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NAVAL POSTGRADUATE SCHOOL Monterey, California



CONTRACTOR REPORT

WAVE ROTOR RESEARCH: A COMPUTER CODE FOR PRELIMINARY DESIGN OF WAVE DIAGRAMS

A. MATHUR

EXOTECH, INC. 1901 S. BASCOM AVE, SUITE 337 CAMPBELL, CALIFORNIA ,

MAY 1985

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NAVAL POSTGRADUATE SCHOOL Monterey, California

Rear Admiral R. H. Shumaker Superintendent D. A. Schrady Provost

The work reported herein was carried out for the Naval Postgraduate School by Exotech, Inc. under contract N00014-84-C-0677. The work was part of the Air-Breathing Propulsion Research Program carried out at the Turbopropulsion Laboratory under the sponsorship of Naval Air Systems Command, under the cognizance of G. Derderian (AIR310E).

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A one-dimensional program for solving the unsteady, inviscid, compressible flow in wave rotor devices is described. The Random Choice Method implemented in the code is shown to be very suitable for describing the multiple discontinuities and wave interactions in these flows. The modular structure of the program allows studying different "families" of wave diagrams quickly and inexpensively. Example applications are included.

22a NAME OF RESPONSIBLE INDIVIDUAL R. P. SHREEVE (108)6/6-2593 6785
R. P. SHREEVE $(/08)6/6-2503$

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1. INTRODUCTION

Unsteady flow in the passages of wave rotor devices can adequately be modelled on a one-dimensional basis. However, this modelling can be quite involved due to the peculiar characteristics typical of wave rotor type flows. The numerical calculation has to provide approximate solutions of time-dependent compressible fluid flow problems which involve discontinuities and strong wave interactions. Ref. (1) lists three criteria which such approximate solutions should satisfy simultaneously: (i) the solution must be reasonably accurate in smooth regions of the flow. Continuous waves (rarefaction waves, compression waves) should propagate at the correct speed and should maintain the correct shape which involves steepening or spreading at the correct rate; (ii) discontinuities, contact surfaces), should be modelled by sharp and discrete jumps, and should be transported at the correct speed; and (iii) nonlinear discontinuities such as shocks should be computed stably and accurately.

In addition, the complex pattern of shock waves and contact surfaces that could evolve in wave rotor devices precludes the use of numerical methods which rely on either some type of artificial viscosity or a special treatment of discontinuities. Such methods would quickly become quite impractical for this application due to programming difficulties and cost of execution.

Computation of such solutions has generally been carried out by solving a set of finite difference equations which approximate the governing differential equations of flow. All such schemes inherently have a finite amount of dissipation as well as dispersion of the wave modes they model, and it is difficult to construct difference schemes which simultaneously satisfy the criteria given above. Stability problems may also be an added concern for

these schemes.

In view of the foregoing, an alternative approach to solving wave rotor type flows was sought, and the purpose of this report is to describe such a scheme along with some results. The scheme is known variously as Glimm's method, the Random Choice Method (RCM) or the piecewise sampling method. The method evolved from a constructive proof of the existence of solutions to systems of nonlinear hyperbolic conservation laws given by Glimm (Ref. 2). Chorin (Refs. 3 and 4) developed the scheme into an effective numerical tool for gas dynamic applications, with emphasis on detonation combustion problems and reacting gas flows. Although the RCM computes solutions on a fixed grid, it is not a difference scheme, utilizing solutions of locally defined Riemann problems as the basic building blocks for the global solution. Each of the local Riemann problems (defined in more detail in section 2) provides an analytically exact elementary similarity solution. By means of a suitable sampling procedure, usually of a pseudo-random or quasi-random nature, the similarity solutions are superposed to construct the approximate solution to the equations.

With an appropriate sampling technique, the RCM in one dimension is possibly superior to any finite difference scheme in meeting the criteria established above.

2. METHOD

2.1. Solution Procedure

The method models the one-dimensional, compressible, inviscid Euler equations, expressed in conservation form as

$$\frac{\partial U}{\partial t} + \frac{\partial F(U)}{\partial x} = 0$$
, where

$$U(\mathbf{x},\mathbf{t}) = \begin{cases} \rho \\ \rho u \\ E \end{cases} \quad \text{and} \quad F(U) = \begin{cases} \rho \\ \rho u^2 + p \\ (E + p)\rho \end{cases}$$
(1)

Here E is the total energy per unit volume and may be expressed as (for a polytropic gas)

$$E = \rho \varepsilon + \frac{1}{2} \rho u^2 , \quad \varepsilon \stackrel{\Delta}{=} \text{ internal energy per unit mass}$$
$$= \frac{1}{\gamma - 1} \left(\frac{p}{\rho} \right)$$

p is the density, p is pressure and u is velocity in the one space dimension being considered here. With initial data specified in the form

$$U(x,0) = \varphi(x) ,$$

an initial value problem is defined for the Euler equations. The simplest initial value problem for which discontinuities appear is the Riemann problem: to find the gas flow resulting from an initial state in which the gas on the right of an 'origin' is in a constant state, and the gas on the left is in another constant state, i.e.,

with

$$U_{L,R} = \begin{cases} \wp L, R\\ (\wp u)_{L,R}\\ E_{L,R} \end{cases}$$

where the subsripts L and R denote the left and right sides of the 'origin', here arbitrarily prescibed at 0 . That is, the Riemann problem consists of prescribing constant initial data on either side of an origin where a jump discontinuity exists. As mentioned before, the solution of the problem constitutes a basic building block of the random choice method. A special case of the Riemann problem in which $u_L = u_R = 0$ is often referred to as the shock tube problem. The answer to the problem is that there are four possible types of subsequent flow, depending on the inequalities in the left and right side data prescribed. Thus, in both directions from the origin, a shock or a centered rarefaction wave may propagate, giving rise to the above mentioned four different possibilities. Fig. (1) illustrates the special case of shock tube type flow and the evolution of the wave pattern.

Fig. (2) shows the simple fixed Cartesian grid set up for the method. Let Δx be a spatial increment and Δt a time increment. The solution is to be evaluated at time $(n + 1)\Delta t$, n being a non-negative integer, at spatial increments $i\Delta x$, $i = 1,2,3, \ldots$. The initial data is prescribed for each time step at $n\Delta t$ in a piecewise constant manner i.e., it consists of intervals of length Δx where the data is constant, separated by jump discontinuities:

$$U(x, n\Delta t) = U_{i}^{n}, (i\frac{1}{2})\Delta x < x < (i\frac{1}{2})\Delta x$$

The solution at time $(n+1)\Delta t$ then is required to have the same property, i.e., it is piecewise constant over an interval Δx , and it serves as the initial data for the next time step:

$$U(x,(n+1)\Delta t) = U_{i}^{n+1}$$
, $(i - \frac{1}{2})\Delta x < x < (i + \frac{1}{2})\Delta x$

This procedure defines a sequence of local Riemann problems to be solved at each time level. On the grid shown in Fig. 2, for example, initial data would be specified at points 1, 3, 5, setting up a succession of Riemann problems defined by each pair of states (1,3), (3,5), (5,7), with the discontinuities at the midpoint of each, i.e., at 2, 4, 6, etc. If the time step increment Δt is calculated such that

$$\Delta t < \sigma.(\Delta x). \max_{i} (|u_{i}^{n}|+a_{i}^{n}) , \text{ with}$$
$$0 < \sigma < \frac{1}{2}$$

then the waves generated at the discontinuities of adjacent Riemann problems will not interact, as shown schematically in Fig. 2.

Each of the local Riemann problems yields an exact analytical solution, with the resulting wave structure a particular combination/variation of the general structure shown in Fig. 3.

In the x-t plane, the solution to a Riemann problem consists of essentially four regions connected by three waves. Thus states I and IV are the prescribed left and right states for the problem, and states II and III are the 'starred' middle states separated by a slip line or contact discontinuity $\frac{dx}{dt} = u^*$. The velocity, u , and pressure, p , are continuous across the contact, but φ in general is not. Thus $u_L^* = u_R^*$, $p_L^* = p_R^*$ and $\rho_L^* \neq \rho_R^*$. $S_{1,b}$, $S_{2,b}$ and $S_{1,f}$, $S_{2,f}$ represent respectively the backward and forward facing waves generated at the point of discontinuity and may be either shocks or rarefaction waves.

Still referring to Fig. 3, it is seen that at a time $n\Delta t < t < (n+1)\Delta t$, the exact solution of the local Riemann problem for the interval $[(i-1)\Delta x]$, $i\Delta x$ may actually consist of several distinct states. Consider now a

translation of each interval $[(i-1)\Delta x, i\Delta x]$ to $\left[-\frac{\Delta x}{2}, +\frac{\Delta x}{2}\right]$ such that the discontinuity (i.e., the point from which the waves are generated) is centered at a zero origin. Let 0 be the value of a random variable, defined over the interval $\left[-\frac{1}{2}, +\frac{1}{2}\right]$, and let

$$\xi = 0\Delta x$$
, i.e. $-\frac{\Delta x}{2} < \xi < +\frac{\Delta x}{2}$

Also, define $U_{\text{exact}}^{n+}(x,t)$, $n\Delta t < t < (n+1)\Delta t$, to be the exact solution to each Riemann problem. Using the value of ξ to fix a point in the interval Δx of each Riemann problem, the exact solution at that point is determined and assigned to either the left or the right grid point, depending on whether ξ is < qr > 0. Thus, if the point fixed by ξ is P' (Fig. 3), the exact solution to the Riemann problem at that sampled location is assigned to the grid point on the right and if the sampled point is P", the solution at that location is assigned to the grid point on the left, i.e., for a typical interval [(i-1)\Delta x, i\Delta x],

if
$$\xi < 0$$
, $U_{i-1}^{n+1} = U_{exact}^{n+}$ (ξ , t)
and if $\xi > 0$, $U_{i}^{n+1} = U_{exact}^{n+}$ (ξ , t)

It is seen immediately that although the solutions are computed on a grid in this method, it is not a differencing scheme. Also, instead of using a weighted average of the Riemann problem solution to arrive at the solution for a grid point[†], the RCM samples a particular value from an explicit wave [†] The Godunov method, for example implements

$$U_{i}^{n+1} = \frac{1}{\Delta x} \int_{(1-\frac{1}{2})\Delta x}^{(1+\frac{1}{2})\Delta x} U_{exact}^{n+} (x,t)dx$$

solution, thus eliminating the smoothing out of wave transport and interaction information inherent in averaging. This leads to the 'infinite' resolution of contact discontinuities and shocks that the scheme displays.

