in partial fulfillment of the
requirements for the degree of

MASTER OF SCIENCE IN AERONAUTICAL ENGINEERING

from the

NAVAL POSTGRADUATE SCHOOL

June 1977

ABSTRACT

A computer program was developed to obtain the wind tunnel wall corrections for wing angle of attack, induced drag, and pitching moment in incompressible flow. The vortex lattice method is used for computation of these correction factors. The program can be applied to wind tunnels of arbitrary cross-sectional shape, and wings of any desired planform, subject to the constraint of straight leading and trailing edges.

TABLE OF CONTENTS

I.	INTRODUCTION -----	12
II.	METHODS USED -----	15
	A. GENERAL -----	15
	B. VORTEX LATTICE METHOD -----	17
	C. AIRFLOW REPRESENTATION -----	20
	D. DETERMINATION OF WALL CORRECTIONS -----	24
III.	RESULTS AND DISCUSSION -----	30
	A. THE COMPUTER PROGRAM -----	30
	B. GROUND EFFECT -----	31
	C. WIND TUNNEL APPLICATION -----	34
IV.	CONCLUSIONS AND RECOMMENDATIONS -----	43
	APPENDIX A: ASSUMPTIONS -----	44
	APPENDIX B: DEVELOPMENT OF INDUCED VELOCITY EQUATIONS -----	45
	APPENDIX C: COMPUTER PROGRAM INPUT -----	50
	COMPUTER PROGRAM -----	51
	LIST OF REFERENCES -----	74
	INITIAL DISTRIBUTION LIST -----	75

LIST OF FIGURES

1.	Wind Tunnel Geometry -----	18
2.	Wing Geometry -----	22
3.	Ground Effect Ratio Plotted as a Function of Wing Height Above the Ground -----	32
4.	Wing Span Load Distribution -----	35
5.	Induced Drag Distribution -----	39
6.	Angle of Attack Correction Factor Plotted as a Function of Span Ratio -----	40
7.	Angle of Attack Correction Factor Plotted as a Function of Sweep Angle -----	41
8.	Velocity Induced by a Vortex Segment -----	46

LIST OF TABLES

1.	Ground Effect Factor Variation With Sweep Angle -----	33
2.	Wing Parameter Variation with Span -----	36
3.	Wing Parameter Variation with Sweep Angle -----	37

LIST OF SYMBOLS

[AERO]	Wing aerodynamic influence coefficient matrix at the 0.75 chord position
AR	Wing aspect ratio = b^2/S
b	Wing Span
C	Wind tunnel cross-sectional area
c	Local wing chord, streamwise direction
c_{ave}	Average wing chord, (s/b)
c_l^c	Wing span loading, (ℓ/q)
C_L	Wing lift coefficient = Lift/ qS , dimensionless
$C_{L_{\alpha_g}} / C_{L_{\alpha_{Fa}}}$	Ground effect ratio
C_m	Pitching moment coefficient = Moment/ $qS\bar{c}$
C_R	Root chord
C_T	Tip chord
C_{D_i}	Wing induced drag coefficient
C_d^c	Spanwise induced drag distribution (d/q)
d	Wing induced drag distribution, drag/unit span
[DAERO]	Wing aerodynamic influence coefficient matrix at the wing quarter-chord
[GAMAL]	Wall vortex loop strength
h	Wing height above the ground
H	Wind tunnel height
ℓ	Wing running span load, lift/unit span
NS	Number of horseshoe vortices per semispan
q	Dynamic pressure

[ROL]	Wall aerodynamic influence coefficient matrix
[ROT]	Influence coefficient matrix for wall-on-tail
[ROW]	Influence coefficient matrix for wall on wing
S	Wing area
TR	Wing tape ratio, C_T/C_R
V	Freestream velocity
w	Induced downwash velocity
W	Wind tunnel width
$(\frac{W}{V})_{3c/4}$	Induced downwash angle at 0.75 chord position
[WOL]	Influence coefficient matrix for wing-on-wall
[WOT]	Influence coefficient matrix for wing-on-tail
X	Axial coordinate
Y	Vertical coordinate
Z	Spanwise coordinate
α	Angle of attack
δ	Wind tunnel wall interference factor
Γ	Vortex strength
ϵ	Induced downwash angle at the tail
η	Wing spanwise stations ($\frac{2z}{b}$)
η_{TL}	Tail efficiency factor

Subscripts:

FA	free air
g	ground
l	wall vortex loops
T	wind tunnel

TL tail
w wing
 $()_\alpha$ $\partial()/\partial\alpha$

Matrix Notation:

[] Rectangular matrix
{ } Column matrix
⌈ ⌋ Diagonal matrix
[]⁻¹ Inverse of a square matrix

ACKNOWLEDGMENT

My sincere gratitude goes to Professor L. V. Schmidt for his invaluable assistance throughout the course of this work and to my wife Anne for her patience and understanding.

I. INTRODUCTION

In the process of wind-tunnel testing the experimental procedure itself constrains and alters the flow past the wing under examination. This modified flow induces errors which must be corrected if accurate results are to be obtained. The major interference effects in subsonic wind tunnels result from the constraining influence of wind tunnel walls, disturbances from model supports and measuring equipment, and turbulence and non-uniformity in the airflow itself.

Russell [Ref. 10] treats the problems resulting from model support interference and introduces a method for reduction of this effect. The differential equations governing flow within a wind tunnel are the same as those in free air. However, the presence of the wind tunnel walls changes the outer boundary conditions. The result is a series of perturbations of the velocity-potential gradient normal to the model surface. The effect is pervasive in that almost all of the measured aerodynamic quantities must be corrected.

Generally, Prandtl is acknowledged as having established the foundations for research on wind-tunnel wall interference. His lifting-line theory and concept of trailing vortices opened the doors to much experimental investigation in this area. The resulting studies considered two-dimensional

and three-dimensional effects, open and closed wind tunnels, and various geometrically shaped test sections.

References 1 and 8 offer a comprehensive treatment of wind-tunnel wall interferences. Much tabular and graphical data are presented for different tunnel shapes and wing spans. Pankhurst and Holder included much data on octagonal wind tunnels, while Pope concentrated more on a uniformly loaded wing.

With the advent of sweptback, slender wings designed for high-speed flight, the lifting line model was no longer suitable. In these situations, the wing lifting system may be represented by distributed horseshoe vortex elements [Refs. 6 and 7]. In Ref. 9, data, graphs, and formulas are assembled from various sources and systematically analyzed for various types of wings in wind tunnels. Although the mathematical formulations are tedious, the resulting graphs and tables summarized very well the data obtained from each theoretical treatment.

Even with all this information available, it is still an arduous task to approach tabulated data with a specific wind tunnel shape and geometric configuration, and hope for a solution to the wall interference problem. It is the purpose of this paper to develop a computerized, closed-form solution to this problem. The design goal was to develop a digital computer code that would be applicable to wind tunnels of arbitrary cross-section and wings with

varying planforms. Such versatility would enhance the accuracy of test data and provide a valuable, accurate tool in wind-tunnel testing.

II. METHODS USED

A. GENERAL

Wind tunnels provide an invaluable tool in the design and performance prediction of wings and wings-and-bodies. However, the wind-tunnel testing environment introduces its own set of problems. The interference action from the walls of the wind tunnel alters the development of induced velocities by the wing lifting system. As a result, downwash formation is suppressed and the wing aerodynamic characteristics are those of a wing having greater aspect ratio. The accurate determination of wind tunnel wall interference is, therefore, an important consideration in wing experiments.

The classical wall correction factor, δ , for the case of a single horseshoe vortex representing the complete wing is defined by:

$$\Delta\alpha = \delta \frac{S}{c} C_L \quad (1)$$

where

$$\Delta\alpha = \tan^{-1} \frac{w}{V}$$

Using small angle approximations, the tangent is approximately equal to the angle. The wall-correction factor may be expressed in terms of wing circulation, vortex span and average induced downwash velocity by:

$$\delta = \frac{w}{2b} \frac{c}{\Gamma_w} \quad (2)$$

Calculation of δ is dependent on the determination of the downwash velocity induced by the wind tunnel walls. Classical methods involve the utilization of an image system of vortices which cancel the effect of the wing lifting system at the wall. The boundary condition of no flow through the wall is, therefore, preserved. This system can provide an accurate, closed-form solution to the ground effect problem. However, when four walls are present, each wall must be represented by an image system which affects other image systems, as well as the model itself. The result is a series of infinite systems. Truncation of this system introduces inaccuracies of unknown magnitude and significance.

This method of images has been applied to tunnels of rectangular cross-section with success. However, it is inadequate when arbitrary tunnel cross-sections are encountered. Add to this a wing with sweep and taper, and the problem becomes significantly altered.

Therefore, a new method was sought to solve this problem specifically for the NPS 3.5 X 5 ft. octagonal wind tunnel. The technique chosen was presented by Joppa in Refs. 4 and 5. This approach lends itself very well to computer solution and can be applied to wind tunnels of any cross-sectional shape.

In this study, an extension of Joppa's vortex lattice method was made to allow the treatment of wings with varying shape, sweep, and aspect ratio. Such treatment requires a modification of the single horseshoe vortex representation of the wing lifting system. The method of Weissinger as presented in Ref. 6 provides an accurate means of representing variable planforms.

B. VORTEX LATTICE METHOD

Since the method of images was considered to be limited in application, it was necessary to find another, more versatile method of representing the wind-tunnel walls. The problem is essentially one of finding a vorticity distribution which will accurately model the wind-tunnel walls. This vortex system must satisfy the boundary condition of no flow through the walls.

In Ref. 4, Joppa presents a method which accurately models the wind-tunnel walls. This was accomplished by representing the tunnel walls with a lattice network of rectangular vortex loops. This vortex system lies in the plane of the tunnel walls and satisfies Helmholtz's theorem that a vortex filament can neither begin nor end in the flow. Fig. 1 shows a representation of this system as applied to the NPS 3.5 by 5 ft. wind tunnel.

Each vortex segment in a given rectangle has vortex strength Γ_i , and has a corresponding control point located

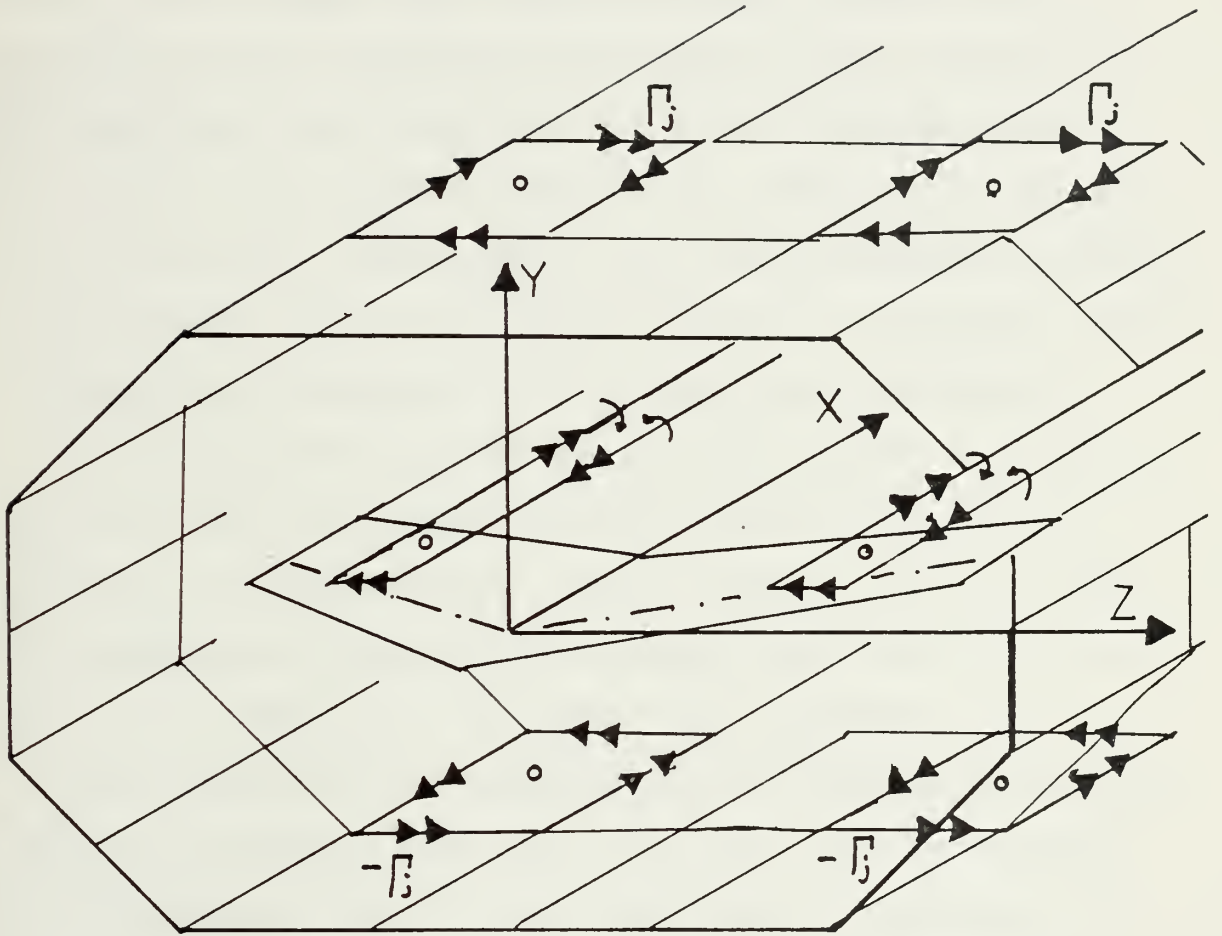


Figure 1. Wind Tunnel Geometry

in the center of each rectangle where the no-flow boundary condition is satisfied. The last vortex lattice rectangles located far downstream are represented by horseshoe vortices trailing to infinity. The reasoning is that far downstream, where the influence upon the wall vortex lattice array of the bound vortex elements on the wing is small relative to the trailing vortex elements, one finds that the vortex strengths of the lattice terms do not change in the stream-wise direction. Consequently, by a straightforward cancellation argument, one can visualize replacing the vortex lattice rectangles by horseshoe vortices trailing to infinity.