From the foregoing discussion, it is evident that the success of the scheme hinges, to a large extent, on the inexpensive and exact solution of Riemann problems and an appropriate sampling technique. Ref. (3) describes a modification to an iterative method due to Godunov (Ref. 5). Theoretical details for the Riemann problem solution are also given in Ref. (6).

The mathematical properties required in a sampling procedure applicable to this scheme are defined in Ref. (1). A brief description of the procedure is given below.

In previous computations using the RCM, random sampling with some variance reduction technique (stratified sampling); was used, i.e., the values were taken from the random number generator installed in the computer (Ref. 3). It was shown in Ref. (1) that a more accurate form of sampling is a technique due to van der Corput (Ref. 7). The sequence generated is, strictly speaking, non-random, but has particular statistical properties that are suitable to the application. The sequence is referred to as quasirandom and is generated as follows:

The binary expansion of natural numbers may be expressed as (with R=2):

 $n = A_0 R^0 + A_1 R^1 + A_2 R^2 + \dots + A_m R^m , \quad (0 \le A_k < R)$ i.e. $n = \sum_{k=0}^{m} A_k \cdot 2^k , \text{ with } A_k = 0 \text{ or } 1 , \quad n = 1, 2, 3, \dots$

Next, the digits of the binary numbers are reversed and a decimal point is put preceding the number; this gives the numbers

$$\phi_{n} = A_{0}R^{-1} + A_{1}R^{-2} + \dots + A_{m}R^{-(m+1)}$$

or,
$$\phi_{n} = \sum_{k=0}^{m} A_{k} \cdot 2^{-(k+1)}$$
, again with $A_{k} = 0$ or 1

Conversion to the decimal scale of these numbers yields the required sequence of quasirandom numbers defined over the interval [0,1], i.e.,

> $\phi_n \text{ (decimal)} = \Theta_n + \frac{1}{2}$ or $\Theta_n = \phi_n \text{ (decimal)} - \frac{1}{2}$

and $\xi_n = O_n \cdot \Delta x$ as defined earlier.

The first few elements of the sequence given below illustrate the construction =

(decimal)	=	<pre>l (binary);</pre>	ψı	=	0.1 (binary)	=	0.5 (decimal)
-		10	. 1		0.01		0.25
		11			0.11		0.75
		100			0.001		0.125
		101			0.101		0.625
		110			0.011		0.375
		111			0.111		0.875
		1000			0.0001		0.0625
					•		
					•		
	(decimal)	(decimal) =	<pre>(decimal) = 1 (binary);</pre>	(decimal) = 1 (binary); ψ ₁ 10 11 100 101 110 111 1000	$(decimal) = 1 (binary); \psi_1 = 10 \\ 11 \\ 100 \\ 101 \\ 110 \\ 111 \\ 1000 \\ . \\ . \\ . \\ . \\ . \\ . \\ . \\ . \\ . $	$\begin{array}{llllllllllllllllllllllllllllllllllll$	$\begin{array}{llllllllllllllllllllllllllllllllllll$

The van der Corput sequence is 'equidistributed', and yields better results than those obtained using a 'stratified' random sampling technique.

The subroutine employed in the program to compute the random numbers is described in Appendix B.

2.2. Boundary Conditions

In general, the implementation of boundary conditions in the RCM is quite straightforward, but does require some thought. Referring to Fig. 2, the b.c.'s are specified at points 1 and N for the left and right boundary respectively. Note that if the sampled solution at $(n+1)\Delta t$ corresponds to a random number $\xi_n < 0$, the solution is assigned to the grid point on the left. For the Riemann problem defined by points 1 and 3, the sampled solution would then be assigned to grid point 1 at $(n+1)\Delta t$; however this is overridden by assigning the proper boundary condition at 1 again, and there is no contradiction. A similar procedure is adopted at the right hand boundary when $\xi_n > 0$.

The subroutines for the boundary conditions are named in the format BCxn , BC standing for <u>B</u>oundary <u>C</u>ondition, x being either L (for <u>L</u>eft), or R (for <u>R</u>ight boundary) and n being a number from 1 to 5 with the following designations:

- l solid wall condition
- 2 outflow at constant static pressure
- 3 special formulation ('piston' inflow)
- 4 isentropic inflow from reservoir
 - 5 special formulation (rarefaction wave cancellation)

2.2.1. Solid Wall Conditions

The solid wall boundary condition requires a zero normal velocity at the wall for inviscid flow computations. Due to the random sampling involved in the method and the lateral movement of the sampled solution $\frac{\Delta x}{2}$ to the left or right of the discontinuity, the condition is difficult to implement uniquely. However, the procedure adopted here is found to yield reasonably accurate results for the applications intended. (Note that the difficulty is not unique to this method only. The implementation of zero mass flux through a surface is difficult per se for the Euler equations).

Referring to Fig. 2, let the physical boundaries be at point 2 and

point (N-1) for the left and right sides respectively. However, the boundary conditions are specified at point l (point N) for the left (right) side as a fictitious 'mirror' state of the conditions at point 3 (point (n-2)) respectively, but with the reverse sign taken for the velocity component. Thus, for the left hand boundary Riemann problem,

$$P_L = p(3)$$
, $\rho_L = \rho(3)$, $u_L = -u(3)$
 $p_R = p(3)$, $\rho_R = \rho(3)$, $u_R = u(3)$

and, analogously, for the right hand boundary Riemann problem.

$$p_L = p(N-2)$$
, $p_L = p(N-2)$, $u_L = u(N-2)$
 $p_R = p(N-2)$, $p_R = p(N-2)$, $u_R = -u(N-2)$

The solutions are then sampled in the manner outlined earlier.

2.2.2. Outflow Conditions

For subsonic outflow, only the static pressure p is defined, with the continuation condition being applied to the rest of the variables. Thus, for the right hand boundary for example, the Riemann problem is defined as follows:

$$p_L = p(N-2)$$
, $\rho_L = \rho(N-2)$, $u_L = u(N-2)$
 $p_R = p_{out}$, $\rho_R = \rho(N-2)$, $u_R = -u(N-2)$

where p_{out} is the specified outlet pressure. If the flow going out is supersonic, there can be no propagation of disturbances upstream, and the continuation condition is implemented for all the variables, i.e., the Riemann problem now is the trivial case defined by

$$p_{L} = p(N-2) , \rho_{L} = \rho(N-2) , u_{L} = u(N-2)$$
$$p_{R} = p(N-2) , \rho_{R} = \rho(N-2) , u_{R} = -u(N-2)$$

2.2.3. Special Formulation of 'Piston' Inflow

In general, for idealized wave rotor flows, hot combustion gases are

introduced into the rotor through nozzles angled such as to allow the flow to 'slip onto' the rotor, i.e., without incurring incidence or deviation angle losses. Also, in the ideal treatment, the air in the passages of a wave rotor is exposed to the hot gas at high pressure instantaneously. The idealizations allow for uniform conditions to be prescribed at the hot gas inlet port. Thus, a 'special' form of inflow boundary condition needs to be specified here, namely, the static pressure, the velocity and the density of the incoming hot gas. Although equivalent to specifying the total pressure and temperature in the usual inflow boundary condition treatment, some thought is required in wave rotor type flows when specifying $p_{
m gas}$, $ho_{
m gas}$ and $u_{
m gas}$. This is because only a shock wave needs to be generated, with no waves travelling opposite to the direction of flow. The solution to the Riemann problem would then consist of just two states connected by a single shock wave. The flow is equivalent to that generated when a piston is pushed instantaneously into a gas at rest. In general, the state of the air inside the rotor passage is known; explicit relations for two states connected through a shock wave are given in Ref. (6). These so-called transition functions help in specifying the boundary conditions for the incoming flow properly.

If we consider the left boundary for this inflow, the Riemann problem is set up as:

$$PL = Phot gas$$
, $\rho L = \rho hot gas$, $uL = u hot gas$
 $PR = p(3)$, $\rho R = \rho(3)$, $uR = u(3)$

with p_L , ρ_L and u_L having been chosen in accordance with the considerations discussed above.

2.2.4. Isentropic Inflow From Reservoir

The induction of fresh charge or air onto the rotor usually corresponds to an isentropic inflow situation. The flow in the vicinity of the passage end can be treated as quasi-steady, with the assumption that no flow separation takes place when the flow enters. Two boundary conditions are required for this type of inflow; these are provided by the conservation of energy in the flow from the external region to the inlet (assumed to be steady), and by the prescibed entropy level of the gas in the external region.

The boundary conditions may thus be expressed as

$$u_{in}^{2} + \frac{2}{\gamma - 1} a_{in}^{2} = \frac{2}{\gamma - 1} a_{tot}^{2}$$
$$S_{in} = S_{tot}$$

where the subscripts 'in' and 'tot' apply to conditions at the inlet of the passage and external reservoir respectively. The sonic velocity is denoted by a , and flow velocity by u . Note that knowledge of the Riemann variable arriving at the passage end from within the passage is required to be able to solve the energy equation above for a_{in} and u_{in} . For the left end, for example,

$$Q_{in} = \frac{2}{\gamma - 1} a_{in} - u_{in}$$

which together with the energy equations yields

$$a_{in} = \frac{Q_{in} + \sqrt{\frac{\gamma+1}{\gamma-1}} a_{tot}^2 - \frac{\gamma-1}{2} Q_{in}^2}{\frac{\gamma+1}{\gamma-1}}$$

and subsequently the other variables.

The simple analytical treatment given above has to be modified somewhat if a contact discontinuity is formed when the inflow begins. This is due to the fact that the value of the arriving Riemann variable is changed across such a discontinuity, which thus leads to an additional unknown. Procedures for solving the inflow for these situations are given in Ref. (8). In the program developed here, reasonably good results are obtained by setting the velocity at the boundary point equal to the velocity at the point nearest the physical boundary. For the left end e.g., the variables for the left state of the Riemann problem are obtained as follows:

$$u(1) = u(3)$$
,

a reasonably accurate assumption just at the point of inlet opening.

Then, from the 'energy ellipse',

$$a(1) = \sqrt{a_{tot}^2 - \frac{\gamma - 1}{2} u(1)^2}$$

 $M(1) = \frac{u(1)}{a(1)}$, incoming Mach number

$$p(1) = \frac{Ptot}{[1+\frac{\gamma-1}{2} M(1)^2]} \gamma/(\gamma-1) ,$$

with similar isentropic relations to compute other flow variables. Note that once the interface or contact discontinuity has moved a certain distance inside the passage, the simple analytical expressions given earlier in the section can be used, since now the value of the arriving Riemann variable would be known at the boundary.

2.2.5. Special Formulation for Rarefaction Wave Cancellation

The spreading of rarefaction fans leads to unwanted wave reflections

which occupy large zones in the passages of wave rotors. Fig. (4) shows a wave diagram proposed by Spectra Technology, Inc., which incorporates so-called 'wave management' or 'tuning' ports to ideally cancel (and otherwise attenuate) impinging rarefaction fans. The physical boundary conditions are thus dictated by the flow developing in the passage, i.e., the port has non-uniform flow conditions in it, which at each point match those of the flow at the end of the passage so as to disallow any reflections to take place. Numerically, this condition is achieved by implementing the continuity condition across the boundary for all the flow variables involved. For the left boundary, thus, the Riemann problem is defined by:

$$p_L = p(3)$$
, $\rho_L = \rho(3)$, $u_L = u(3)$
 $p_R = p(3)$, $\rho_R = \rho(3)$, $u_R = u(3)$

and analogously for the right boundary. Note that these boundary conditions may involve either inflow or outflow.

2.3 Example Calculations

The listing of the program is included in Appendix A, and the various names for the variables are listed in Appendix B, along with some instructions on how to use the program. No effort as yet has been made to optimize the code either for storage requirements or for execution efficiency.

In this section, some sample calculations are carried out using the code, to illustrate its usefulness in constructing idealized design point wave diagrams which can serve as the starting configuration for detailed construction of diagrams incorporating real flow effects.

2.3.1. Test Case for 1-D, Inviscid, Unsteady, Compressible Flow

Fig. (1) illustrates the initial conditions in a shock tube, with the diaphragm at x_0 . Sod (Ref. 9) suggested a test case for hyperbolic

conservation laws with the following conditions as initial states in the shock tube:

$$p_1 = 1.0$$
, $p_1 = 1.0$, $u_1 = 0.0$
 $p_5 = 0.1$, $p_5 = 0.125$, $u_5 = 0.0$

i.e., the gas on either side of the diaphragm is in a quiescent state initially. The ratio of specific heats is chosen to be 7/5, and Δx is chosen to be 0.01.

The solution (before any wave has reached either the left or right end) is shown in Fig. (5). The squares shown at locations x_1 , x_2 , x_3 and x_4 in the density plot give the analytically calculated amplitude and location of the head - and tail waves of the left-running rarefaction, the contact surface moving to the right and the shock wave moving at supersonic velocity to the right respectively. The solid lines are the solutions obtained by the RCM at different time levels; the zero numerical diffusion feature of the method is evident in the 'infinite' resolution of the contact discontinuity and the shock, and the dispersion (phase error) is within one grid spacing. The constant states are perfectly realized.

It is these features of the method that make it very attractive for application to wave rotor type flows, since the successful design of the device is predicated on being able to accurately compute wave arrival times at the various ports.

2.3.2. Wave Turbine Experiment

Ref. (10) describes the wave rotor experimental set up at the Turbopropulsion Laboratory. Initial tests being carried out currently are with the wave rotor in a turbine mode, i.e., one side of the rotor is blocked off, and high pressure air is brought onto the rotor and taken off again from

the other side. The passages of the rotor being angled at 60° to the axis, the 180° reversal in the direction of the fluid flow creates an angular momentum change, in turn generating large turbomachinery work coefficients. Fig. (6) shows the wave diagram computed using the code. The movement of the rotor is from top to bottom. At t=0, the high pressure air is brought into contact with quiescent atmospheric air in the rotor passages, at point a. This corresponds to the 'piston' inflow boundary condition described in section 2.2.3.. A shock, S , is generated immediately, (idealized case of instantaneous cell opening), which travels from the right to the left, and strikes the solid wall at the left end. The reflection of the shock takes place at point b according to the solid wall boundary condition described in section 2.2.1.. Behind this shock, and moving at a slower velocity is the contact surface, I, which penetrates into the passage only a fractional distance before encountering the reflected shock, RS, at point c. The reflected shock is transmitted through the contact surface, (bringing the flow to a near halt), and reaches the right side at point d, whereupon the inlet port is closed. The air trapped in the rotor passages is now at a high pressure and in a quiescent state. When this air is released at point e to a low pressure region, a rarefaction wave is generated, R, which travels to the left, spreading out in the process. It interacts with the stationary contact surface, I, setting it into motion again, and reflects off the solid wall at the left as RR . The boundary condition imposed at point e is the outflow at constant static pressure condition described in section 2.2.2... The outlet port is closed at a time when the exit velocity falls to about half its initial value.

This experiment embodies two fundamental processes in wave rotors: those of cell filling and cell emptying. Almost all the other processes

typical to wave rotors are combinations of the cell filling and cell emptying unit processes. Comparison of the ideal computed numbers obtained here with experimental data will provide information helpful in the identification and sources of losses.

The program is set up to start at t=0 in this case, with initial data provided along the entire passage, i.e., from x=0 to x=0.1863m (the actual length of the wave rotor being tested). Since the passages have quiescent atmospheric air in them at t=0, the initial data, of course, describes these conditions. Switches for the left and right boundaries describe what type of boundary conditions prevail and direct the program to the appropriate subroutines. These switches, designated SWL and SWR , for left and right respectively, are assigned integer number values which correspond to the numeric value of the particular boundary condition they represent. Thus, if the left boundary is a solid wall, SWL=1 , corresponding to the boundary condition subroutine BCLl . In this example then, the initial switch settings at t=0 are SWL=1 and SWR=3 , corresponding to a solid wall at the left and a 'piston' inflow at the right (which starts at t=0 at point a). At point d , the switches are reset to SWL=1 and SWR=1 due to the closure of the inlet port. At point e, the switches are SWL=1 , SWR=2 , signifying opening of the exhaust port with outflow at a constant static pressure. The whole wave diagram can thus be packaged into a 'module' subroutine and called from the main program with a single call statement. This type of modularity allows for wave diagrams of different 'families' to be developed by simply calling the right 'module' subroutine.

The next two examples illustrate this concept as they deal with two very different types of wave diagrams.

2.3.3. General Electric Wave Engine

Fig. (7) shows a schematic of the wave diagram constructed for the G.E. wave engine. Briefly, the device is configured for a gas generator mode of operation, with counterflow scavenging, and is capable of producing net shaft power. For a fuller description of the machine, see Ref. (11). In this example, fresh charge (air) is induced into the rotor (from an external reservoir) through the wave action of the rarefaction fan originating at the exhaust port opening. The usefulness of the rotor is gauged by the net pressure rise across the machine, i.e., the ratio of the total exhaust ports of total (fresh air) inlet pressure.

For performance estimation purposes, it is sufficient to investigate only the exhaust and induction processes as shown in Fig. (8). The initial data specified is as follows: the exhausting pressure ratio p_e/p_0 , the total pressure ratio across the rotor p_{te}/p_{ta} and an assumed total temperature ratio T_{te}/T_{ta} . In this particular cycle, the amount of fresh charge induced in is ideally equal to the gases exhausted out, i.e., $m_{in} = m_{out}$, and this mass balance is carried out after each computation to correct the assumed temperature ratio T_{te}/T_{ta} (which otherwise constitutes overspecification of the initial conditions).

The calculation starts at t=0 , with initial data consistent with the chosen pressure and temperature ratios specified along the passage length. Initial switch settings are SWL=1 and SWR=2 for the solid wall boundary at the left and the exhaust to a constant pressure at the right. As shown in the figure, a rarefaction fan is generated, propagating to the left and reflecting off the solid wall. At time $t=\tau_1$, the pressure at the wall has been reduced to that outside the passage, p_{ta} , which is when the inlet port is opened. The switches are now set to SWL=4 and SWR=2 for isentropic inflow

from an external reservoir at the left, and still outflow at a constant pressure at the right. The exhaust port is closed at time $t=\tau_2$ which corresponds to the exit velocity having dropped off to approximately half its steady state value at the beginning of the exhaust process. Now the switches are set to SWL=4 and SWR=1 , for the solid wall condition at the right. The sudden closure of the exhaust port generates a 'hammer' shock travelling to the left, interacting with the incoming interface (shown by dashed line), and reaching the passage end at $t=\tau_4$ at which time the inlet port is closed, with the switches being reset to SWL=1 and SWR=1 . Note the reflected shock travelling from left to right generated at the interaction of the contact surface and the hammer shock.