The mathematical presentation of the theory is based on the Biot-Savart law describing the velocity induced at a point by a vortex segment. Joppa in Refs. 4 and 5 follows the mathematical formulation beginning with the Biot-Savart law. This development is summarized in Appendix B.

The general matrix representation of this method centers around the boundary condition of no flow through the wall. As mentioned previously, this condition is satisfied at a control point located at the center of each vortex loop. Therefore, it follows that the velocity induced at each control point by the vortex loops must be exactly cancelled by the velocity created by the wing lifting system. This is presented below in matrix representation

$$[\text{ROL}] \{ \Gamma_L \} = [\text{WOL}] \{ \Gamma_w \} \quad (3)$$

which allows a solution of vortex lattice strengths in terms of the wing vortex strengths.

$$\{\Gamma_L\} = [ROL]^{-1} [WOL] \{\Gamma_w\} \quad (4)$$

Note that the [ROL] matrix, although possibly quite large, is square and hence may be inverted.

[ROL] represents the wall influence coefficient matrix. It is obtained by calculating the downwash induced at each wall control point by a unit value of each vortex loop. Therefore, ROL_{ij} is the downwash at wall control point "i" induced by vortex loop "j". [WOL] is the influence coefficient matrix describing the wing effect on each loop control point. WOL_{ij} is the downwash produced at control point "i" by the j^{th} wing horseshoe vortex.

By inverting [ROL] and premultiplying with [WOL], the strength of the wall vortex loops can be found in terms of the wing circulation. The inversion of [ROL] can be very time-consuming, since it may be a very large matrix. However, by using symmetry, the order of this matrix can be reduced by a factor of four. This requires the wing to be placed on the horizontal and vertical centerline of the wind tunnel.

C. AIRFOIL REPRESENTATION

In Ref. 5, Joppa stated that the wing can be represented by a lifting system more complicated than a single

elementary horseshoe vortex. In order to model swept wings of arbitrary planform, a more definitive lifting system model was employed. Gray and Schenk, Ref. 6, present a modified Weissinger method designed to find the load distribution of wings with arbitrary planform. The wing is represented by a series of horseshoe vortices. The midspan of each horseshoe vortex bound element is located at the wing quarter-chord position. The condition of flow tangency is satisfied at the wing three-quarter-chord point in the center of each horseshoe vortex. Figure 2 illustrates the configuration chosen.

Pearson [Ref. 7] modified this technique by allowing the bound vortices to be swept, and including chord-wise horseshoe vortices. For this presentation it was felt that unswept bound vortices would accurately represent the lifting system of a swept wing. In addition it was felt that little deterioration of accuracy would result if the chordwise system of bound vortices was combined into a single bound vortex at the quarter-chord. Figure 2 illustrates the configuration chosen.

An important concept in this representation of the wing is that of flow tangency at the three quarter-chord. The downwash angle at the wing can, therefore, be determined by placing a control point at this position in the center of each horseshoe vortex. The rationale behind the three-quarter chord flow tangency condition is a product of

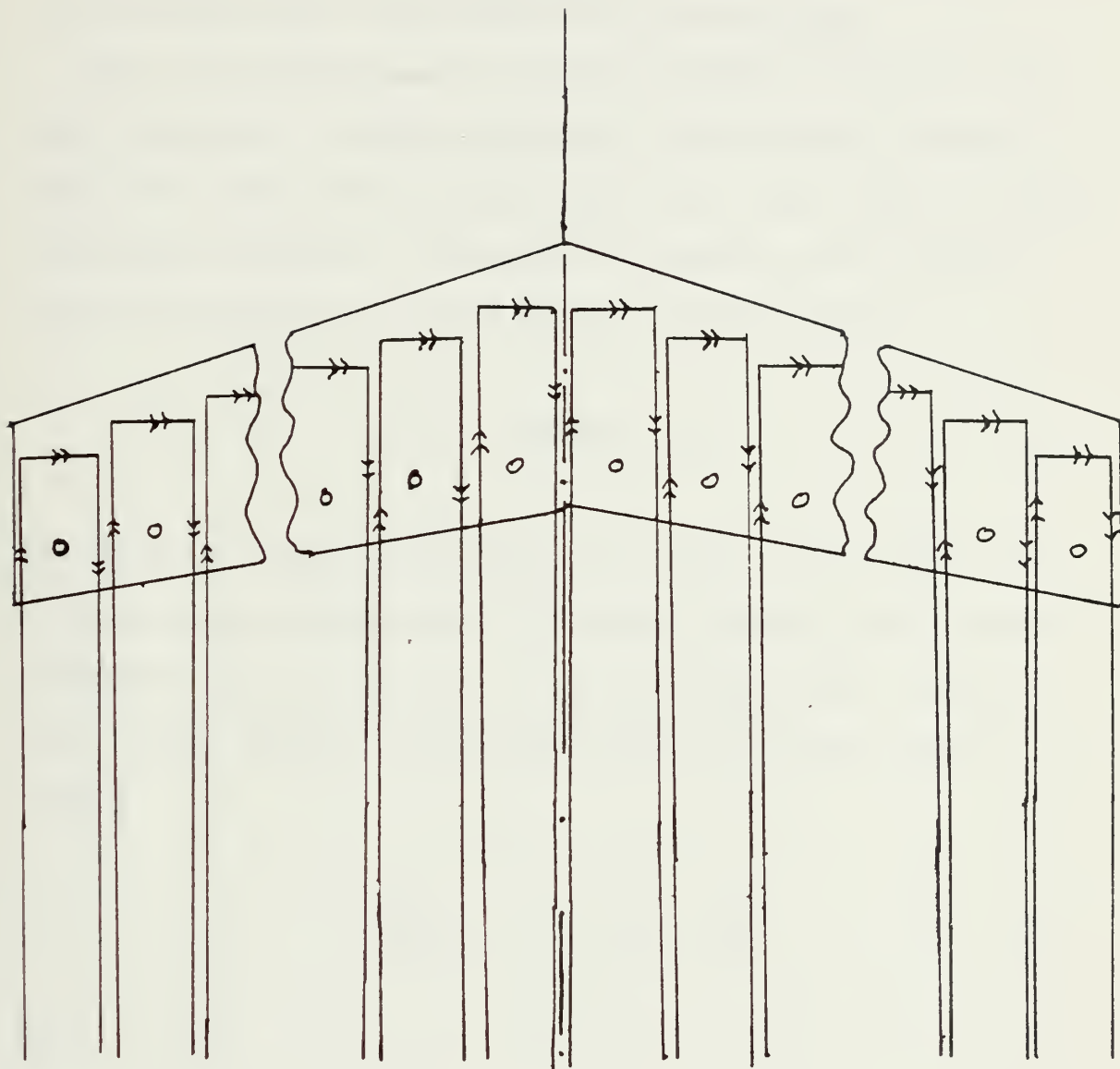


Figure 2. Wing Geometry

two-dimensional flow considerations. Extension of this technique to the three-dimensional wing has been shown to produce experimentally confirmed results. However, it is still unclear why this technique works so well.

The wing aerodynamic influence coefficient matrix was then developed. [AERO] represents the downwash induced at each 0.75 chord wing control point by a unit value of wing horseshoe vortices. The matrix formulation for induced downwash formation in free air is presented below:

$$\{w\} = [AERO] \{\Gamma_w\} \quad (5)$$

Dividing the above expression by freestream velocity, one obtains an expression for 0.75 chord control point induced downwash angles. The flow tangency requirement equates this column matrix to the wing angle of attack column vector.

$$\left\{ \frac{w}{V} \right\}_{3c/4} = [AERO] \left\{ \frac{\Gamma}{V} \right\} \quad (6)$$

and

$$\{\alpha\} = \left\{ \frac{w}{V} \right\}_{3c/4}$$

It should be noted here that $\frac{\ell}{q}$ is equal to $\frac{2\Gamma}{V}$, from the Kutta-Joukowski Law. Substitution into equation 6 yields the following results:

$$\left\{ \frac{w}{V} \right\} = 0.5 \text{ [AERO] } \left\{ \frac{\ell}{q} \right\}_{FA} \frac{3c}{4} \quad (7)$$

Solving equation 7 for $\left\{ \frac{\ell}{q} \right\}$, one can obtain the wing span load distribution. Since $\frac{\ell}{q}$ is equivalent to the sectional value of $C_{\ell}c$, integration of the $\frac{\ell}{q}$ distribution vs. span provides a direct measure of the wing lift coefficient, C_L . When one assumes a uniform angle of attack value of one radian along the span, the resultant integration of the span load solution will yield the wing lift curve slope, $C_{L\alpha}$. It should be borne in mind that these techniques are predicated upon principles from thin airfoil theory and in the limit for an infinite aspect ratio wing will yield a wing lift curve slope of $2\pi(\text{rad}^{-1})$.

D. DETERMINATION OF THE WALL CORRECTIONS

The classical wall interference factor δ , which includes a ratio of wing to tunnel cross-section area, is generally found by representing the wing as a single horseshoe vortex. Since the present formulation utilizes ten horseshoe vortices per semi-span, δ in a modification can best be found by continuing our matrix algebra.

$$\alpha_{FA} = \alpha_T + \delta C_L$$

$$\alpha_{FA} = \frac{C_L}{C_{L\alpha_{FA}}} \quad (8)$$

$$\alpha_T = \frac{C_L}{C_{L\alpha_T}}$$

By assuming that the lift coefficient is the same in both tunnel and free air, the following equations result:

$$\frac{C_L}{C_{L\alpha_{FA}}} = \frac{C_L}{C_{L\alpha_T}} + \delta C_L \quad (9)$$

Cancelling the lift coefficient and solving for δ :

$$\delta = \frac{1}{C_{L\alpha_{FA}}} - \frac{1}{C_{L\alpha_T}} \quad (10)$$

The free air lift slope was found in the previous section. The wing lift curve slope for the wing in the wind tunnel can be found by a simple extension of this same method. The total downwash at the wing control points is equal to that induced by the wing added to that created by the tunnel walls. The effect produced by the tunnel walls is represented by the vortex rectangle-on-wing influence coefficient matrix [ROW]. ROW_{ij} is the downwash induced at the i^{th} wing control point by the j^{th} wall vortex loop. Multiplying this matrix by the vortex loop strength, one obtains the total wall effect.

$$\{w\} = [AERO] \{\Gamma_w\} + [ROW] \{\Gamma_L\} \quad (11)$$

Substitution of equation 4 for $\{\Gamma_L\}$ forms the following set of equations:

$$\{w\} = [AERO] \{\Gamma_w\} + [ROW] [ROL]^{-1} [WOL] \{\Gamma_w\}$$

$$\left\{ \frac{w}{V} \right\} = 0.5 \left[[AERO] + [ROW] [ROL]^{-1} [WOL] \right] \left\{ \frac{\ell}{q} \right\}_T \quad (12)$$

By establishing one radian angle of attack, solving for $\frac{\ell}{q}$, and integrating the result, the wind-tunnel lift curve slope can be determined. It should be noted that the correction factor obtained from this process is different from the classical δ , since the correction factor computed above already contains the wing area to tunnel area ratio influence. Therefore, the correction to angle of attack can be obtained by a direct application of this δ .

$$\Delta\alpha = \delta C_L \quad (13)$$

In most literature, the correction for induced drag is obtained by application of the same δ as that used for angle of attack.

$$\Delta C_{D_i} = \delta C_L^2 \quad (14)$$

However, in this presentation, the induced drag correction is calculated in a different manner because of added available aerodynamic information. The spanwise induced drag distribution in free air is given by the following formula:

$$\left\{ \frac{d}{q} \right\}_{FA} = \left[\frac{\ell}{q} \right]_{FA} [DAERO] \left\{ \frac{\ell}{q} \right\}_{FA} \quad (15)$$

[DAERO] is the wing aerodynamic influence coefficient matrix computed with the wing control point now located at the quarter-chord position. The wall effect can similarly be found by including additional matrix terms for the wall effect on the wing quarter-chord position.

$$\left\{ \frac{d}{q} \right\}_T = \left[\frac{\ell}{q} \right]_T \left[[DAERO] + [ROW] [ROL]^{-1} [WOL] \right] \left\{ \frac{\ell}{q} \right\}_T \quad (16)$$

Integration of equations 15 and 16 result in the free air and wind tunnel induced drag, respectively. The induced drag correction factor can then be found in the following manner.

$$C_{D_{i_{FA}}} = K_{FA} C_{L_{FA}}^2$$

$$C_{D_{i_T}} = K_T C_{L_T}^2$$

$$\begin{aligned}
K_{FA} &= C_{Di_{FA}} / C_{L_{FA}}^2 \\
K_T &= C_{Di_T} / C_{L_T}^2 \\
K &= K_{FA} - K_T \\
\Delta C_{Di} &= K C_{L_T}^2
\end{aligned}
\tag{17}$$

When testing a model in the tail-on configuration, the presence of the wind tunnel walls serves to modify the downwash angle induced at the tail. This altered flow field can have a significant effect on the pitching moment coefficient. The following increment in pitching moment coefficient is generated by the horizontal tail:

$$\Delta C_{m_{TL}} = \left(\eta_{TL} \frac{S_T \ell_{TL}}{S_w c} C_{L_{\alpha_{TL}}} \right) \alpha_{TL}
\tag{18}$$

The term in parentheses is approximately equal to the stabilizer effectiveness, $\frac{\partial C_m}{\partial \delta_i}$. The tail angle of attack can be estimated as follows:

$$\alpha_{TL} = \alpha - \varepsilon + \delta_i
\tag{19}$$

At a given value of wing lift coefficient an incremental change in downwash angle at the tail due to the wall effect can be computed:

$$\Delta\varepsilon = \varepsilon_T - \varepsilon_{FA} \quad (20)$$

Therefore, the correction to pitching moment coefficient is given by the following relation:

$$\Delta C_m = C_{mi} \Delta\varepsilon \quad (21)$$

Since the downwash angle ε is equal to $\frac{w}{V}$ at the tail position, ε for free air and for the wind tunnel can be found from the following relations, respectively:

$$\varepsilon_{FA} = 0.5 [WOT] \left\{ \frac{l}{q} \right\}_{FA}$$

$$\varepsilon_T = 0.5 [[WOT] + [ROT][GAMAL]] \left\{ \frac{l}{q} \right\}_T \quad (22)$$

[WOT] is the wing effect on the tail position and [ROT][GAMAL] represents the wall effect on the tail. Equation 20 can then be used to find $\Delta\varepsilon$. The pitching moment correction, as evaluated in equation 21, is thus dependent on being given an experimental value for the tail effectiveness parameter.

III. RESULTS AND DISCUSSION

A. COMPUTER PROGRAM

The computer program developed consists of two major subroutines. Subroutine Loop calculates the downwash at any point due to a vortex rectangle. Subroutine HSHOE computes the downwash at any arbitrary point due to a horseshoe vortex. HSHOE is used for both the wing horseshoe and those of the wall system located far downstream in the tunnel walls. The program offers two basic options. One option establishes whether ground effect or wind-tunnel wall corrections are to be calculated. The other option indicates whether the tail-on or tail-off case is to be considered.

Each computer run offers the inclusion of many wings of different span, aspect ratio, taper ratio, and sweep. The wing parameters are read as input data after the inversion of the large wall-on-wall coefficient matrix. Therefore, with a given tunnel configuration, a variety of different wings can be included with a minimum of computer time consumed.

Integration of the wing span loads is accomplished by a subroutine obtained from the NPS source library. It should be noted that in the integration scheme the assumption is made that the wing loading at $\eta = 0.0$ is the same as that for $\eta = .05b$. Any inaccuracy resulting from this assumption

appears to be negligible. Appendix C describes the necessary input to the program.

B. GROUND EFFECT

Originally, ground effect calculations were conducted merely to check the accuracy of the vortex lattice method. As previously stated, the method of images provides a closed-form solution to the ground effect problem. Therefore, this provided an excellent opportunity for a convergence check. As an object of academic interest an option for ground effect computation was retained in the final computer program.

The results of the convergence check showed that the vortex lattice method could very accurately compute the velocity induced at a point by the presence of a wall. By applying the theory previously developed, the lift curve slopes for free air and ground effect were computed. Results were then compared with those presented in Etkin [Ref. 3]. The free air lift curve slope was found to correlate extremely well for both straight and sweptback wings.

Furthermore, in Ref. 3, Etkin defines a ground effect ratio as the ground effect lift curve slope divided by that in free air. The results are tabulated in Table 1, and Figure 3 compares the results obtained from the computer program with those presented in Etkin. As can be seen, agreement is very favorable.

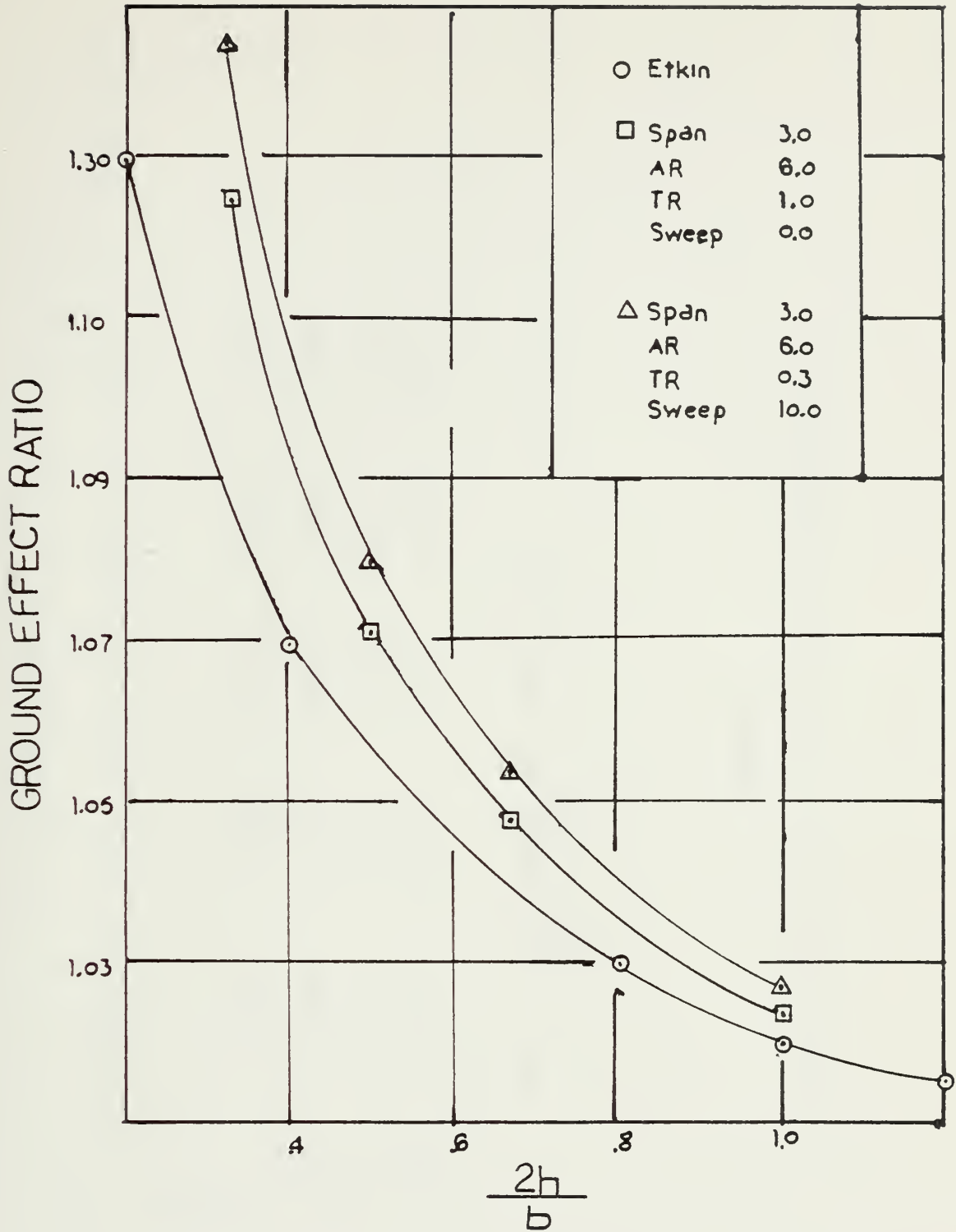


Figure 3. Ground Effect Ratio Plotted as a Function of Wing Height Above the Ground

0.25 Chord Sweep Angle, deg

	0.0	10	20	30	40
$\frac{2h}{b}$					
1.0	1.0248	1.0266	1.0259	1.0244	1.022
.667	1.0488	1.0541	1.0521	1.0481	1.0426
.50	1.072	1.080	1.079	1.073	1.065
.333	1.126	1.145	1.139	1.125	1.01

Note: Values apply to a wing with

AR = 6.0

TR = 0.3

Table 1

Ground Effect Factor Variation with Sweep Angle

Several computer runs were conducted at different wing heights above the ground. For each run, sweep was varied from 0 to 40 degrees. Results are tabulated in Figure 4. It can be noted that the ground effect ratio initially increases with sweepback but returns to the unswept value at about 30 degrees.

As a note of caution, care should be exercised when the wing gets very close to the ground. It is necessary to greatly decrease the vortex loop size for accurate results. This procedure seems to provide a much more finely defined ground representation. Otherwise, calculations will result in inordinately high values.

C. WIND TUNNEL APPLICATION

A convergence check of the wind tunnel wall correction factor was obtained by applying the program to a 3 X 5 ft rectangular tunnel. The correction factor obtained was converted to the classical δ by including the factors $\frac{S}{C}$ and 57.3 (radians to degrees). The result of 0.1216 was compared to that presented by Joppa in Ref. 5. The wing geometric configuration presented in Ref. 5 consisted of a single horseshoe vortex. The value of 0.127 from Ref. 5 correlates very well with the results of this study.

Tables 2 and 3 present the data obtained from computations with the NPS 3.5 X 5.0 ft octagonal wind tunnel. Computer runs were conducted using wings of varying span

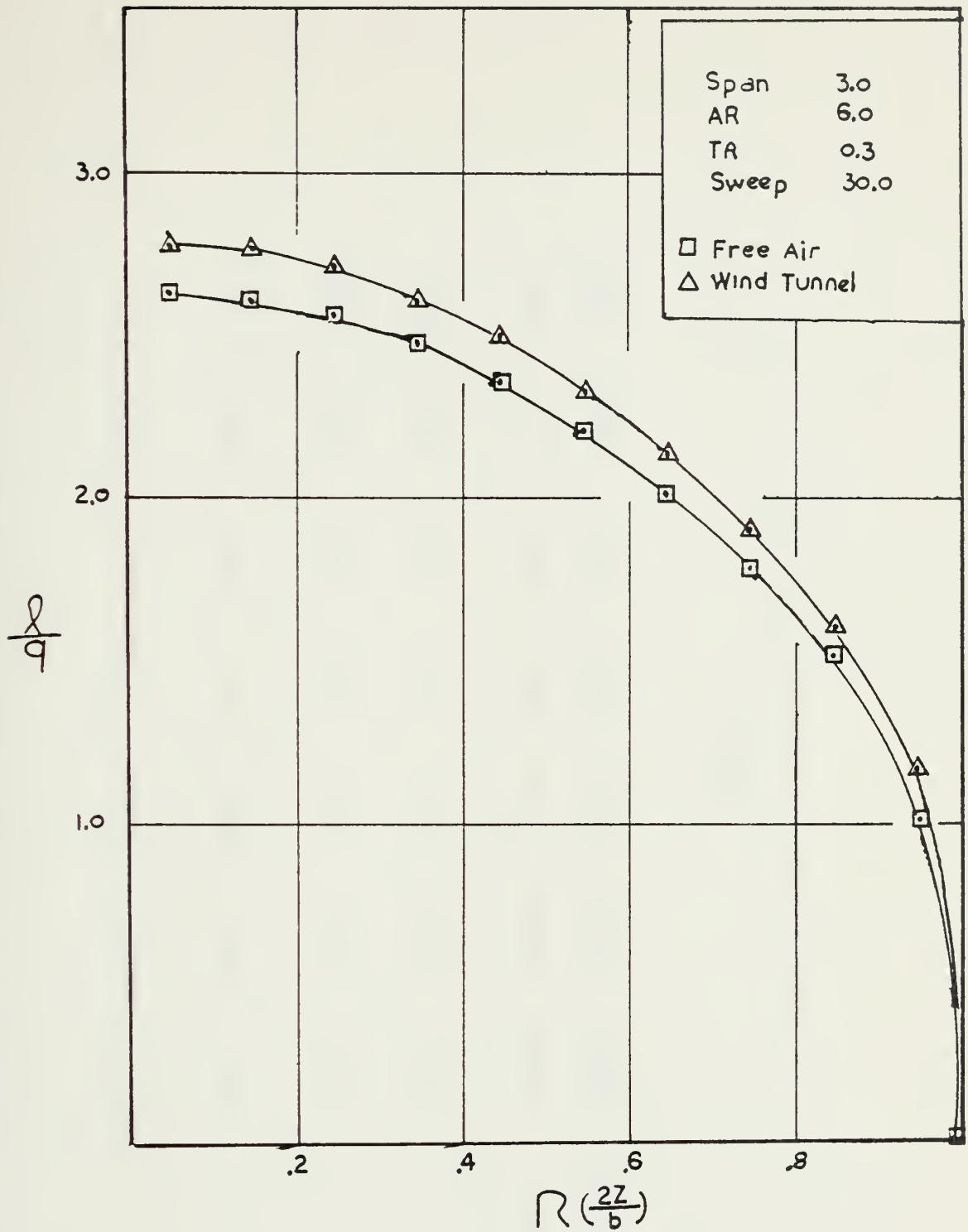


Figure 4. Wing Span Load Distribution

SPAN RATIO	.4	.5	.6	.7	.8	.9	.10
$C_{L\alpha_{FA}}$	4.2545	4.2545	4.2545	4.2545	4.2545	4.2545	4.2545
$C_{L\alpha_T}$	3.354	4.4135	4.4907	4.594	4.7489	5.6563	6.2838
$C_{D_{FA}}$.9342	.9342	.9342	.9342	.9342	.9342	.9342
C_{D_T}	.8855	.8583	.8240	.7793	.7145	.5904	-.003
$\Delta\alpha$ Correction	.30799	.48539	.7086	.9955	1.4022	2.1358	4.3493
ΔC_D Correction	.0049	.00755	.0107	.0147	.0199	.0285	.0517

Table 2
Wing Parameter Variation With Span

c/4 Chord Sweep	0	5	10	15	20	25	30	35	40
$C_{L\alpha_{FA}}$	4.2545	4.3929	4.3816	4.3479	4.290	4.205	4.09	3.9401	3.7505
$C_{L\alpha_T}$	4.4907	4.6475	4.6347	4.5966	4.5312	4.4355	4.3062	4.1388	3.9285
$C_{D_{FA}}$.9342	.9948	.9924	.9806	.9585	.9252	.8796	.8208	.7480
C_{D_T}	.824	.882	.8799	.8694	.8494	.8190	.7773	.7235	.6570
$\Delta\alpha$ Correction	.7086	.7144	.7141	.7129	.7107	.70754	.7035	.69845	.69197
ΔC_D Correction	.0107	.01073	.01072	.01072	.01072	.01071	.01069	.01066	.01061

Table 3

Wing Parameter Variation with Sweep Angle

and sweep angle. Figures 4 and 5 illustrate the span loads calculated for a typical wing. It is interesting to note that as sweep angle increased, negative induced drag appears on the outboard wing stations. Therefore, total induced drag is seen to steadily decrease with increasing sweep angle.

As sweep angle is increased, the free air lift curve slope decreases. Correspondingly, the corrections to angle of attack and induced drag are reduced. Figure 6 graphically displays the data for a straight wing. In the past, the correction factors for the NPS 3.5 X 5.0 ft octagonal wind tunnel were obtained by assuming an elliptic cross-section. The correction factors presented in Ref. 1 for elliptic cross-section are 0.610 for angle of attack and 0.0106 for induced drag. In comparison, the vortex lattice program computes values of 0.7086 and 0.01075, respectively. It is interesting to note that the induced drag correction is almost identical, whereas the correction to angle of attack is slightly higher for the octagonal wind tunnel. Figure 7 illustrates the angle of attack correction factor with varying tunnel span ratios. The correction factor can be seen to steadily increase with the span ratio.