Once this solution is obtained, integration of the mass flux through the inlet and exhaust ports is carried out and if the two numbers do not match, the assumed temperature ratio T_{te}/T_{ta} is adjusted in the initial data, till such time as $m_{in} = m_{out}$.

This calculation is sufficient for performance analyses: if the entire wave diagram has to be worked out, then at a time $t > r_3$, hot gas from the combustion chamber is brought onto the rotor (the boundary condition corresponding to 'piston' inflow) on the right hand side. This would generate the shock to compress the induced air and when this shock reached the left end, the transfer port (see Fig. 7) would be opened for such time it takes for the compressed air to be completely scavenged out of the rotor. Fig. (9) shows some performance curves obtained using the procedure outlined above. In Figs. (10a, b, c) are shown three sets of flow parameters at different time steps corresponding to the inlet port just opening, the exhaust port closing and the inlet port closing; the qualitative distributions of the flow parameters in the passage are immediately seen to be accurate when

compared with the wave diagram shown in Fig. (8). Of interest is the set of plots for the time step when the inlet port has just been closed. The flow between the end of the passage and the location of the interface is seen to be quite non-uniform in the density plot. At the same time, the shock reflected from the interface has reached the right side and reflected off the solid wall. These considerations help to decide optimum port opening and closing times. For example, Fig. (11) shows what happens if the inlet port is not closed at just the time the shock reaches the end, but rather at some short time later. The shock now sees an open boundary and reflects off as an expansion to match the high pressure behind it with the incoming total pressure which is at a lower value. This reflected expansion is manifested in the pressure, density and velocity plots of the figure.

The entire sequence of wave interactions of this example is computed by the RCM without the implementation of artificial viscosity or artificial compression methods, or tracking and capturing schemes. This 'hands off' feature of the method renders it eminently useful for fast preliminary evaluations of complex wave diagrams for the application at hand.

The next example computes an idealized wave diagram for the nine-port pressure exchanger concept proposed by Spectra Technology, Ref. (12).

2.3.4. Spectra Technology Pressure Exchanger

Fig. (4) shows the ideal wave diagram for the nine-port pressure exchanger. This configuration is a good case example to compute with the RCM because of the different types of boundary conditions that need to be dealt with in the evaluation of the cycle. The computation is started at t=0, at the point of high pressure hot gas inlet (driver gas inlet). In the manner described in the G.E. wave engine example, the initial data is prescribed for

the entire passage at this time step and the boundary condition switches are initially set at SWL=1 and SWR=3 for the solid wall at the left, and the 'piston' inflow at the right hand end. Since there is a multiplicity of types of boundary conditions, e.g., three outflow ports, an index, JCOUNT, is used to ensure proper sequencing of the switches. The following table is presented as an example of the settings of the switches to carry out calculations for one cycle. The inflow and outflow port conditions are those proposed by Spectra Technology for their idealized diagram.

TIME STEP, N	JCOUNT	SWL	SWR	REMARKS
0	0	1	3	CYCLE STARTS. HP GAS INLET PORT OPENS
500	1	2	3	HP AIR OUTLET PORT OPENS
1408	2	2	1	HP GAS INLET PORT CLOSES
1765 -	3	5	1	HP AIR OUTLET PORT CLOSES. TUNING PORT L1 OPENS
1816	4	2	1	TUNING PORT L1 CLOSES. IP GAS OUTLET PORT OPENS (PORT E1)
2069	5	2	5	TUNING PORT R1 OPENS
2261	6	2	1	TUNING PORT R1 CLOSES
2595	7	5	1	IP GAS OUTLET PORT CLOSES. TUNING PORT L2 OPENS
2636	8	2	1	TUNING PORT L2 CLOSES. LP GAS OUTLET PORT OPENS (PORT E2)
3029	9	2	5	TUNING PORT R2 OPENS
3237	10	2	4	TUNING PORT R2 CLOSES. LP AIR INLET PORT OPENS
4961	11	1	4	LP GAS OUTLET PORT CLOSES
5529,0	0	1	3	LP AIR INLET PORT CLOSES. CYCLE COMPLETED

The total cycle time as calculated by the RCM is 3.0676 mseconds, which compares well with the time computed by Spectra Technology (using the FCT-SHASTA algorithm) of 3.07 mseconds. The execution time on an IBM 370-3033AP for the 5529 steps computed in the example above was 3 minutes 38 seconds, including the I/O operations and the graphics.

Figs. (12a, b, c) show three sets of plots of the flow parameters for the following cases: a) the H.P. air outlet port opens on time, i.e., just as the shock reaches the left end of the passage, b) the port opens before the shock has reached the end, and c) the port opens after the shock has reached the end. The constant pressure and velocity states that prevail in the passage just after the shock has reached the left end (time 'section' line T in wave diagram), are perfectly realized in Fig. (12a), while the contact surface is at the location shown by the sharp discontinuities in the density and entropy plots. Should the inlet port be opened earlier, e.g., at the time level shown by τ_{1-} in the wave diagram, what happens is as follows: the pressure in the passage is still at the pre-compressed level and this comes into contact with the pressure level in the port which is considerably higher, resulting in a shock propagating into the passage, colliding with the left moving shock and raising the overall pressure level to ~ 3.0 as shown in Fig. (12b). However, as soon as the left moving shock reaches the end, it now encounters an open boundary with conditions that do not match those behind the shock, resulting in a rarefaction fan being generated, which propagates to the right. This expansion fan, travelling at sonic velocity relative to the gas into which it is propagating, soon overtakes the right moving shock which is travelling at a subsonic velocity relative to the same gas. This interaction results in an attenuation of both the rarefaction as well as the shock wave. Note that the overall pressure and velocity levels behind the rarefaction are about the same as for case a), i.e., the effects of the mismatch are not very significant at the outlet port. However, should the right moving pressure perturbations of case b) not attenuate each other significantly before they reach the right hand end, the consequences could be severe for the overall wave diagram, since this will lead to further (unwanted) wave reflections.

Fig. (12c) shows what occurs if the outlet port is opened too late, corresponding to time level τ_{1+} on the wave diagram. Now the left travelling shock encounters a wall boundary condition on reaching the left end and reflects off as a shock, effectively doubling the pressure level behind it (>3.5 in pressure plot of Fig. (12c)). When the outlet port opens, there is again a mismatch of conditions in the port and in the passage, with the pressure level in the passage being considerably higher than that prescribed for the outlet port. A rarefaction wave is generated which propagates to the right and overtakes the reflected shock. The same criterion holds for this case too, i.e., the ensuing attenuation of these pressure pulses should occur before they reach the right hand end, preferably even before they reach the interface still propagating towards the left at the flow velocity.

The considerations above give a preview of the nature of decisions required in the successful design of a wave rotor device. It is clear that quite a few iterations are involved in the process of designing a viable wave diagram for a particular application, and each iteration entails calculating two or more complete cycles to ensure 'closure' or repeatability of the cycle. A fast solver like the RCM allows reaching an idealized 'base' design quickly and inexpensively.

Appendix A is a listing of the program in its present development stage. As mentioned earlier, no attempt has been made to optimize the program, either for storage requirements or for execution.

Appendix B gives a description of the structure of the program, a listing of the important variables, the subroutines and the function subprograms. A step by step guide is also included to set up and run the program.

3.1. Discussion

For meeting the criteria listed in the Introduction, in one dimension, Glimm's method or the RCM appears to be superior to any difference method. For wave rotor type applications, where discontinuities need to be computed with sharpness, the 'infinite' resolution of such discontinuities inherent in the RCM make it a natural choice to carry out ideal flow calculations for preliminary design purposes. Boundary conditions can be implemented quite easily and do not require information from points outside the domain of dependance as is the case in some finite difference schemes. The van der Corput sampling technique results in the best possible representation of the wave propagation, which is essential for the correct representation of continuous waves, particularly those produced by nonlinear interactions.

The method, however, is not recommended to solve for flows with real effects such as friction, heat transfer and area change, or to be extended to multi-dimensional flows. Although considerable research is being done to rigorously extend the method to such flows, with some degree of success (see Refs. 1, 4, 13), the present state of development is not mature enough to ensure a useful practical code as the outcome.

3.2. Recommendations

Many options are available for one wishing to develop either a I-D code with real effects and/or a multi-dimensional code for wave rotor type applications. The author prefers to recommend numerical formulations which are dependent on the solution of Riemann problems, such as the Godunov method; the motivating reason for this preference is that a Riemann problem constitutes the solution of a discontinuity in the flow in terms of other

discontinuities (if any are, indeed, present), and the scheme is thus intrinsically suited for solving such flows; on the other hand, the other schemes, in general, require to be made aware of discontinuities in the flow through some external device, and then treat them through other artificial devices.

A second-order, quasi one-dimensional (variable cross-sectional area) scheme has recently been developed by Ben-Artzi and Falcovitz (Ref. 14). The method is based on the exact solution of 'generalized Riemann propblems', and has demonstrated very good results; it's least accurate approximation is equivalent to Godunov's first order method (Ref. 9). The resolution of shocks and other disconitinuities and singularities of the flow field is also high. Extension to more than one dimension appears to be straightforward through the use of operator splitting techniques, but has as yet not been tried extensively.

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SPECIAL CASE OF SHOCK-TUBE FLOW


O- intermediate grid points BC- points where boundary conditions are

X- location where local Riemann Problem solution is sampled specified





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Fig.4 : Ideal Nave Diagram for Pressure Exchanger (Spectra Technology). I.P. IP. HP: Low, Intermediate, High Pressure

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Wave Diagram Computed by 1-D Random Choice Method. S--Shock; RS--Reflected Shock; R--Rarefaction Fan; RR--Reflected Rarefaction; I--Interface;

Figure 6.