It is an interesting observation that the value of induced drag for a wing span of 5.0 ft was almost zero. This compares very well with airfoil theory in that a wing

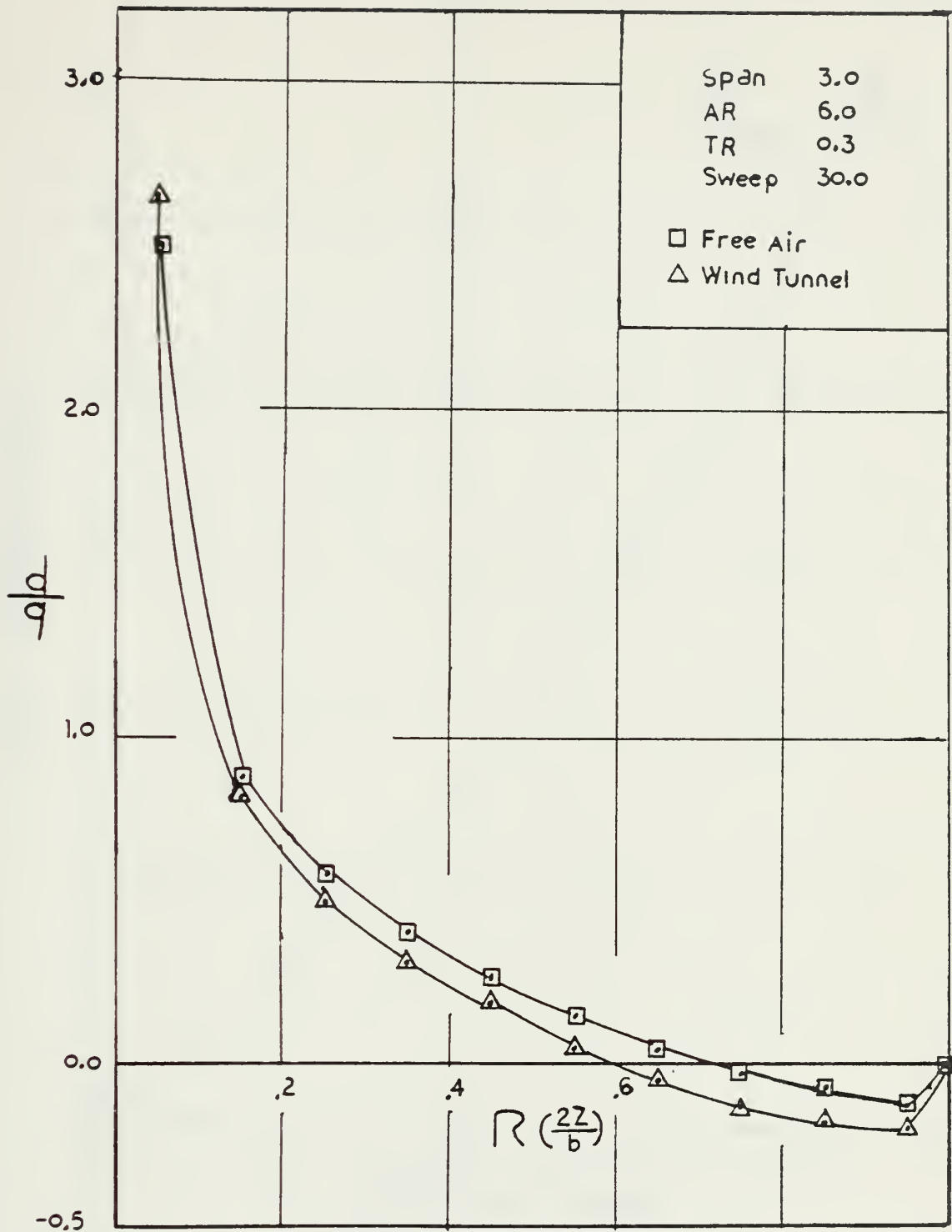


Figure 5. Induced Drag Distribution

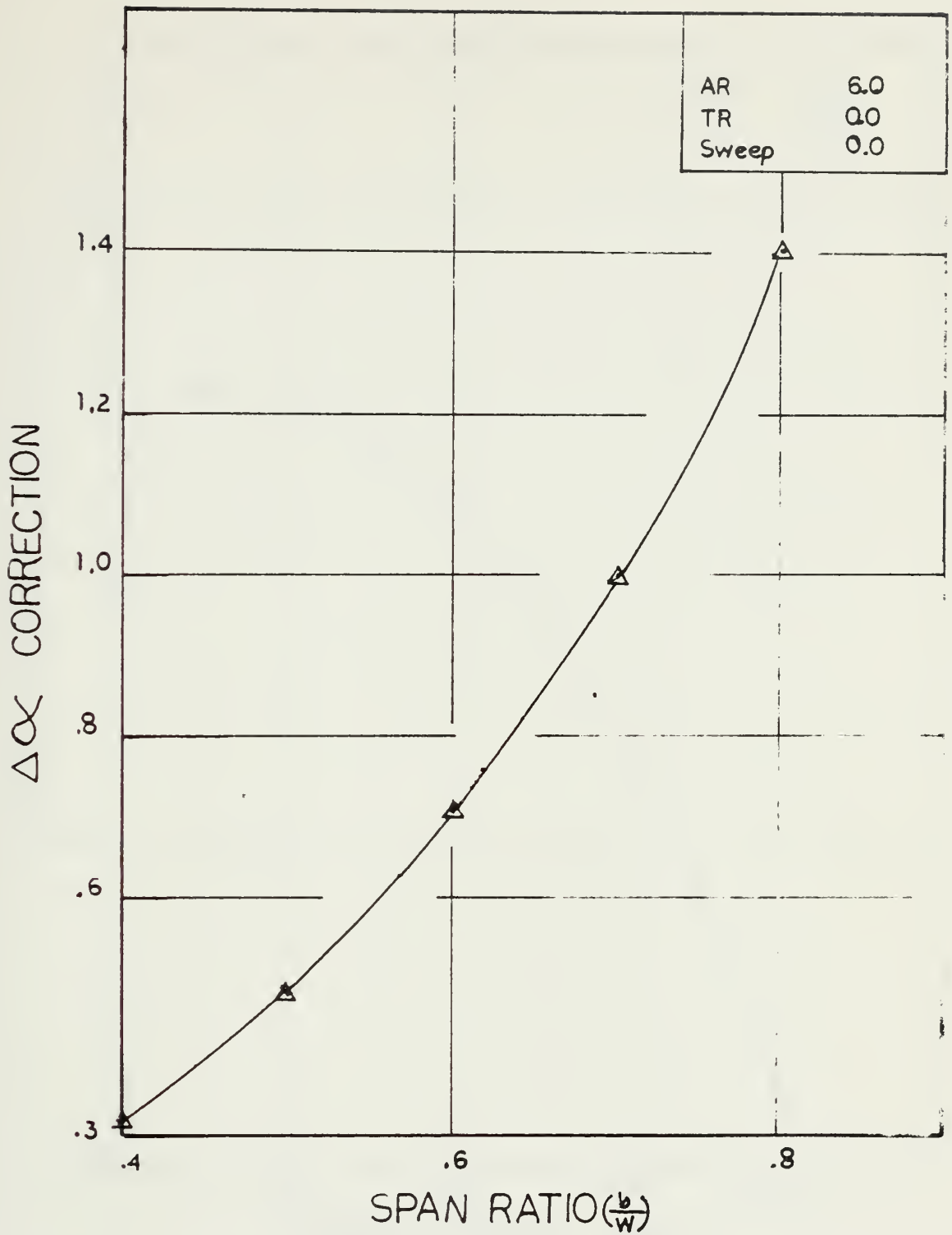


Figure 6. Angle of Attack Correction Factor Plotted as a Function of Span Ratio

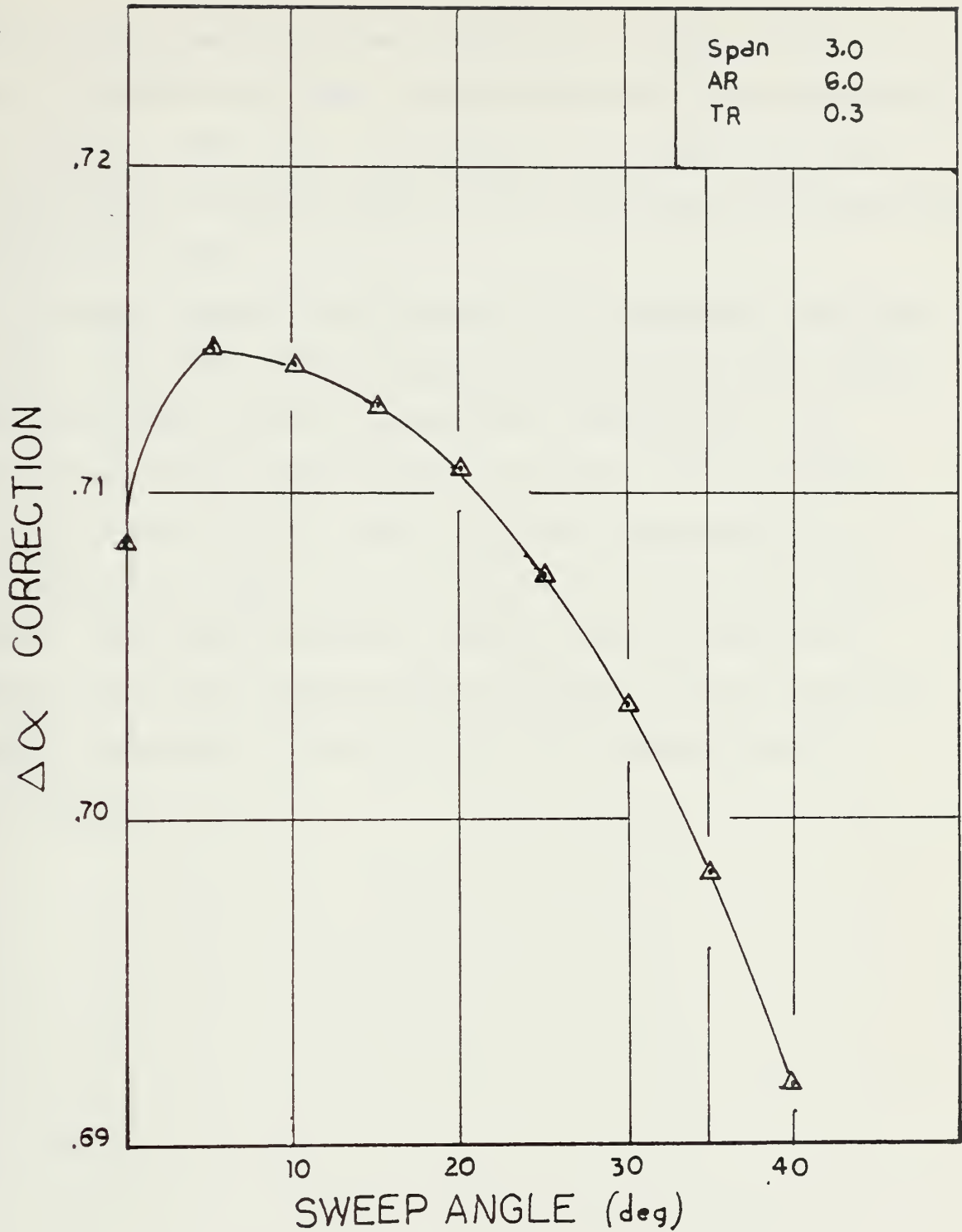


Figure 7. Angle of Attack Correction Factor Plotted As A Function Of Sweep Angle

which spans the wind tunnel represents an approximation to the two-dimensional wing. Induced drag for a two-dimensional wing should equal zero. In addition, the wind-tunnel lift curve slope is within 0.0006 of the theoretical two-dimensional value of $2\pi \text{ rad}^{-1}$.

A sample computer run was made for the moment correction factor. The tail quarter-chord was placed two feet behind the wing bound vortex, on the tunnel centerline. The correction factor obtained for a straight wing of aspect ratio 6.0 was -0.2297. For a wing with sweep angle of 30 degrees and taper of 0.3, a value of -0.1887 was calculated. The above correction factors must be multiplied by the stabilizer effectiveness parameter, using consistent angular measures, in order to find the pitching moment correction.

IV. CONCLUSIONS AND RECOMMENDATIONS

It is felt that the vortex lattice computer program as presented in this paper offers a very reliable and flexible tool for the determination of wind-tunnel wall corrections. It is capable of treating wings of any span, taper ratio, aspect ratio, and quarter-chord sweep, subject to the constraint of straight leading and trailing edges. The geometric shape of the wind tunnel cross-section can similarly be varied at the discretion of the program user. Resultant accuracy appears to be excellent. However, caution should be exercised in determining the vortex loop size. As the wing is positioned closer to the walls, a smaller, more definitive vortex loop representation must be used.

A logical extension of this program would be the inclusion of wings with an antisymmetric load distribution. Furthermore, slight modifications could incorporate the ability to consider the wall effects on other stability derivatives. In its present form, this program offers the wind tunnel user a versatile tool for determination of wind tunnel wall corrections.

APPENDIX A

The general assumptions used in the compilation of this program are listed below.

1. The two-dimensional lift-curve slope is $2\pi \text{ rad}^{-1}$.
2. The wing load distribution is symmetrical.
3. Aeroelastic effects were not considered.
4. The wing is located on the horizontal and vertical centerline of the wind tunnel.
5. The leading and trailing edges of the wing are straight.

APPENDIX B

DEVELOPMENT OF INDUCED VELOCITY EQUATIONS

The equations required to solve for induced velocities consist of two main types. One equation solves for the velocity induced by an arbitrarily oriented vortex segment, whereas the other basic equation applies to horseshoe vortex elements. These equations have been incorporated in sub-routines LOOP and HSHOE, respectively. The development of these equations presented below follows closely that found in Ref. 4 and 5.