Fig.7 : Ideal Wave Diagram for General Electric Wave Engine



Fig.8 : Gas Exhaust and Fresh Air Induction Process in G.E. Wave Engine



Fig.9 : Ideal Performance Curves for G.E. Wave Rotor as Gas Generator

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Fig.ll : Distribution of Flow Parameters in Rotor Passage When Inlet Port Closes Late, i.e. After Arrival Of Shock. N= 1700.



Fig.12 a : Distribution of Flow Parameters in Rotor Passage when the H.P. Air Outlet Port Opens on Time.





: H.P. Air Outlet Port Opens Late

J

: H.P. Air Outlet Port Opens Prematurely

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APPENDIX A

Listing of Program RCM

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PROGRAM RCM WITH VAN DER CORPUT SAMPLING AND SINGLE TIME STEP RCM00030 INTEGER QPRINT, QSTOP, SWL, SWR RCM00040 DIMENSION XX(6), YY(6) RCM00050 DIMENSION XARRAY(100) RCM00060 DIMENSION WNORM(12), IDIGT(12) RCM00070 DIMENSION P(203), R(203), U(203), A(203), S(203), X(203)RCM00080 COMMON/SUBS/P.R.U.A.S.X RCM00090 COMMON/GLIMM1/PGLIM, RGLIM, UGLIM, PL, RL, UL, PR, RR, UR, AL, AR, GL, GR, EPS RCM00100 COMMON/GLIMM2/DT, DX, XI RCM00110 COMMON/FUN1/G, PA, RA, UA, RB, RMU RCM00120 COMMON / SAMPLE / WNORM. IDIGT RCM00130 COMMON XARRAY, N1 RCM00140 CALL COMPRS RCM00150 CALL BLOWUP(0.5) RCM00160 CALL PAGE(11.0.8.5) RCM00170 CALL HWSCAL('SCREEN') RCM00180 DATA K, SWL, SWR/500, 1, 3/ RCM00190 DATA N, CFLNUM, TTOTAL/0,0.60,0.0/ RCM00200 DATA PSEXIT, PSINL, PSINR, RINL, RINR/116954., 3770000., 3819952.50, 6.8, RCM00210 *6.800/ RCM00220 DATA PSOUT1, PSOUT2, PSOUT3/3819952.5, 2431800.0, 1530007.5/ RCM00230 DATA PTOTIN, RTOTIN/1656663.8, 7.486/ RCM00240 DATA PREF, RREF, XREF/1656663.8, 7.486, 0.1800/ RCM00250 G=1.4 RCM00260 GL=1.4 RCM00270 GR = 1.4RCM00280 EPS=1.E-06 RCM00290 OSTOP=20RCM00300 N1 = 0RCM00310 JCOUNT=0 RCM00320 RCM00330 KCOUNT=0UEXMAX=0. RCM00340 DX = 0.01RCM00350 AREF = SORT (PREF / RREF) RCM00360 RCM00370 TIMREF=XREF/AREF RMU = SQRT((G-1.)/(G+1.))RCM00380 RCM00390 X(1) = -0.5 * DXZETA=WDP(1) RCM00400 XII=DX*(WDP(0)-0.5)RCM00410 DO 25 I=2,203RCM00420 X(I) = X(I-1) + 0.5 * DXRCM00430 25 CONTINUE RCM00440 DO 35 I=1,100RCM00450 XARRAY(I) = X(I*2+1)RCM00460 RCM00470 **35 CONTINUE** RCM00480 INITIAL DATA CALL INIT1 RCM00490 CALL INIT2L(PSEXIT) RCM00500 CALL INIT2R(PSEXIT, PREF, RREF) RCM00510 CALL INIT3L(PSINL,RINL) RCM00520 CALL INIT3R(PSINR, RINR) RCM00530 NONDIMENSIONALIZATION RCM00540 DO 30 I=1,203,2 RCM00550 P(I) = P(I) / PREFRCM00560



	R(I) = R(I) / RREF	RCMU
	$\mathbf{U}(\mathbf{T}) = \mathbf{U}(\mathbf{T}) / \mathbf{A} \mathbf{P} \mathbf{F} \mathbf{F}$	RCMC
		DCMC
	A(1)=A(1)/AREF	RUMU
	S(I) = ALOG(P(I)/R(I) * G)	RCMC
30	CONTINUE	RCMC
50		DOMO
	CALL PLOTI(K)	RUMU
	DO 40 J=1,K	RCMC
	N = N + 1	RCMC
	$\mathbf{N} = \mathbf{N} \cdot \mathbf{I}$	DCMC
	X11=DX*(WDP(0)-0.5)	KOM
	QPRINT=N/50	RCMU
	DT = 100.	RCMC
	DO 50 T-1 203 2	RCMC
	D = (1, 2, 0)	DOM
	DTT=CFLNUM*DX/(2.*AMAXI(ABS(A(1)+U(1)),ABS(A(1)-U(1))))	RCMU
	DT=AMIN1(DTT,DT)	RCMC
50	CONTINUE	RCMC
50		DCMC
	ITOTAL=ITOTAL+DI	RUMU
	TIME=TTOTAL*TIMREF	RCMU
	XT = - XTT	RCMC
		PCMC
	$D_{0} = 0$ [=1,201,2	ROM
	PL=P(I)	RCMU
	RL=R(I)	RCMC
		RCM
		DOM
	PR=P(1+2)_	RUMU
	RR=R(I+2)	RCMC
	IIR = II(T+2)	RCMC
		PCMC
		RONG
	IF(I.EQ.I) XI=ABS(XI)	RCMU
	IF((I.EO.201).AND.(XI.GT.0.0)) XI=-XI	RCMC
	CALL GLIMM(OSTOP PSTAR USTAR ÁSTAR)	RCMC
		P.CM(
		KOM
	P(I+1)=PGLIM	RCMU
	R(I+1)=RGLIM	RCMC
		RCM
60		DOM
60	CONTINUE	RUMU
	DO 70 I=1,201,2	RCM
	TF(XI, LT, 0,) GOTO 80	RCMC
	P(T,2) = P(T,1)	PCMC
	$\mathbf{r}(1+\mathbf{Z}) - \mathbf{r}(1+1)$	KOPIC
	R(I+2) = R(I+1)	RCMU
	U(I+2) = U(I+1)	RCM
	$A(T+2) = SORT(C \times P(T+2)/P(T+2))$	R CM(
	$\frac{1}{2} \left(\frac{1}{2} \right) - \frac{1}{2} \left(\frac{1}{2} \right) - \frac{1}$	DCM
	$S(1+2) = ALOG(P(1+2)/R(1+2)^{A}G)$	RUM
	GOTO 70	RCM(
80	P(T) = P(T+1)	RCM()
	P(T) - P(T+1)	PCM
	K(1) - K(1+1)	ROI K
	U(1)=U(1+1)	RCM(
	$A(I) = SQRT(G^*P(I)/R(I))$	RCM(
	$S(T) = ATOC(P(T))/R(T) \times C$	R CM(
70		DCM
10		RUMI.
	CALL GE(SWL,SWR,N,TTOTAL,TIME,UEXMAX,PTOTIN,PREF)	RCM(
	CALL DETON(SWL,SWR,N,OPRINT,TTOTAL,TIME)	RCM(
	CALL SPOTRA (N SWL SWR TIME HEYMAY DEEXIT DECUTT DECUTT DECUTT	RCM
	COLUTION TANK, THE, CANAR, TSEATT, TSUTT, TS	DOM.
	ACOUNT, QPRINT, TIUTAL, KOUNT)	RCMI.
	IF(SWL.EQ.1) CALL BCL1	RCM(
	IF (SWL, EO, 2) CALL BCL2 (PSEXIT, PREF)	RCM

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IF(SWL.EO.3) CALL BCL3(PSINL, RINL, PREF, RREF) RCM01110 IF(SWL.EQ.4) CALL BCL4(PTOTIN, RTOTIN, PREF, RREF) RCM01120 IF(SWL.EO.5) CALL BCL5 RCM01130 IF(SWR.EQ.1) CALL BCR1 RCM01140 IF(SWR.EQ.2) CALL BCR2(PSEXIT, PREF) RCM01150 IF(SWR.EO.3) CALL BCR3(PSINR,RINR,PREF,RREF) RCM01160 **IF(SWR.EQ.4)** CALL BCR4(PTOTIN, RTOTIN, PREF, RREF) RCM01170 IF(SWR.EO.5) CALL BCR5 RCM0118C IF $((N, EO, (50 \times OPRINT)), AND, (N, GE, O))$ CALL PLOT2(N,K) RCM01190 **40 CONTINUE** RCM01200 CALL ENDPL(0) RCM01210 CALL DONEPL RCM01220 STOP RCM01230 END RCM01240 SUBROUTINE GLIMM(QSTOP, PSTAR, USTAR, ASTAR) RCM01250 INTEGER Q,QSTOP RCM01260 REAL ML, MR, MLN, MRN RCM01270 COMMON/GLIMM1/PGLIM, RGLIM, UGLIM, PL, RL, UL, PR, RR, UR, AL, AR, GL, GR, EPS RCM01280 COMMON/GLIMM2/DT, DX, XI RCM01290 DATA 0,ML,MR/0,100.,100./ RCM01300 PSTAR=0.5*(PL+PR) RCM01310 COEFL=SQRT(PL*RL) RCM01320 COEFR=SQRT_(PR*RR) RCM01330 ALPHA=1. RCM01346 BEGIN GODUNOV ITERATION RCM01350 30 Q=Q+1 RCM01360 **IF(PSTAR.LT.EPS)** PSTAR=EPS RCM01370 COMPUTE NEXT ITERATION FOR ML AND MR RCM01380 MLN=COEFL*PHI(PSTAR, PL) RCM01390 MRN=COEFR*PHI (PSTAR, PR) RCM01400 DIFML=ABS(MLN-ML) RCM01410 DIFMR=ABS(MRN-MR) RCM01426 ML=MLN RCM01430 MR=MRN RCM01446 COMPUTE NEW PSTAR RCM01456 PTIL=PSTAR RCM01460 PSTAR=(UL-UR+PL/ML+PR/MR)/(1./ML+1./MR) RCM01470 PSTAR=ALPHA*PSTAR+(1.-ALPHA)*PTIL RCM0148C IF(Q.LE.QSTOP) GOTO 10 RCM01490 IF(ABS(PSTAR-PTIL).LT.EPS) GOTO 20 RCM01500 COMPUTE NEW ALPHA RCM01510 ALPHA=0.5*ALPHA RCM01520 RCM01530 0 = 0IF((1.-ALPHA).LT.EPS) GOTO 20 RCM01540 10 IF(DIFML.GE.EPS) GOTO 30 RCM01550 IF(DIFMR.GE.EPS) GOTO 30 RCM01560 END OF GODUNOV ITERATION; COMPUTE USTAR RCM01570 20 USTAR=(PL-PR+ML*UL+MR*UR)/(ML+MR) RCM01580 BEGIN SAMPLING PROCEDURE RCM0159(IF (XI.LT.USTAR*DT) GO TO 40 RCM01600 RIGHT SIDE; SELECT CASE OF SHOCK OR EXPANSION RCM01610 IF (PSTAR.LT.PR) GO TO 50 RCM01620 RIGHT WAVE IS A SHOCK WAVE RCM0163C RCM0164C WR=UR+MR/RR

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		IF (XI, LT, WR*DT) GO TO 60	R CMO
C		PICUT OF PICUT SUCCE CASE	PCMO
0			DCMO
		RGLIM- RK	RCMU
		PGLIM=PR	RCMU
		UGLIM=UR	RCMO
		RETURN	RCMO
С		LEFT OF RIGHT SHOCK CASE	RCMO
	60	RGLIM=-MR/(USTAR-WR)	RCMC
		PGLIM=PSTAR	RCMC
			RCMC
			RCMC
~		NETOWN	DCMO
U	50	CONCERNED A RAREFACTION WAVE	RCMU
	50	CUNST=PR/RR**GR	RCMU
		RSTAR= (PSTAR/CONST) ***(1./GR)	RCMC
		ASTAR=SQRT(GR*PSTAR/RSTAR)	RCMC
		AR = SQRT(GR*PR/RR)	RCMC
		IF (XI.GE. (USTAR+ASTAR)*DT) GO TO 70	RCMC
С		LEFT OF RIGHT FAN CASE	RCMC
		RGLIM=RSTAR	RCMC
		LIGLIM=USTAR	RCMC
		PCLIM=DSTAR	RCMC
			DCMC
~		CELECT DICUT OF TAN OF TA FAN	RCMC
L	70	SELECT RIGHT OF FAN OR IN FAN	RUMU
-	/0	IF (XI.GE.(UR+AR)*DT) GU TU 80	RCMC
С		IN RIGHT FAN CASE	RCMC
		UGLIM=2./(GR+1.)*(XI/DT-AR+(GR-1.)/2.*UR)	RCMC
		RGLIM=(((AR+(GR-1.)/2.*(UGLIM-UR))**2.)/(GR*CONST))**(1./(GR-1.)) RCM(
		PGLIM=CONST*RGLIM**GR	RCMC
		RETURN	RCMC
С		RIGHT OF RIGHT FAN CASE	RCMC
	80	RGLIM=RR	RCMC
		PGLIM=PR	RCMC
		UGLIM=UR	RCMC
		RETURN	RCMC
С		LEFT SIDE: SELECT CASE OF SHOCK OR RAREFACTION	RCMC
0	40	IF (PSTAR LT PL) GO TO 90	RCMC
C	10	LET WAVE IS A SUCCE WAVE	PCMC
0		LEFT WAVE IS A SHOCK WAVE	DCMO
			RUMU
~		IF (XI.GE.WL^DI) GO IO IOO	RCMU
C		LEFT OF LEFT SHOCK CASE	RCMU
		RGLIM=RL	RCM
		PGLIM=PL	R CM(
		UGLIM=UL	RCM
		RETURN	RCM(
С		RIGHT OF LEFT SHOCK CASE	RCM
	100	RGLIM=ML/(USTAR-WL)	RCM(
		PGLIM=PSTAR	RCM(
		UGLIM=USTAR	RCM
		RETURN	RCM
C		LEFT WAVE IS A RAREFACTION WAVE	DCM
U	00	CONCT-DI /DI **CI	DCM
	90	$DCMDI = ID/RD^{-1}CDNCM + \frac{1}{2} $	RUMU
		$ASTAR - (FSTAR / UUNST)^{(1)} (L. / UL)$	RUM
		$ASIAK = SUKI(GL^{*}PSIAK/KSIAK)$	RCM
		AL=SQKI(GL^PL/KL)	RCM

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		IF (XI.LT.(USTAR-ASTAR)*DT) GO TO 110	RCM02190
С		RIGHT OF LEFT FAN CASE	RCM02200
		RGLIM=RSTAR	RCM02210
		PGLIM=PSTAR	RCM02220
		UGLIM=USTAR	RCM0223 0
		RETURN	RCM02240
С		SELECT LEFT OF FAN OR IN FAN CASE	RCM02250
_	110	IF (XI.LT.(UL-AL)*DT) GO TO 120	RCM02260
С		IN LEFT FAN CASE	RCM02270
		UGLIM=2./(GL+1.)*(AL+(GL-1.)/2.*UL+XI/DT)	RCM02280
		RGLIM=(((AL+(GL-1.)/2.*(UL-UGLIM))**2.)/(GL*CONST))**(1./(GL-1.))	RCM02290
		PGLIM=CONSI^RGLIM**GL	RCMU2300
~		RETURN	RCM02310
C	120	LEFT OF LEFT FAN CASE	RCM02320
	120		RCM02350
			RCM02340
		PETURN	RCM02350
		FND	RCM02370
		FUNCTION PHI(Y 7)	RCM02380
		REAL RMI	RCM02390
		COMMON/FUN1/G.PA.RA.UA.RB.RMU	RCM02400
		EPS=1, $E=06$	RCM02410
		PARAM=Y/Z	RCM02420
		IF (ABS(1PARAM).GE.EPS) GO TO 10	RCM02430
		PHI=SQRT(G)	RCM02440
		RETURN	RCM02450
	10	IF (PARAM.GE.1.) GO TO 20	RCM02460
		PHI=(G-1.)/2.*(1PARAM)/(SQRT(G)*(1PARAM**((G-1.)/(2.*G))))	RCM02470
		RETURN	RCM02480
	20	PHI = SQRT((G+1.)/2.*PARAM+(G-1.)/2.)	RCM02490
		RETURN	RCM02500
		END	RCM02510
		FUNCTION PHIL(PB)	RCM02520
		REAL RMU	RCM02530
		UMMON/FUNI/G, FA, KA, UA, KD, KMU $DUTI = (DP, DA) \div COPT((1 = DMII \div 2))/(DA \div (DB + DMII \div 2)))$	RCM02540
		$\mathbf{P}_{\mathbf{T}} = (\mathbf{P}_{\mathbf{T}} - \mathbf{P}_{\mathbf{T}})^{*} SQKI((\mathbf{T}_{\mathbf{T}} - \mathbf{M}_{\mathbf{T}})^{*} (\mathbf{K}_{\mathbf{T}} (\mathbf{T}_{\mathbf{T}} - \mathbf{M}_{\mathbf{T}})^{*})$	RCM02550
		FND	RCM02570
		FUNCTION PSI(PB)	RCM02580
		REAL RMU	RCM02590
		COMMON/FUN1/G.PA.RA.UA.RB.RMU	RCM02600
		PSI=SORT(1RMU**4.)/RMU**2./SORT(RA)*PA**(1./(2.*G))*(PB**((G-1.	RCM02610
	,	*/(2.*G))-PA**((G-1.)/(2.*G)))	RCM02620
		RETURN	RCM02630
		END	RCM02640
		SUBROUTINE INIT1	RCM02650
		DIMENSION P(203), R(203), U(203), A(203), S(203), X(203)	RCM02660
		COMMON/FUN1/G,PA,RA,UA,RB,RMU	RCM02670
		COMMON/SUBS/P,R,U,A,S,X	RCM02680
		DO 10 I=1,9,2	RCM02690
		P(I) = 810600.00	RCM02700
		R(1) = 0.7132	RCM02710
		U(1)=644.4	KCMU2720