According to the Biot-Savart law, the velocity induced at a point p is found from:

$$\bar{w} = \frac{\Gamma}{4\pi h} (\cos B_1 + \cos B_2) \bar{v} \quad (1B)$$

For vortex segments oriented in the Y-Z plane,

$$\cos B_1 + \cos B_2 = \frac{R_1 + R_2}{2R_1 R_2 S} (S^2 - (R_1 - R_2)^2) \quad (2B)$$

It is now necessary to consider \bar{v} , the unit vector which establishes direction. From Fig. 8, it can be seen that

$$\bar{v} = \frac{\bar{R}_1 \times \bar{S}}{|\bar{R}_1 \times \bar{S}|} \quad (3B)$$

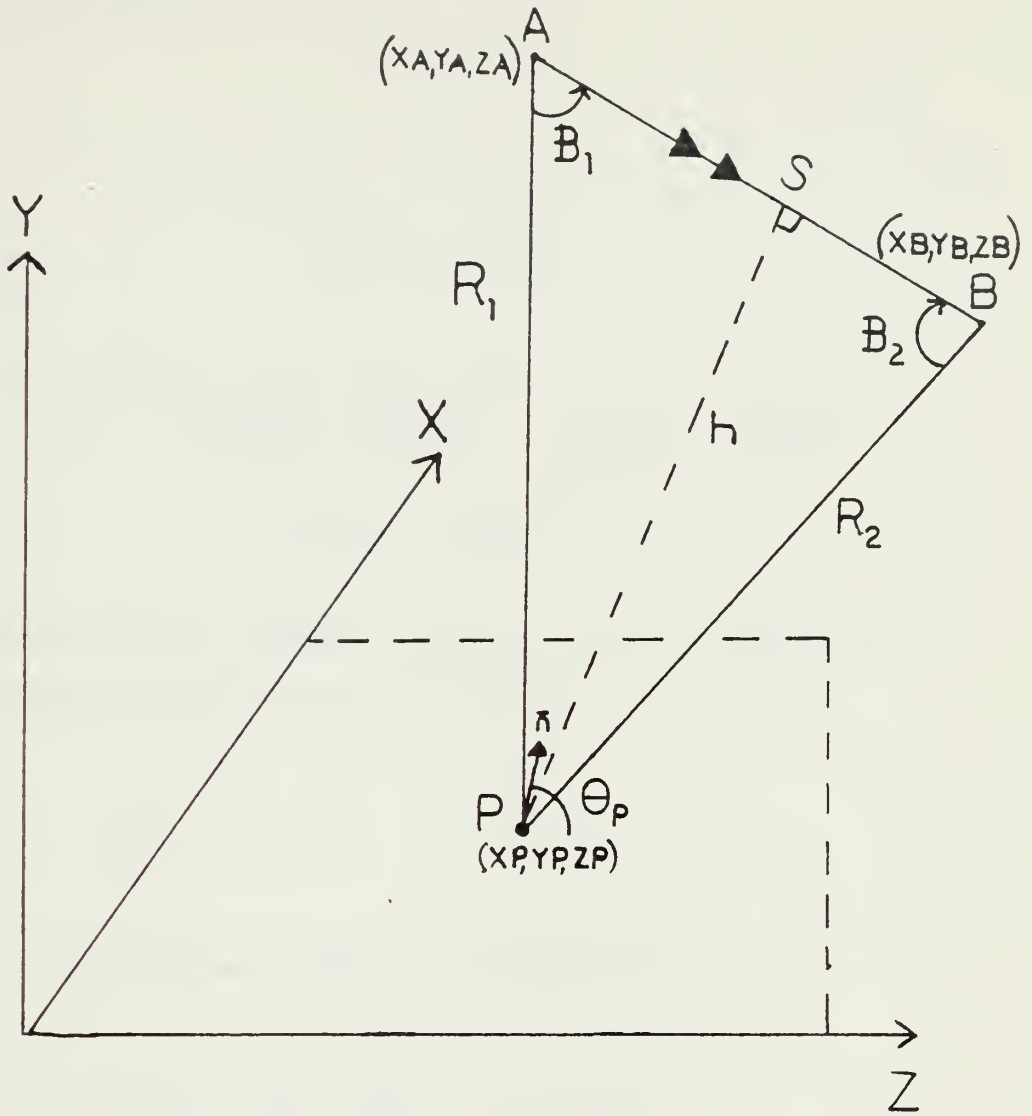


Figure 8. Velocity Induced By A Vortex Segment

Noting from Fig. 8 that

$$hs = |\bar{R}_1 \times \bar{S}| \quad (4B)$$

then

$$hs = [(R_{1Y}S_Z - R_{1Z}S_Y)^2 + (R_{1Z}S_X - R_{1X}S_Z)^2 + (R_{1X}S_Y - R_{1Y}S_X)^2]^{1/2}$$

Calculating the induced velocity in the direction of outward normal of point P per unit Γ ,

$$\frac{w}{\Gamma} = \frac{V}{\Gamma} \cdot \bar{n} \quad (5B)$$

where the unit normal vector is defined by:

$$\bar{n} = o\bar{i} + (\sin \theta_p)\bar{j} + (\cos \theta_p)\bar{k}$$

Therefore, one finally obtains:

$$\frac{w}{\Gamma} = \frac{R_1 + R_2}{8\pi R_1 R_2 (hs)^2} [S^2 - (R_1 - R_2)^2] \cdot [(\sin \theta_p)(R_{1Z}S_X - R_{1X}S_Z) + (\cos \theta_p)(R_{1X}S_Y - R_{1Y}S_X)] \quad (6B)$$

A conditional statement must be included in the program to set the downwash equal to zero if h_s is equal to zero. This will preclude having a zero term in the denominator.

The trailing elements of a vortex loop can be treated with more simplicity. For these segments,

$$\cos B_1 = \frac{(R_1^2 - h^2)^{1/2}}{R_1} \tag{7B}$$

$$\cos B_2 = \frac{(R_2^2 - h^2)^{1/2}}{R_2}$$

However, it can be seen from Fig. 8 that

$$R_1^2 = (x_p - x_A)^2 + (y_A - y_p)^2 + (z_A - z_p)^2 \tag{8B}$$

$$h^2 = (y_A - y_p)^2 + (z_A - z_p)^2$$

Combining equations 7 and 8,

$$\cos B_1 = \frac{x_p - x_A}{R_1} \tag{9B}$$

$$\cos B_2 = \frac{x_B - x_p}{R_2}$$

As a result, the equation for the trailing elements of a vortex loop is simply

$$\frac{w}{\Gamma} = \frac{\cos B_1 + \cos B_2}{4\pi h^2} [(\sin \theta_p)(z_A - z_p) + (\cos \theta_p)(y_p - y_A)] \quad (10B)$$

For the horseshoe vortex, the equation for the bound segment is identical to equation 6. Similarly, the trailing elements can be treated as in equation 11 with a slight modification. In this case, the cosine of one enclosed angle is equal to 1, since the trailing element extends downstream to infinity. The induced velocity equation becomes

$$\frac{w}{\Gamma} = \frac{1 + \cos B_1}{4\pi h^2} [(z_A - z_p)\bar{j} + (y_p - y_A)\bar{k}]$$

$$\frac{w}{\Gamma} = \frac{1 + \cos B_1}{4\pi h^2} [(\sin \theta_p)(z_A - z_p) + (\cos \theta_p)(y_p - y_A)] \quad (11B)$$

APPENDIX C
COMPUTER PROGRAM INPUT

Card Number	Column Number	Description	Format
1	1-72	Program title	18A4
2	1-5	MM=Number of Spanwise Stations	I5
	6-10	NN=Number of Downstream Stations	I5
	11-20	Deltax=Loop length	F10.0
3	1	NOPT=1 for Ground Effect	I1
	2	NTAIL=1 for tail-on	I1
4	1-72	Tunnel y-coordinates (one quadrant only)	8F10.0
5	1-72	Tunnel z-coordinates (one quadrant only)	8F10.0
6	1-10	Span	F10.0
	11-20	Aspect Ratio	F10.0
	21-30	Taper Ratio	F10.0
	31-40	c/4 Sweep (degrees)	F10.0
7	1-10	x-Coordinate of tail quarter-chord	F10.0
	11-20	z-Coordinate of tail quarter-chord	F10.0

Input cards 5 and 6 can be repeated for different planforms and tail locations.


```

C*****
C THIS PROGRAM IS DESIGNED TO CALCULATE THE INTERFERENCE PARAMETERS
C FCR ARBITRARY PLANFORMS IN THE PRESENCE OF THE GROUND CR A WIND-
C TUNNEL OF ANY CROSS-SECTIONAL SHAPE. CORRECTICN FACTORS ARE CCOMPUTED
C FCR ANGLE CF ATTACK, INDUCED DRAG, AND PITCHING MOMENT (FCR TAIL-
C CN CCFICURATICNS).
C*****
C IMPLICIT REAL*8 (A-H,O-Z)
C COMMON/C1/ DELTAX,P8,P4,PI,MM,NN,M4
C COMMON/C2/ SPAN,AR,TR,SC4,B2,NS
C COMMON/C3/ XH(10),XWP(10),ZH1(10),ZH2(10),ZWP(10),C(10),ETA(12)
C COMMON/C4/ XLP(50),XLP(50),YLP(50),YLP(50),THE TAP(50),ZL1(50),ZL2(50)
C COMMON/C5/ YLP(50),XLP(50),WOL(50,10),ROW(10,50)
C DIMENSION CN
C DIMENSION GAMAL(50,10),W(10,10),CLC2(12),CDC2(12)
C DIMENSION DAERO(10,10),WD(10,10),CLC(10),CDC(10)
C DIMENSION TITLE(20),AERO(10,10),COORD(20)
C DIMENSION ROT(1,50),WCT(1,10),Wf(1,10),CLCFA(10),CLCT(10)
C*****
C 1001 FCRMAT(18A4)
C 1002 FCRMAT(4F10.0)
C 1003 FCRMAT(2I5,F10.0)
C 1004 FCRMAT(8F10.0)
C 1005 FCRMAT(2I11)
C 2001 FCRMAT(1H1,18A4//)
C 2002 FCRMAT(,T12,5HMM = ,I2,1X,4LHVCRTEX RECTANGLES IN TUNNEL CIRCUM
C 2003 FCRMAT(,T12,5HNN = ,I2,1X,37HVEVTEX RECTANGLES DOWNSTREAM/
C 2004 FCRMAT(,T5,19HFREE-AIR SPAN LCADS//)
C 2005 FCRMAT(,T5,17,3HETA,T20,3HL/Q,T34,3HD/Q/)
C 2006 FCRMAT(//IX,T5,32HTHE FREE-AIR LIFT CURVE SLOPE = ,F6.4,1X,
C 2007 FCRMAT(,T5,22HWIND-TUNNEL SPAN LOADS//)
C 2008 FCRMAT(//IX,T7,35HTHE WIND-TUNNEL LIET CURVE SLOPE = ,F6.4,
C 2009 FCRMAT(,T5,28HWIND-TUNNEL WALL CORRECTICNS//T7,12HDEL-ALPHA = ,
C 2010 FCRMAT(,T5,8HCL(8HCL(17,12HDEL-CD = ,F7.5,1X,5HCL*2//)
C 2011 FCRMAT(,T5,24HGRUND EFFECT SPAN LOADS//)
C 2012 FCRMAT(//IX,T7,37HTHE GRUND-EFFECT LIFT CURVE SLOPE = ,F6.4,
C 2013 FCRMAT(,T7,35HTHE WING HEIGHT ABOVE THE GROUND = ,F5.2,
C 2014 FCRMAT(,T7,26HTHE GROUND EFFECT RATIO = ,F6.4//)
C 2015 FCRMAT(,T10,7HSPAN = ,F3.1,1X,4HFEET/T2,15HASPECT RATIO = ,
C 2016 FCRMAT(,T14,HTAPER RATIO = ,F3.1/T5,12HC/4 SWEEP = ,F3.0,1X,

```



```

      CCCRC (8) = YL2(J)
      CCCRD (9) = ZL1(J)
      CCCRD (10) = ZL2(J)
      CALL LCCP (COORD, WASH1)
C   CALCULATE EFFECT IN QUADRANT 1
C   ESTABLISH COORD FOR QUADRANT 2
      CCCRC (7) = YL2(J)
      CCCRD (8) = YL1(J)
      CCCRD (9) = -ZL2(J)
      CCCRD (10) = -ZL1(J)

C   CALCULATE EFFECT IN QUADRANT 2
      CALL LOCP(COORD, WASH2)
      IF (NOPT.EQ.1) GO TO 134
C   ESTABLISH COORD FOR QUADRANT 3
      CCCRC (7) = -YL2(J)
      CCCRD (8) = -YL1(J)
      CCCRD (9) = -ZL2(J)
      CCCRD (10) = -ZL1(J)
      CALL LCCP(COORD, WASH3)
C   CALCULATE EFFECT IN QUADRANT 3
C   ESTABLISH COORD FOR QUADRANT 4
      CCCRC (7) = -YL1(J)
      CCCRD (8) = -YL2(J)
      CCCRD (9) = ZL1(J)
      CCCRD (10) = ZL2(J)
C   CALCULATE EFFECT IN QUADRANT 4
      CALL LOCP(COORD, WASH4)
134 CONTINUE
      RCL(I, J) = WASH1+WASH2+WASH3+WASH4
      GO TO 139

125 CONTINUE
      CALL LCCP(COORD, WASH1)
C   CALCULATE EFFECT FROM END HORSESHOES
C   ESTABLISH COORD FOR QUADRANT 1
      CCCRC (5) = XL1(J)
      CCCRD (6) = YL1(J)
      CCCRD (7) = YL2(J)
      CCCRD (8) = ZL1(J)
      CCCRD (9) = ZL2(J)
      CALL LOCP(COORD, WASH1)
C   CALCULATE EFFECT FOR QUADRANT 1
C   ESTABLISH COORD FOR QUADRANT 2
      CCCRC (6) = YL2(J)
      CCCRD (7) = YL1(J)
      CCCRD (8) = -ZL2(J)
      CCCRD (9) = -ZL1(J)
      CALL LCCP(COORD, WASH2)
C   CALCULATE EFFECT FROM QUADRANT 2

```



```

C      IF (NOPT.EQ.1) GO TO 138
C      ESTABLISH COORD FOR QUADRANT 3
C      CCOORD(6)=-YL2(J)
C      CCOORD(7)=-YL1(J)
C      CCOORD(8)=-ZL2(J)
C      CCOORD(9)=-ZL1(J)
C      CALCULATE EFFECT FROM QUADRANT 3
C      CALL FSHOE (COORD,HL3)
C      ESTABLISH COORD FOR QUADRANT 4
C      CCOORD(6)=-YL1(J)
C      CCOORD(7)=-YL2(J)
C      CCOORD(8)=ZL1(J)
C      CCOORD(9)=ZL2(J)
C      CALCULATE EFFECT FROM QUADRANT 4
C      CALL FSHOE (COORD,HL4)
138 CCNTINUE
139 CCNTINUE
140 CCNTINUE
141 CCNTINUE
C      INVERT THE WALL INFLUENCE COEFFICIENT MATRIX.
C      CALL INVR (ROL,NNM4,50)
C
C      145 CCNTINUE
C      READ IN NEW WING PARAMETERS FOR THIS COMPUTATION.
C      READ(5,1002) SPAN,AR,TR,SC4
C      IF THERE IS NO MORE WING PARAMETER INPUT,GO TO END
C      CF PROGRAM.
C      IF (SPAN.EQ.0.000) GO TO 500
C      ENTER THE NUMBER OF WING HORSESHOE VORTICES.
C      NS = AC. CF HORSESHOE VORTICES (ONE SIDE ONLY)
C      NS=10
C      WRITE(6,2001) (TITLE(I),I=1,18)
C      WRITE TUNNEL PARAMETERS
C      WRITE(6,2002) MM,NN,DELTA X
C      WRITE WING PARAMETERS.
C      WRITE(6,2014) SPAN,AR,TR,SC4,NS
C      CALL GECMW
C
C      CALCULATE EFFECT OF WING ON WALL CONTROL PTS.
C      ESTABLISH COORD FOR WALL CONTROL PTS.