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A(I) = SQRT(G*P(I)/R(I))
10 CONTINUE
   DO 20 I=11,203,2
   P(I) = 101325.0
   R(I) = 1.22
   U(I) = 0.0
   A(I) = SQRT(G*P(I)/R(I))
20 CONTINUE
   RETURN
   END
   SUBROUTINE INIT2R(PSEXIT, PREF, RREF)
   DIMENSION P(203), R(203), U(203), A(203), S(203), X(203)
   COMMON/FUN1/G, PA, RA, UA, RB, RMU
   COMMON/SUBS/P,R,U,A,S,X
   DO 10 I=3,201,2
   P(I) = PREF
   R(I) = RREF
   U(I) = 0.0
   A(I) = SQRT(P(I) * G/R(I))
10 CONTINUE
   P(1) = P(3)
   R(1) = R(3)
   U(1) = -U(3)
   A(1) = SQRT(G*P(1)/R(1))
   P(203) = PSEXIT
   R(203) = R(201)
   PA=P(201)
   RA = R(201)
   UA = U(201)
   PB = P(203)
   RB=R(203)
   IF(PA.GT.PB) GO TO 20
   U(203) = UA - PHI1(PB)
   GO TO 30
20 U(203)=UA-PSI(PB)
30 A(203) = SQRT(G*P(203)/R(203))
   RETURN
   END
   SUBROUTINE INIT2L(PSEXIT)
   DIMENSION P(203), R(203), U(203), A(203), S(203), X(203)
   COMMON/FUN1/G, PA, RA, UA, RB, RMU
   COMMON/SUBS/P,R,U,A,S,X
   DO 10 I=3,201,2
   P(I) = 285080.0
   R(I)=0.897
   U(I) = 0.0
   A(I) = SQRT(G*P(I)/R(I))
10 CONTINUE
   RETURN
   END
   SUBROUTINE INIT3L(PSINL, RINL)
   DIMENSION P(203), R(203), U(203), A(203), S(203), X(203)
   COMMON/FUN1/G, PA, RA, UA, RB, RMU
   COMMON/SUBS/P, R, U, A, S, X
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RCM0 **RCMO RCMO** RCM0 RCM0 **RCMO** RCM0 **RCMO RCMO RCMO** RCM0 RCMO RCM0 RCM0 RCM0 RCM0 RCM0 RCM01 RCM01 RCM0 RCM01 RCM0 RCM0 RCMO RCMC RCMC

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DO 10 I=3,201,2
                                                                              RCM03270
   P(I) = 2390000.0
                                                                              RCM03280
   R(I) = 9.787
                                                                              RCM03290
   U(T) = 0.0
                                                                              RCM03300
   A(I) = SQRT(G*P(I)/R(I))
                                                                              RCM03310
10 CONTINUE
                                                                              RCM03320
   P(1) = PSINL
                                                                              RCM03330
   R(1)=RINL
                                                                              RCM03340
   PA=P(3)
                                                                              RCM03350
   RA=R(3)
                                                                              RCM03360
   UA=U(3)
                                                                              RCM03370
   PB=P(1)
                                                                              RCM03380
   U(1) = UA + PHI1(PB)
                                                                              RCM03390
   A(1) = SORT(G*P(1)/R(1))
                                                                              RCM03400
   P(203) = P(201)
                                                                              RCM03410
   R(203) = R(201)
                                                                              RCM03420
   U(203) = -U(201)
                                                                              RCM03430
   A(203) = SQRT(G*P(203)/R(203))
                                                                              RCM03440
   RETURN
                                                                              RCM03450
   END
                                                                              RCM03460
   SUBROUTINE INIT3R(PSINR, RINR)
                                                                              RCM03470
   DIMENSION P(203), R(203), U(203), A(203), S(203), X(203)
                                                                              RCM03480
   COMMON/SUBS/P.R.U.A.S.X
                                                                              RCM03490
   COMMON/FUN1/G.PA.RA.UA.RB.RMU
                                                                              RCM03500
   DO 10 I=3,201,2
                                                                              RCM03510
   P(I) = 2421667.5
                                                                              RCM03520
   R(I) = 9.787
                                                                              RCM03530
   U(I) = 0.0
                                                                              RCM03540
   A(I) = SORT(G*P(I)/R(I))
                                                                              RCM03550
10 CONTINUE
                                                                              RCM03560
   P(203) = PSTNR
                                                                              RCM03570
   PA=P(201)
                                                                              RCM03580
   RA=R(201)
                                                                              RCM03590
   UA = U(201)
                                                                              RCM03600
   PB = P(203)
                                                                              RCM03610
   U(203) = UA - PHI1(PB)
                                                                              RCM03620
   R(203) = RINR
                                                                              RCM03630
   A(203) = SQRT(G^{*}P(203)/R(203))
                                                                              RCM03640
   P(1) = P(3)
                                                                              RCM03650
   R(1) = R(3)
                                                                              RCM03660
   U(1) = -U(3)
                                                                              RCM03670
   A(1) = SQRT(G*P(1)/R(1))
                                                                              RCM03680
   RETURN
                                                                              RCM03690
   END
                                                                              RCM03700
   SUBROUTINE BCL1
                                                                              RCM03710
   DIMENSION P(203), R(203), U(203), A(203), S(203), X(203)
                                                                              RCM03720
   COMMON/SUBS/P,R,U,A,S,X
                                                                              RCM03730
   COMMON/FUN1/G, PA, RA, UA, RB, RMU
                                                                              RCM03740
   P(1) = P(3)
                                                                              RCM03750
   R(1) = R(3)
                                                                              RCM03760
   U(1) = -U(3)
                                                                              RCM03770
   A(1) = SORT(G*P(1)/R(1))
                                                                              RCM03780
   RETURN
                                                                              RCM03790
   END
                                                                              RCM03800
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   SUBROUTINE BCR1
                                                                            RCM0
   DIMENSION P(203), R(203), U(203), A(203), S(203), X(203)
                                                                            RCM0
   COMMON/SUBS/P,R,U,A,S,X
                                                                            RCM0
   COMMON/FUN1/G, PA, RA, UA, RB, RMU
                                                                            RCM0
   P(203) = P(201)
                                                                            RCM0
   R(203) = R(201)
                                                                            RCM0
   U(203) = -U(201)
                                                                            RCM0
   A(203) = SQRT(G*P(203)/R(203))
                                                                            RCM0
   RETURN
                                                                            RCM0
   END
   SUBROUTINE BCL2(PSEXIT, PREF)
                                                                            RCM0
   DIMENSION P(203), R(203), U(203), A(203), S(203), X(203)
                                                                            RCM0
                                                                            RCM0
   COMMON/SUBS/P,R,U,A,S,X
                                                                            RCM0
   COMMON/FUN1/G, PA, RA, UA, RB, RMU
                                                                            RCM0
   P(1)=PSEXIT/PREF
                                                                            RCM0
   R(1)=R(3)
   U(1)=U(3)
                                                                            RCM0
   A(1) = SQRT(G*P(1)/R(1))
                                                                            RCM0
                                                                            RCM0
   RETURN
                                                                            RCM0
   END
   SUBROUTINE BCR2(PSEXIT, PREF)
                                                                            RCM0
   DIMENSION P(203), R(203), U(203), A(203), S(203), X(203)
                                                                            RCM0
                                                                            RCM0
   COMMON/SUBS/P,R,U,A,S,X
   COMMON/FUN1/G, PA, RA, UA, RB, RMU
                                                                            RCM0
   P(203)=PSEXIT/PREF
                                                                            RCM0
                                                                            RCM0
   R(203) = R(201)
   PA = P(201)
                                                                            RCM0
   RA=R(201)
                                                                            RCM0
   UA=U(201)
                                                                            RCM0
   PB = P(203)
                                                                            RCM01
   RB=R(203)
                                                                            RCM01
   IF(PA.GT.PB) GO TO 10
                                                                            RCM01
   U(203)=UA-PHI1(PB)
                                                                            RCM01
   GO TO 20
                                                                            RCM01
10 U(203) = UA - PSI(PB)
                                                                            RCM01
20 A(203) = SORT(G*P(203)/R(203))
                                                                            RCM01
   RETURN
                                                                            RCM01
   END
                                                                            RCM01
   SUBROUTINE BCL3(PSINL, RINL, PREF, RREF)
                                                                            RCMO
   DIMENSION P(203), R(203), U(203), A(203), S(203), X(203)
                                                                            RCM0
   COMMON/SUBS/P,R,U,A,S,X
                                                                            RCM0
   COMMON/FUN1/G, PA, RA, UA, RB, RMU
                                                                            RCM0
   P(1)=PSINL/PREF
                                                                            RCM0
   R(1)=RINL/RREF
                                                                            RCM0
   PA=P(3)
                                                                            RCM0
   RA=R(3)
                                                                            RCM0
   UA=U(3)
                                                                            RCM0
   PB=P(1)
                                                                            RCM0
   U(1)=UA+PHI1(PB)
                                                                             RCM0
   A(1) = SQRT(G*P(1)/R(1))
                                                                             RCM0
   RETURN
                                                                             RCM0
                                                                             RCM0
   END
   SUBROUTINE BCR3(PSINR, RINR, PREF, RREF)
                                                                            RCM0
   DIMENSION P(203), R(203), U(203), A(203), S(203), X(203)
                                                                            RCM0
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COMMON/SUBS/P,R,U,A,S,X
                                                                           RCM04350
   COMMON/FUN1/G.PA.RA.UA.RB.RMU
                                                                           RCM04360
   P(203)=PSINR/PREF
                                                                           RCM04370
   R(203)=RINR/RREF
                                                                           RCM04380
   PA=P(201)
                                                                           RCM04390
   RA = R(201)
                                                                           RCM04400
   UA = U(201)
                                                                           RCM04410
   PB = P(203)
                                                                           RCM04420
   U(203) = UA - PHI1(PB)
                                                                           RCM04430
   A(203) = SORT(G*P(203)/R(203))
                                                                           RCM04440
   RETURN
                                                                           RCM04450
   END
                                                                           RCM04460
   SUBROUTINE BCL4 (PTOTIN.RTOTIN.PREF.RREF)
                                                                           RCM04470
   INTEGER QOUT
                                                                           RCM04480
   DIMENSION P(203), R(203), U(203), A(203), S(203), X(203)
                                                                           RCM04490
   DIMENSION XARRAY(100)
                                                                           RCM04500
   COMMON/SUBS/P,R,U,A,S,X
                                                                           RCM04510
   COMMON/FUN1/G, PA, RA, UA, RB, RMU
                                                                           RCM04520
   COMMON XARRAY, N1
                                                                           RCM04530
   N1 = N1 + 1
                                                                           RCM04540
   OOUT=N1/5
                                                                           RCM04550
   PTOT=PTOTIN/PREF
                                                                           RCM04560
   RTOT=RTOTIN/RREF
                                                                           RCM04570
   ATOT=SQRT(G*PTOT/RTOT)
                                                                           RCM04580
   STOT=ALOG(PTOT/RTOT**G)
                                                                           RCM04590
   U(1) = U(3)
                                                                           RCM04600
   A(1) = SORT(ATOT**2, -(G-1, )/2, *ABS(U(1))**2, )
                                                                           RCM04610
   AMACH=U(1)/A(1)
                                                                           RCM04620
   IF(AMACH.LT.0.0) GO TO 60
                                                                           RCM04630
   P(1) = PTOT / (1. + (G-1.) / 2. *AMACH**2.)**(G/(G-1.))
                                                                           RCM04640
   R(1)=RTOT/(1.+(G-1.)/2.*AMACH**2.)**(1./(G-1.))
                                                                           RCM04650
   S(1) = ALOG(P(1)/R(1) * G)
                                                                           RCM04660
   GO TO 50
                                                                           RCM04670
60 P(1)=PTOT/(1.+(G-1.)/2.*ABS(AMACH)**2.)**(G/(G-1.))
                                                                           RCM04680
   R(1)=RTOT/(1.+(G-1.)/2.*ABS(AMACH)**2.)**(1./(G-1.))
                                                                           RCM04690
   S(1) = ALOG(P(1)/R(1) * G)
                                                                           RCM04700
50 RETURN
                                                                           RCM04710
   END
                                                                           RCM04720
   SUBROUTINE BCR4 (PTOTIN, RTOTIN, PREF, RREF)
                                                                           RCM04730
                                                                           RCM04740
   INTEGER QOUT
   DIMENSION P(203), R(203), U(203), A(203), S(203), X(203)
                                                                           RCM04750
   DIMENSION XARRAY(100)
                                                                           RCM04760
   COMMON/SUBS/P,R,U,A,S,X
                                                                           RCM04770
   COMMON/FUN1/G, PA, RA, UA, RB, RMU
                                                                           RCM04780
   COMMON XARRAY, N1
                                                                           RCM04790
   N1 = N1 + 1
                                                                           RCM04800
                                                                            RCM04810
   QOUT=N1/25
   PTOT=PTOTIN/PREF
                                                                            RCM04820
   RTOT=RTOTIN/RREF
                                                                            RCM04830
   ATOT = SQRT (G*PTOT / RTOT)
                                                                            RCM04840
   STOT = ALOG(PTOT / RTOT * G)
                                                                            RCM04850
   U(203) = U(201)
                                                                            RCM04860
   A(203) = SQRT(ATOT**2.-(G-1.)/2.*ABS(U(203))**2.)
                                                                            RCM04870
   AMACH=U(203)/A(203)
                                                                            RCM04880
```