```



```

HL4=0.0D0
IF (J.GE.NNEW) GO TO 208
  CCCRC(5)=XL1(J)
  CCCRC(6)=XL3(J)
  CCCRC(7)=YL1(J)
  CCCRC(8)=YL2(J)
  CCCRD(5)=ZL1(J)
  CCCRD(10)=ZL2(J)
  C  CALCULATE EFFECT FROM QUADRANT 1
  CALL LCOP (COORD,WASH1)
  C  ESTABLISH COORD FOR QUADRANT 2
  CCCRD(7)=YL2(J)
  CCCRD(8)=YL1(J)
  CCCRD(9)=-ZL2(J)
  CCCRD(10)=-ZL1(J)
  C  CALCULATE EFFECT FOR QUADRANT 2
  CALL LCOP (COORD,WASH2)
  IF (NOT.EQ.1) GO TO 207
  C  ESTABLISH COORD FOR QUADRANT 3
  CCCRD(7)=-YL2(J)
  CCCRD(8)=-YL1(J)
  CCCRD(9)=-ZL2(J)
  CCCRD(10)=-ZL1(J)
  C  CALCULATE EFFECT FROM QUADRANT 3
  CALL LCOP (COORD,WASH3)
  C  ESTABLISH COORD FOR QUADRANT 4
  CCCRD(7)=-YL1(J)
  CCCRD(8)=-YL2(J)
  CCCRD(9)=ZL1(J)
  CCCRD(10)=ZL2(J)
  C  CALCULATE EFFECT FROM QUADRANT 4
  CALL LCOP (COORD,WASH4)
207 CONTINUE
  C  ADC CONTRIBUTIONS FROM EACH QUADRANT
  ROW(I,J)=WASH1+WASH2+WASH3+WASH4
  GC TO 209
208 CONTINUE
  C  CALCULATE EFFECT FROM END HORSESHOES
  SET CCORD FOR END HCRSESHCES
  C  CALCULATIONS FOR QUADRANT 1
  CCCRC(5)=XL1(J)
  CCCRD(6)=YL1(J)
  CCCRD(7)=YL2(J)
  CCCRD(8)=ZL1(J)
  CCCRD(9)=ZL2(J)
  C  CALCULATE EFFECT FOR QUADRANT 1
  CALL HSHOE (COORD,HL1)
  C  ESTABLISH COORD FOR QUADRANT 2

```



```

CCCRD(6)=YL2(J)
CCCRD(7)=YL1(J)
CCCRD(8)=-ZL2(J)
CCCRD(9)=-ZL1(J)
C CALCULATE EFFECT FROM QUADRANT 2
CALL HSHOE(COORD,HL2)
IF(NOPT.EG.1)GO TO 206
C ESTABLISH COORD FOR QUADRANT 3
CCCRD(6)=-YL2(J)
CCCRD(7)=-YL1(J)
CCCRD(8)=-ZL2(J)
CCCRD(9)=-ZL1(J)
C CALCULATE EFFECT FROM QUADRANT 3
CALL HSHOE(COORD,HL3)
C ESTABLISH COORD FOR QUADRANT 4
CCCRD(6)=-YL1(J)
CCCRD(7)=-YL2(J)
CCCRD(8)=ZL1(J)
CCCRD(9)=ZL2(J)
C CALCULATE EFFECT FROM QUADRANT 4
CALL HSHOE(COORD,HL4)
206 CCNTINUE
209 RCW(I,J)=HL1+HL2+HL3+HL4
210 CCNTINUE
220 CCNTINUE
C
C
C
C CALCULATE THE DOWNWASH PRODUCED BY THE WING FORSESHOES
CN THE WING CONTROL PTS. (AERO).
C
C
C DEFINE CONTROL PT. COORDINATES FOR THIS ITERATION
C
C
C
C ESTABLISH COORD FOR LEFT SIDE OF WING
CCCRD(5)=XH(J)
CCCRD(6)=C.000
CCCRD(7)=0.000
CCCRD(8)=ZH1(J)
CCCRD(9)=ZH2(J)
C CALCULATE DOWNWASH FROM LEFT SIDE OF WING
CALL HSHOE(COORD,WSHL)
C ESTABLISH COORD FOR RIGHT SIDE OF WING
CCCRD(8)=-ZF2(J)

```



```

C CALCCORD(9)=-ZF1(J)
C CALCULATE DOWNWASH FROM RIGHT SIDE OF WING
C CALL HSHOE (COORD,WSHR)
C AERO(I,J)=(WSHL+WSHR)*0.5D0
C CONTINUE
C CCNTINUE

30
40
C
C
C ESTABLISH COORD FOR INCUCED DRAG CALCULATION
DC 60 I=1,NS
C DEFINE C/4 CONTROL PCINTS FOR THIS ITERATION
CCCRD(1)=XH(I)
CCCRD(2)=C.CD0
CCCRD(3)=ZWF(I)
CCCRD(4)=-50.0D0
C ESTABLISH COORD FOR LEFT WING
DC 50 J=1,NS
CCCRD(5)=XH(J)
CCCRD(6)=0.CD0
CCCRD(7)=C.CD0
CCCRD(8)=ZH1(J)
CCCRD(9)=ZF2(J)
C CALCULATE C/4 DOWNWASH FOR LEFT WING
C CALL HSHOE (COORD,WSHL)
C ESTABLISH COORD FOR RIGHT WING
CCCRD(8)=-ZF2(J)
CCCRD(9)=-ZF1(J)
C CALCULATE C/4 DOWNWASH FOR RIGHT WING
C CALL HSHOE (COORD,WSHR)
C AERO(I,J)=(WSHL+WSHR)*0.5D0
C CONTINUE
C CCNTINUE

50
60
C
C
C FIND THE TOTAL DOWNWASH AT WING CONTROL PTS.
C MULTIPLY (ROW)*(GAMAL) TO GET WALL EFFECT ON WING CONTROL PTS.
CC 250 I=1,NS
C SET 1.0 RADIAN ANGLE CF ATTACK ACROSS SEMI-SPAN.
CC CLC(I)=1.0D0
CC 240 J=1,NS
CC KW=0.0D0
CC 230 K=1,NNM4
CC W=WM+ROW(I,K)*GAMAL(K,J)
C 23C CCNTINUE
C SET (W) EQUAL TO TOTAL WING DOWNWASH (AERO-WALL EFFECT)
W(I,J)=(AERO(I,J)-(W*0.5D0))
C 240 CCNTINUE

```



```

25C CCNTINUE
C ELU AND SLVB TO SOLVE : (L/Q)*(AERC)=(ALPHA)
CALL ELU (AERO,NS,10)
CALL SLVB (AERO,NS,10,CLC)
WRITE(6,2003)
WRITE(6,2004)

C SOLVE THE MATRIX EQN : (D/Q)=(L/Q)*(CAERO)*(L/G)
CC 80 I=1,NS
DI=C-OC0
CC 50 K=1,NS
DI = DI+DAERO(I,K)*CLC(K)
CCNTINUE
C CETA IN CDC
CCC(I) = CLC(I)*DI
ETA2=ZWP(I)/B2
C WRITE WING SPAN LOADS IN FREE AIR.
WRITE(6,2005) ETA2,CLC(I),CDC(I)
80 CCNTINUE
CLC2(1)=CLC(1)
CLC2(12)=0.000
CCC2(1)=CDC(1)
CCC2(12)=0.000
CC 10 I = 2,11
CCC2(I)=CDC(I-1)
CLC2(I)=CLC(I-1)
CLCFA(I-1)=CLC(I-1)
1C1 CCNTINUE

C INTEGRATE SPAN LOADS TO OBTAIN LIFT-CURVE SLOPE
AND INDUCED DRAG IN FREE AIR.
CALL CQTFG (ETA,CLC2,CDC2,12)
CALL CQTFG (ETA,CDC2,CDC2,12)
C CAVE=SPAN/AR
CLFA=CLC2(NS+2)/CAVE
CDFA=CCC2(NS+2)/CAVE
WRITE(6,2006) CLFA,CDFA

C
C
C CALCULATE WALL EFFECT CN WING C/4 CONTROL PTS FOR
INDUCED DRAG CALCULATIONS.
ESTABLISH COORD FOR WING C/4 PTS.
CC 280 I = 1,NS
CCCCR(1)=XF(I)
CCCCR(2)=0.000
CCORD(3)=ZWP(I)

```



```

CCCCRC(4)=-90.0D0
CC 270J=1,NM4
WASH3=0.0D0
WASH4=0.0D0
HL3=0.0D0
HL4=0.0D0
IF (J.GE.NNEW) GO TO 265
C CALCULATIONS FOR QUADRANT 1
CCCCRC(5)=XLI(J)
CCCCRC(6)=XL3(J)
CCCCRC(7)=YLI(J)
CCCCRC(8)=YL2(J)
CCCCRC(9)=ZLI(J)
CCCCRC(10)=ZL2(J)
C CALCULATE EFFECT FROM QUADRANT 1
CALL LCOP (COORD,WASH1)
C ESTABLISH COORD FOR QUADRANT 2
CCCCRC(7)=YL2(J)
CCCCRC(8)=YLI(J)
CCCCRC(9)=-ZL2(J)
CCCCRC(10)=-ZLI(J)
C CALCULATE EFFECT FOR QUADRANT 2
CALL LCOP (COORD,WASH2)
IF (NOPT.EQ.1) GO TO 264
C ESTABLISH COORD FOR QUADRANT 3
CCCCRC(7)=-YL2(J)
CCCCRC(8)=-YLI(J)
CCCCRC(9)=-ZL2(J)
CCCCRC(10)=-ZLI(J)
C CALCULATE EFFECT FROM QUADRANT 3
CALL LCOP (COORD,WASH3)
C ESTABLISH COORD FOR QUADRANT 4
CCCCRC(7)=-YL2(J)
CCCCRC(8)=-YLI(J)
CCCCRC(9)=ZLI(J)
CCCCRC(10)=ZL2(J)
C CALCULATE EFFECT FROM QUADRANT 4
CALL LCOP (COORD,WASH4)
264 CONTINUE
C ADD CONTRIBUTIONS FROM EACH QUADRANT
RCW(I,J)=WASH1+WASH2+WASH3+WASH4
GO TO 269
265 CONTINUE
C SET COORD FOR END HORSESHOES
CCCCRC(5)=XLI(J)
CCCCRC(6)=YLI(J)
CCCCRC(7)=YL2(J)
CCCCRC(8)=ZLI(J)

```



```

CCRC(9)=ZL2(J)
C   CALCULATE EFFECT FOR QUADRANT 1
  CALL HSHOE (COORD,HL1)
C   ESTABLISH COORD FOR QUADRANT 2
  CCRC(6)=YL2(J)
  CCRC(7)=YL1(J)
  CCRC(8)=-ZL2(J)
  CCRC(9)=-ZL1(J)
C   CALCULATE EFFECT FRGM QUADRANT 2
  CALL HSHOE (COORD,HL2)
  IF (NOPT.EQ.1) GO TO 268
C   ESTABLISH COORD FOR QUADRANT 3
  CCRC(6)=-YL2(J)
  CCRC(7)=-YL1(J)
  CCRC(8)=-ZL2(J)
  CCRC(9)=-ZL1(J)
C   CALCULATE EFFECT FRGM QUADRANT 3
  CALL HSHOE (COORD,HL3)
C   ESTABLISH COORD FOR QUADRANT 4
  CCRC(6)=-YL1(J)
  CCRC(7)=-YL2(J)
  CCRC(8)=ZL1(J)
  CCRC(9)=ZL2(J)
C   CALCULATE EFFECT FROM QUADRANT 4
  CALL HSHOE (COORD,HL4)
268 CCNTINUE
265 CCNTINUE
270 CCNTINUE
280 CCNTINUE
C   (ROW)*(GAMAL) TO GET WALL EFFECT CN WING
  C/4 CCNTROL PTS.
  CC 320 I =1,NS
  CC 310 J =1,NS
  W =0.0D0
  CC 300 K =1,NM4
  W=W+ROW(I,K)*GAMAL(K,J)
300 CCNTINUE
C
C   SET (WD) EQUAL TO TOTAL DCWNWASH AT C/4 PTS : (DAERC-WALL EFFECT)
  WD(I,J)=(CAERO(I,J)-(WW*.5D0))
310 CCNTINUE
  CLC(I)=1.0D0
320 CCNTINUE
C
C   ELU AND SLVB TO SOLVE THE MATRIX EQUATION :
  (ALPHA)=(AERC-W)*(L/Q).

```



```

CALL ELU (W,NS,10)
CALL SLVB (W,NS,10,CLC)
IF(NOPT.EQ.1) GO TC 321
WRITE(6,2007)
GC TO 322
321 CCNTINUE
322 WRITE(6,2010)
CCNTINUE
WRITE(6,2004)

C SOLVE THE MATRIX EQN. : (D/Q)=(L/Q)*(WD)*(L/Q)
CC 330 I=1,NS
CC 329 K=1,NS
CC 329 CL=DI+WD(I,K)*CLC(K)

329 CCNTINUE
C OBTAIN CDC
ETA2=ZWP(I)/B2
C WRITE WING SPAN LOADS IN PRESENCE OF WALL.
330 CCNTINUE
CLC2(I)=CLC(I)*D1
CCC2(I)=CCC(I)
CLC2(I2)=0.000
CCC2(I2)=0.000
CC 340 I=2,11
CLC2(I)=CLC(I-1)
CCC2(I)=CCC(I-1)
CLC(I-1)=CLC(I-1)
CCC(I-1)=CCC(I-1)
CCNTINUE
340 CCNTINUE
C INTEGRATED DRAG IN WALL EFFECT.
AND INDUCTED DRAG (ETA,CLC2,CLC2,12)
CALL LGTFG (ETA,CDC2,CDC2,12)
CALL LGTFG (ETA,CDC2,CDC2,12)
CLT=CLC2(NS+2)/CAVE
CCT=CCC2(NS+2)/CAVE
IF(NOPT.EQ.1) GO TC 342
WRITE(6,2008) CLT,CCT
DKT=CCT/(CLT**2)
DKFA=CCDFA/(CLFA**2)
DELCD=DKFA-DKT
C CONVERT LIFT-CURVE SLOPE TO DEGREES.
CLFA=CLFA*.01745329D0
CLT=CLT*.01745329D0
DELA=(1.0D0)/CLFA-1.0D0/CLT)
WRITE(6,2009) DELA,DELCD
GC TO 341

```



```

342 CCNTINUE HEIGHT ABOVE THE GROUND.
C WRITE WING HEIGHT ABOVE THE GROUND.
  WRITE(6,2012) Y(1)
  WRITE(6,2011) CLT,CDT
C CALCULATE THE GROUND-EFFECT RATIO.
  GER=CLT/CLFA
  WRITE(6,2013) GER
341 CCNTINUE
C GC TO THE END CF PROGRAM FCR TAIL-OFF CONFIGURATIONS.
C IF (NTAIL.NE.1) GO TO 400
C
C
C READ IN X AND Z COORDINATES OF TAIL QUARTER-CHRD.
  READ(5,1006) XT,ZT
  WRITE(6,2016) XT,ZT
C CALCULATE DOWNWASH PRODUCED BY THE WING ON THE TAIL.
C ESTABLISH COORD FOR TAIL POSITION.
  CCCRD(1)=XT
  CCCRC(2)=0.000
  COORD(3)=ZT
  CCCRC(4)=-5J.000
C ESTABLISH COORD FOR LEFT WING.
  DO 350 J=1,NS
  CCCRD(5)=XF(J)
  CCCRC(6)=0.000
  COORD(7)=0.000
  CCCRC(8)=ZF1(J)
  CCCRC(5)=ZF2(J)
C CALCULATE EFFECT FRCM LEFT WING
  CALL HSHOE (COORD,WASHL)
  CALL HSHOE (COORD,WASHL)
C
C ESTABLISH COORD FOR RT. WING.
  CCCRD(8)=-ZH2(J)
  CCCRD(5)=-ZH1(J)
C CALCULATE EFFECT FRCM RT. WING.
  CALL HSHOE (COORD,WASHR)
  CALL HSHOE (COORD,WASHR)*0.500
350 CCNTINUE
C
C
C CALCULATE EFFECT OF WALL ON TAIL.
  ESTABLISH COORD FCR LCOP
  ESTABLISH COORD FOR QUADRANT 1
  CC 370 J=1,NNM4
  WAST3=0.000
  WAST4=0.000

```



```

HL3=0.000
HL4=0.000
IF(J.GE.NNEW) GO TC 360
CCCCRD(5)=XL1(J)
CCCCRD(6)=XL3(J)
CCCCRD(7)=YL1(J)
CCCCRD(8)=YL2(J)
CCCCRC(5)=ZL1(J)
CCCCRD(10)=ZL2(J)
C CALCULATE EFFECT FROM QUADRANT 1
CALL LCOP (COORD,WASH1)
C ESTABLISH COORD FOR QUADRANT 2
CCCCRD(7)=YL2(J)
CCCCRD(8)=YL1(J)
CCCCRD(9)=-ZL2(J)
CCCCRD(10)=-ZL1(J)
C CALCULATE EFFECT FROM QUADRANT 2
CALL LCOP (COORD,WASH2)
C SKIF QUADRANT 3 AND GO TO 359
IF (NOPT.EQ.1) GO TO 359
C ESTABLISH COORD FOR QUADRANT 3
CCCCRD(7)=-YL2(J)
CCCCRD(8)=-YL1(J)
CCCCRD(9)=-ZL2(J)
CCCCRD(10)=-ZL1(J)
C CALCULATE EFFECT FROM QUADRANT 3
CALL LCOP (COORD,WASH3)
C ESTABLISH COORD FOR QUADRANT 4
CCCCRD(7)=-YL1(J)
CCCCRD(8)=ZL1(J)
CCCCRD(9)=ZL2(J)
CALL LCOP (COORD,WASH4)
359 CCNTINUE
360 CCNTINUE
C CALCULATE EFFECT FROM END HORSESHCES.
ESTABLISH COORD FOR QUADRANT 1
CCCCRD(5)=XL1(J)
CCCCRD(6)=YL1(J)
CCCCRD(7)=YL2(J)
CCCCRD(8)=ZL1(J)
CCCCRD(9)=ZL2(J)
C CALCULATE EFFECT FROM QUADRANT 1
CALL HSHOE (COORD,HL1)
C ESTABLISH COORD FOR QUADRANT 2
CCCCRD(6)=YL2(J)
CCCCRD(7)=YL1(J)

```



```

CCORD(8)=-ZL2(J)
CCORD(5)=-ZL1(J)
C   CALCULATE EFFECT FROM QUADRANT 2
CALL FSHCE (COORD,HL2)
IF (NOPT.EQ.1) GO TO 369
C   ESTABLISH COORD FOR QUADRANT 3
CCORD(6)=-YL2(J)
CCORD(7)=-YL1(J)
CCORD(8)=-ZL2(J)
CCORD(9)=-ZL1(J)
C   CALCULATE EFFECT FROM QUADRANT 3
CALL FSHCE (COORD,HL3)
C   ESTABLISH COORD FOR QUADRANT 4
CCORD(6)=-YL1(J)
CCORD(7)=-YL2(J)
CCORD(8)=ZL1(J)
CCORD(9)=ZL2(J)
C   CALCULATE EFFECT FROM QUADRANT 4
CALL FSHOE (COORD,HL4)
365 CCNTINUE
RCT(1,J)=HL1+HL2+HL3+HL4
370 CCNTINUE
C   CALCULATE TAIL DOWNWASH ANGLE IN FREE AIR.
EFA=0.000
CC 380 I=1,NS
EFA=EFA+WOT(1,I)*CLCFA(I)
38C CCNTINUE
C   CALCULATE TAIL DOWNWASH ANGLE IN THE PRESENCE OF THE WALL.
MULTIPLY (ROT)*(GAMAL) TO GET WALL EFFECT CN TAIL POSITION.
CC 390 I=1,NS
WT=0.000
CC 385 J=1,NM4
WT=WT+ROT(1,J)*GAMAL(J,I)
38E CCNTINUE
SET (WT) EQUAL TO TOTAL DCNWASH AT THE TAIL.
WT(1,I)=(WOT(1,I)-(WT*0.500))
39C CCNTINUE
C   CALCULATE TAIL DOWNWASH ANGLE IN THE PRESENCE OF THE WALL.
EWT=0.000
CC 395 I=1,NS
EWT=EWT+WT(1,I)*CLCT(I)
39E CCNTINUE
DELE=EWT-EFA
WRITE(6,2015) DELE
40C CCNTINUE
C   RETURN TO MAIN BODY OF PROGRAM FOR CALCULATIONS
C   WITH A NEW WING CONFIGURATION.
GC TO 165

```



```

500 CCNTINUE
STCP
ENC
C*****
C TUNNEL GEOMETRY
C SLBRCTINE GEOMT ESTABLISHES VORTEX RECTANGLE ANC CONTRGL
C PCINT COORDINATES REQUIRED TO CALCULATE LOOP DCWNWASH.
C*****
C DELTAX=VORTEX RECTANGLE LENGTH (X-DIR)
C SIDE=VORTEX RECTANGLE WIDTH
C NN=NUMBER OF VORTEX RECTANGLES IN TUNNEL LENGTH
C INCLUDING THE END HORSESHOE
C M4=1/4 OF THE VORTEX RECTANGLES COMPRISING
C WIND TUNNEL CIRCUMFERENCE
C M4=1/2 OF THE VORTEX RECTANGLES COMPRISING
C THE GROUND REPRESENTATION.
C*****
C M4 X NN SHCULD NOT EXCEED 50.
C*****
C SUBROUTINE GEOMT
C IMPLICIT REAL*8(A-F,O-Z)
C COMMON/C1/ DELTAX,P8,P4,PI,MM,NN,M4
C COMMON/C4/ XL1(50),XL3(50),YL1(50),YL2(50),ZL1(50),ZL2(50)
C COMMON/C5/ YLP(50),XLP(50),THETAP(50),X(10),Y(10),Z(10)
C DIMENSION SIDE(50)
C XN2=DFLCAT(NN/2)
C X(1)=-((XN2*DELTAX)
CC 101 =2,NN
C X(I)=X(I-1)+DELTAX
IC CCNTINUE
K=0
CC 20 I= 1,NN
CC 20 J=1,M4
K=K+1
XL1(K)=X(I)
XL3(K)=XL1(K)+DELTAX
XLP(K)=(XL1(K)+XL3(K))/2.000
YL1(K)=Y(J)
YL2(K)=Y(J+1)
ZL1(K)=Z(J)
ZL2(K)=Z(J+1)
YLP(K)=(YL1(K)+YL2(K))/2.000
ZLP(K)=(ZL1(K)+ZL2(K))/2.000
SIDE(K)=DSQRT((YL2(K)-YL1(K))**2+(ZL2(K)-ZL1(K))**2)
THETAP(K)=DARCOS((YL2(K)-YL1(K))/SIDE(K))
C*****
C CCNTINUE
C CCNTINUE
C RETURN
20
30

```



```

C I=4: THETAP=CUTER NORMAL DIRECTION AT P IN Y-Z PLANE, DEGREES
C I=5: XF=X-COGRD OF HORSESHOE BOUND ELEMENT
C I=6: YH1=Y-COGRD OF HORSESHOE CORNER (1)
C I=7: YH2=Y-COGRD OF HORSESHOE CORNER (2)
C I=8: ZH1=Z-COGRD OF HORSESHOE CORNER (1)
C I=9: ZH2=Z-COGRD OF HORSESHOE CORNER (2)
C WASH = VELOCITY INDUCED AT (P) IN DIRECTION OF OUTER NORMAL
C (OALCNG +Z, 90 ALONG +Y)
C *****
C SUBROUTINE HSHOE (CCCRD, WASH)
C IMPLICIT REAL*8 (A-H, O-Z)
C COMMON/CL/ DELTAX, P8, P4, PI, MM, NN, M4
C DIMENSION C(4)
C XP=COORD(1)
C YP=COORD(2)
C ZP=COORD(3)
C THETAP=COORD(4)*.01745329D0
C XF=COORD(5)
C YF1=COORD(6)
C YF2=COORD(7)
C ZF1=COORD(8)
C ZF2=COORD(9)
C CALCULATE GEOM TERMS
C STP=DSIN(THETAP)
C CTP=CCOS(THETAP)
C R1=DSQRT((XF-XP)**2+(YH1-YP)**2+(ZH1-ZP)**2)
C CSB1=(XP-XH)/R1
C FT1=DSQRT((YH1-YP)**2+(ZH1-ZP)**2)
C IF (HT1.LE.00001C0) GO TO 15
C CALCULATE DELTA-VEL DUE TO LEFT ELEMENT
C DTW1=(1.0D0+CSB1)/(HT1*P4)
C RESOLVE DELTA-VEL COMPONENTS IN THETAP DIRECTION
C WNT1=DTW1*((ZP-ZH1)*(STP)+(YH1-YP)*(CTP))/FT1
C GC TO 18
C CONTINUE
C WNT1=0.0D0
C CONTINUE
C R2=DSQRT((XH-XP)**2+(YH2-YP)**2+(ZH2-ZP)**2)
C CSB2=(XP-XH)/R2
C FT2=DSQRT((YH2-YP)**2+(ZH2-ZP)**2)
C IF (HT2.LE.00001C0) GO TO 16
C CALCULATE DELTA-VEL DUE TO RIGHT ELEMENT
C DTW2=(1.0D0+CSB2)/(HT2*P4)
C RESOLVE DELTA-VEL COMPONENTS IN THETAP DIRECTION
C WNT2 = DTW2*((ZP-ZH2)*(STP)+(YP-YH2)*(CTP))/HT2
C GC TO 15
C CONTINUE
C WNT2=C.0D0

```



```

19 CCNTINUE
   RXSZ=(XF-XP)*(ZH2-ZH1)
   RXXSY=(XF-XP)*(YH2-YH1)
   RYSZ=(YH1-YP)*(ZH2-ZH1)
   RYSY=(YH1-ZP)*(YH2-YH1)
   S=DSQRT((RYSZ-RZSY)**2+(ZH2-ZH1)**2)
   FS=CSQRT((RYSZ-RZSY)**2+(RXSZ)**2)
   IF (HS.LE.C00001C0) GO TO 30
   C FIN DELTA-VEL DUE TO BCND ELEMENT
   C RESOLVE DELTA-VEL COMPONENTS IN THETAP DIRECTION
   WNB = CRW*((-STP*RXSZ)+(CTP*RXS))
   CC TO 40
30 CCNTINUE
40 WNB=0.0C0
   CCNTINUE
   WASH = WNB+WNT1+WNT2
   RETURN
END
C*****
C SLERCLTINE INVR(A,N,ISIZE)
C SLERCLTINE INVR COMPNED THE INVERSE OF THE INFUT MATRIX
C (A). (A) IS DIMENSIONED ISIZE BY ISIZE AND CCNTAINS N ROWS
C ANCLTINE INVR(A,N,ISIZE)
C SLBRPCLTINE INVR WAS CBTAINED FRCM THE FOLLOWING REFERENCE SOURCE:
C JCPRT WINGS, " WIND TUNNEL INTERFERFENCE FACTORS FOR HIGH-
C LIFT WINGS, IN CLOSED WIND TUNNELS", NASA CR-2191, FEB. 1973.
C*****
C*****
C SLEROUTINE INVR(A,N,ISIZE)
C IMFLICIT REAL*8 (A-H,O-Z)
C DIMENSION A(50,50),PIVCT(100)
C DIMENSION IPIVOT(100),INDEX(100,2)
C EQUIVALENCE (AMAX,T,SWAP)
C CC 101 J=1,N
C IPIVCT(J)=0
C CC 550 I=1,N
C AMAX=0.CD0
C CC 105 J=1,N
C IF (IPIVOT(J)-1)107,1C5,107
C CC 120 K=1,N
C IF (IPIVOT(K)-1) 109,12C,740
C IF ((IPIVOT(K))-DABS(A(J,K))) 111,120,120
C IFCW=J
C CCCLUM=K
C AMAX=A(I,J)
C CCNTINUE
100
101
102
104
106
107
108
109
111
112
113
120
125

```



```

110 IPIVOT(ICOLUMN)=IPIVCT(ICOLUMN)+1
130 IF (IROW-ICCLUM) 140,260,140
140 CCNTINUE
150 CC 200 L=1,N
160 SWAP=A(IROW,L)
170 A(IROW,L)=A(ICOLUMN,L)
200 A(ICOLUMN,L)=SWAP
260 INDEX(I,1)=IROW
270 INDEX(I,2)=ICOLUMN
310 PIVCT(I)=A(ICOLUMN,ICOLUMN)
330 A(ICOLUMN,ICCLUM)=I.0
340 CC 350 L=1,N
350 A(ICOLUMN,L)=A(ICOLUMN,L)/PIVCT(I)
380 CC 550 LI=1,N
390 IF(LI-ICCLUM) 400,550,400
400 T=A(LI,ICCLUM)
420 A(LI,ICCLUM)=0.0
430 CC 450 L=1,N
450 A(LI,L)=A(LI,L)-A(ICCLUM,L)*T
550 CCNTINUE
600 CC 710 I=1,N
610 L=N+1-INDEX(L,1)-INDEX(L,2) 630,710,630
620 IF (INDEX(L,1)-INDEX(L,2)) 630,710,630
630 JRCW=INDEX(L,1)
640 JCCUM=INDEX(L,2)
650 CC 705 K=1,N
660 SWAP=A(K,JRCW)
670 A(K,JROW)=A(K,JCOLUMN)
700 A(K,JCOLUMN)=SWAP
705 CCNTINUE
710 RETURN
740 ENC
C ***** ELU TRI-DIAGONALIZES THE INPUT MATRIX (A). *****
C ***** SUBROUTINE ELU(A,N,ND) *****
C ***** IMPLICIT REAL*8(A-H,O-Z) *****
C ***** DIMENSION A(ND,ND) *****
C ***** NM1=N-1 *****
C ***** CC 100 K=1,NM1 *****
C ***** KP1=K+1 *****
C ***** CC 100 I=KP1,N *****
C ***** G=-A(I,K)/A(K,K) *****
C ***** A(I,K)=G *****
C ***** CC 100 J=KP1,N *****
C ***** A(I,J)=A(I,J)+G*A(K,J) *****
C ***** RETURN *****
100

```



```

C*****
C  SUBROUTINE SLVB SOLVES THE TRI-DIAGONALIZED MATRIX (A) OBTAINED
C  FROM ELU BY BACK SUBSTITUTION.
C*****
C  SUBROUTINE SLVB(A,N,ND,B)
C  IMPLICIT REAL*8(A-H,O-Z)
C  DIMENSION A(ND,ND),B(ND)
C  N1=N-1
C  NPI=N+1
C  CC 100 K=1,NM1
C  KP1=K+1
C  DC 100 I=KP1,N
C  R(I)=B(I)+A(I,K)*B(K)
C  E(N)=B(N)/A(N,N)
C  CC 300 K=2,N
C  I=NPI-K
C  JJ=I+1
C  CC 200 J=J1,N
C  R(I)=B(I)-A(I,J)*B(J)
C 300 R(I)=B(I)/A(I,I)
C  RETURN
C  END
C*****
C  SUBROUTINE LCOOP (COORD, WASH)
C  FUNCTS INCUCED VELOCITY DUE TO A RECTANGULAR
C  VORTEX LCOOP ELEMENT OF UNIT STRENGTH.
C*****
C  COORD(I) IS A 10 DIM. COLUMN VECTOR
C  XP=X-COORD OF CCNTROL PCINT
C  I= 2: YP=Y-COORD OF CCNTROL PCINT
C  I= 3: ZP=Z-COORD OF CCNTROL PCINT
C  I= 4: THETAP = OUTER NCRMAL DIRECTION AT P IN Y-Z PLANE, DEGREES
C  I= 5: XH1=(XH2)=X-COORD CF CORNERS 1 AND 2
C  I= 6: XH3=(XH4)=X-COORD CF CORNERS 3 AND 4
C  I= 7: YH1=(YH4)=Y-COORD CF CORNERS 1 AND 4
C  I= 8: YH2=(YH3)=Y-COORD CF CORNERS 2 AND 3
C  I= 5: ZH1=(ZH4)=Z-COORD CF CORNERS 1 AND 4
C  I=10: ZH2=(ZH3)=Z-COORD CF CORNERS 2 AND 3
C*****
C  WASH = INDUCED VEL. AT (P) IN DIRECTION OF CUTER NORMAL
C*****
C  SUBROUTINE LCOOP (COORD,WASH)
C  IMPLICIT REAL*8 (A-H,O-Z)
C  COMMON/C1/ DELTAX,P8,P4,PI,MM,NN,M4
C  DIMENSION CCORD(20)
C  XP=CCORD(1)
C*****
1

```



```

YP=COORC(2)
ZP=COORC(3)
THETAP=COORC(4)*0.01745329D0
XH1=COORC(5)
XH2=COORC(6)
YH1=COORC(7)
YH2=COORC(8)
ZH1=COORC(9)
ZH2=COORC(10)
C  FIND VALUES USED BY ALL FCUR PARTS CF VORTEX LOCP CALCS.
1C  STP=DSIN(THETAP)
   CTP=DCOS(THETAP)
   R1=DSQRT((XH1-XP)**2 + (YH1-YP)**2 + (ZH1-ZP)**2)
   R2=DSQRT((XH2-XP)**2 + (YH2-YP)**2 + (ZH2-ZP)**2)
   R3=DSQRT((XH3-XP)**2 + (YH3-YP)**2 + (ZH3-ZP)**2)
   R4=DSQRT((XH3-XP)**2 + (YH1-YP)**2 + (ZH1-ZP)**2)
C  FIND INCUCED VELOCITY DUE TO ELEMENT (1-2)
2C  RXSZ=(XH1-XP)*(ZH2-ZH1)
   RYSY=(XH1-YP)*(YF2-YH1)
   RZSY=(ZH1-ZP)*(YF2-YH1)
   S=DSQRT((YH2-YH1)**2 + (ZH2-ZH1)**2)
   HS=(HS.LE.0.00001C0) GO TO 25
   IF(HS.LE.0.00001C0) GO TO 25
   CBW1=((R1+R2)*(S**2 - (R1-R2)**2)/(P8*HS**2*R1*R2))
   WNB1=CBW1*((-STP*RXSZ) + (CTP*RYSY))
   GC TO 30
   WNB1=0.0D0
C  FIND INCUCED VELOCITY DUE TO ELEMENT (2-3)
3C  FT2=DSQRT((YH2-YP)**2 + (ZH2-ZP)**2)
   IF(HT2.LE.0.00001C0) GC TO 35
   CSB2=((XP-XH1)/R2)
   CSB3=((XH3-XP)/R3)
   CTW2=(CSB2+CSB3)/(P4*HT2)
   WNT2=DTW2*((ZH2-ZP)*STP + (YP-YH2)*CTP)/FT2
   GC TO 40
   WNT2=0.0D0
C  FIND INCUCED VELOCITY DUE TO ELEMENT (3-4)
4C  RXSZ=(XH3-XP)*(ZF1-ZH2)
   RYSY=(XH3-YP)*(YH1-YH2)
   RZSY=(ZH2-ZP)*(YF1-YH2)
   S=DSQRT((YH2-YH1)**2 + (ZH2-ZH1)**2)
   HS=(HS.LE.0.00001C0) GO TO 45
   IF(HS.LE.0.00001C0) GO TO 45
   CBW3=((R3+R4)*(S**2 - (R3-R4)**2)/(P8*HS**2*R3*R4))
   WNB3=CBW3*((-STP*RXSZ) + (CTP*RYSY))
   GC TO 50

```



```

C      WNB3=0.0DC
45  F INC INCUCED VELOCITY DUE TO ELEMENT (4-1)
5C  HT4=DSQRT((YH1-YP)**2 + (ZH1-ZP)**2)
    IF (HT4.LE.C.0000100) GO TO 55
    CSB1=(XP-XF1)/R1
    CSB4=((XH3-XP)/R4
    CTW4=(CSB1+CSB4)/(P4*HT4)
    WNT4=CTW4*((ZP-ZF1)*STP + (YH1-YP)*CTP)/HT4
    GO TO 60
55  WNT4=0.0DO
C  SUM UP INCUCED VELOCITY INCREMENTS.
6C  WASH=WNB1 + WNT2 + WNB3 + WNT4
    RETURN
    END
C *****
C  SUBROUTINE DQTFG
C *****
C  COMPUTES THE VECTOR OF INTEGRAL VALUES FOR A GIVEN
C  GENERAL TABLE OF ARGUMENT AND FUNCTION VALUES.
C  Y: INPUT VECTOR OF FUNCTION VALUES.
C  X: INPUT VECTOR OF ARGUMENT VALUES.
C  Z: RESULTING VECTOR CF INTEGRAL VALUES.
C *****
C  BEGINNING WITH Z(1)=0, EVALUATION OF VECTOR Z IS DONE BY
C  MEANS OF TRAPEZOIDAL RULE (SECCND ORDER FORMULA).
C  SUBROUTINE DQTFG WAS OBTAINED FROM THE NPS SOURCE
C  LIBRARY.
C *****
C  SLERCUTINE DQTFG(X,Y,Z,NDIM)
C *****
C  DIMENSION X(NDIM),Y(NDIM),Z(NDIM)
C  DCUBLE PRECISION X,Y,Z,SUM1,SUM2
C *****
C  SUM2=0.0D0
C  IF(NDIM-1)4,3,1
C *****
C  INTEGRATION LOOP
1  DC 2 I=2,NDIM
   SUM1=SUM2
   SUM2=SUM2+.5D0*(X(I)-X(I-1))*(Y(I)+Y(I-1))
2  Z(I-1)=SUM1
3  Z(ACIM)=SUM2
4  RETURN
   ENC
DTFG 350
DTFG 360
DTFG 370
DTFG 390
DTFG 400
DTFG 410
DTFG 420
DTFG 430
DTFG 440
DTFG 450
DTFG 460
DTFG 470
DTFG 480
DTFG 490
DTFG 500
DTFG 510

```


LIST OF REFERENCES

1. Pope, A. and Harper, J. J., Low Speed Wind Tunnel Testing, John Wiley and Sons, 1966.
2. Kuethe, A. M. and Schetzer, J. D., Foundations of Aerodynamics, John Wiley and Sons, 1968.
3. Etkin, B., Dynamics of Flight, John Wiley and Sons, 1959.
4. Joppa, R. G., "A Method of Calculating Wind Tunnel Interference Factors for Tunnels of Arbitrary Cross-Section", NASA CR-845, July 1967.
5. Joppa, R. G., "Wind Tunnel Interference Factors for High-Lift Wings in Closed Wind Tunnels", NASA CR-2191, February 1973.
6. Gray, W. L. and Schenk, K. M., "A Method for Calculating the Subsonic Steady-State Loading on an Airplane with a Wing of Arbitrary Planform and Stiffness", NACA TN3030, December 1953.
7. Pearson, L. G., Subsonic Lifting Surface Analysis with Static Aeroelastic Effects, M.S. Thesis, Naval Postgraduate School, Monterey, Ca., 1972.
8. Pankhurst, R. C. and Holder, D. H., Wind-Tunnel Technique, Sir Isaac Pitman and Sons, 1952.
9. Garner, H. C., and others, Subsonic Wind Tunnel Wall Corrections, Agardograph 109, October 1966.
10. Russell, Robert W., Design Study of a Center Plate Mount for Wind Tunnel Models, M.S. Thesis, Naval Postgraduate School, Monterey, Ca., 1977.

INITIAL DISTRIBUTION LIST

	No. Copies
1. Defense Documentation Center Cameron Station Alexandria, Virginia 22314	2
2. Library, Code 0142 Naval Postgraduate School Monterey, California 93940	2
3. Department Chairman, Code 67 Department of Aeronautics Naval Postgraduate School Monterey, California 93940	1
4. Professor L. V. Schmidt, Code 67Sx Department of Aeronautics Naval Postgraduate School Monterey, California 93940	1
5. Lt Chester Arthur Heard, USN c/o Lockard 2939 Nob Hill Ct Alexandria, Va. 22314	1



1 DEC 80
13 FEB 81

26018
27002

Thesis
H41725 Heard 170349
c.1

Wind tunnel wall cor-
rections for arbitrary
planforms and wind tun-
nel cross-sections.

1 DEC 80
13 FEB 81

26018
27002

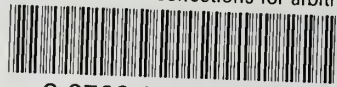
Thesis
H41725 Heard
c.1

170349

Wind tunnel wall cor-
rections for arbitrary
planforms and wind tun-
nel cross-sections.

thesH41725

Wind tunnel wall corrections for arbitra



3 2768 002 08667 0
DUDLEY KNOX LIBRARY