```
IF(AMACH.LT.0.0) GO TO 60
                                                                           RCM04
   P(203)=PTOT/(1.+(G-1.)/2.*AMACH**2.)**(G/(G-1.))
                                                                           RCM04
   R(203)=RTOT/(1.+(G-1.)/2.*AMACH**2.)**(1./(G-1.))
                                                                           RCM04
   S(203) = ALOG(P(203)/R(203)**G)
                                                                           RCM04
                                                                           RCM04
   GO TO 50
60 P(203)=PTOT/(1.+(G-1.)/2.*ABS(AMACH)**2.)**(G/(G-1.))
                                                                           RCM04
   R(203)=RTOT/(1.+(G-1.)/2.*ABS(AMACH)**2.)**(1./(G-1.))
                                                                           RCM04
   S(203) = ALOG(P(203)/R(203)**G)
                                                                           RCM04
50 RETURN
                                                                           RCM04
   END
                                                                           RCM04
   SUBROUTINE BCL5
                                                                           RCM04
   DIMENSION P(203), R(203), U(203), A(203), S(203), X(203)
                                                                           RCM0!
   COMMON/SUBS/P,R,U,A,S,X
                                                                           RCM0!
   P(1)=P(3)
                                                                           RCM0!
   R(1) = R(3)
                                                                           RCM0!
   U(1)=U(3)
                                                                           RCMO!
   A(1) = A(3)
                                                                           RCMO!
   RETURN
                                                                           RCMO!
   END
                                                                           RCM0!
   SUBROUTINE BCR5
                                                                           RCM0!
   DIMENSION P(203), R(203), U(203), A(203), S(203), X(203)
                                                                           RCM0!
   COMMON/SUBS/P,R,U,A,S,X
                                                                           RCM0!
   P(203) = P(201)
                                                                           RCMO!
   R(203) = R(201)
                                                                           RCM0!
   U(203)=U(201)
                                                                           RCMO!
   A(203) = A(201)
                                                                           RCMO!
   RETURN
                                                                            RCM0!
   END
                                                                            RCM0!
   FUNCTION WDP(II)
                                                                            RCM0!
   DIMENSION WNORM(12), IDIGT(12)
                                                                            RCMO!
   COMMON/SAMPLE/WNORM, IDIGT
                                                                            RCMO!
   IF (II.EQ.0) GO TO 10
                                                                            RCMO!
   L1=2
                                                                            RCMO!
   L2 = 1
                                                                            RCMO!
   DO 20 JJ=1,12
                                                                            RCM0!
   IDIGT(JJ)=0
                                                                            RCM0!
   WNORM(JJ)=1./FLOAT(L1**JJ)
                                                                            RCM0!
20 CONTINUE
                                                                            RCMO!
   WDP=0.
                                                                            RCM0!
   RETURN
                                                                            RCM0!
10 DO 40 JJ=1,12
                                                                            RCM0!
   L1=2
                                                                            RCM0.
   L2=1
                                                                            RCM0.
   KJ0=IDIGT(JJ)
                                                                            RCMO.
   KJN=MOD((KJ0+1),L1)
                                                                            RCMO.
   IDIGT(JJ)=KJN
                                                                            RCM0.
   IF (KJO.LT.KJN) GO TO 50
                                                                            RCMO.
40 CONTINUE
                                                                            RCMO.
50 SUM=0.
                                                                            RCMO.
   DO 60 JJ=1,12
                                                                            RCMO.
   KNEW=MOD(IDIGT(JJ)*L2,L1)
                                                                            RCMO.
   SUM=SUM+FLOAT(KNEW)*WNORM(JJ)
                                                                            RCMO.
60 CONTINUE
                                                                            RCMO.
   WDP=SUM
                                                                            RCMO.
```

```
RETURN
                                                                            RCM05430
    END
                                                                            RCM05440
    SUBROUTINE PLOT1(K)
                                                                            RCM05450
    DIMENSION XORG(4), YORG(4), YMAX(4), YMIN(4)
                                                                            RCM05460
    DATA XORG/0.5,4.75,0.5,4.75/
                                                                            RCM05470
    DATA YORG/0.5,0.5,4.75,4.75/
                                                                            RCM05480
    DATA YMAX/3.50,3.0,0.5,2.0/
                                                                            RCM05490
    DATA YMIN/0.5,0.0,-0.5,-2.0/
                                                                            RCM05500
    DO 10 I=1.4
                                                                            RCM05510
    CALL PHYSOR(XORG(I), YORG(I))
                                                                            RCM05520
    CALL AREA2D(3.5,3.5)
                                                                            RCM05530
    CALL FRAME
                                                                            RCM05540
    CALL GRAF(0., 'SCALE', 1.0, YMIN(I), 'SCALE', YMAX(I))
                                                                            RCM05550
    CALL ENDGR(0)
                                                                            RCM05560
10 CONTINUE
                                                                            RCM05570
    CALL PHYSOR(8.5,0.5)
                                                                            RCM05580
    CALL AREA2D(2.25,7.75)
                                                                            RCM05590
    CALL FRAME
                                                                            RCM05600
    CALL GRAF(0., 'SCALE', 1., 0, 'SCALE', K)
                                                                            RCM05610
    CALL ENDGR(0)
                                                                            RCM05620
    RETURN
                                                                            RCM05630
    END
                                                                            RCM05640
    SUBROUTINE_PLOT2(N,K)
                                                                            RCM05650
    DIMENSION XORG(4), YORG(4), YMAX(4), YMIN(4), KNT(4), IYNAM(10)
                                                                            RCM05660
    DIMENSION PARRAY(100), RARRAY(100), UARRAY(100), SARRAY(100), XARRAY(1RCM05670
   *00)
                                                                            RCM05680
    DIMENSION P(203), R(203), U(203), A(203), S(203), X(203)
                                                                            RCM05690
    COMMON/SUBS/P,R,U,A,S,X
                                                                            RCM05700
    COMMON XARRAY
                                                                            RCM05710
    DATA XORG/0.5,4.75,0.5,4.75/
                                                                            RCM05720
    DATA YORG/0.5,0.5,4.75,4.75/
                                                                            RCM05730
    DATA YMAX/3.50,3.0,0.5,2.0/
                                                                            RCM05740
    DATA YMIN/0.5,0.0,-0.5,-2.0/
                                                                            RCM05750
    DATA KNT/1,4,6,9/
                                                                            RCM05760
    DATA IYNAM/'PRES', 'SURE', '$ ', 'DENS', 'ITY$', 'VELO', 'CITY', '$
                                                                           'RCM05770
   ☆,'ENTR','OPY$'/
                                                                            RCM05780
    DO 200 I=1,100
                                                                            RCM05790
    PARRAY(I) = P(I*2+1)
                                                                            RCM05800
    RARRAY(I) = R(I*2+1)
                                                                            RCM05810
    UARRAY(I)=U(I*2+1)
                                                                            RCM05820
    SARRAY(I) = S(I*2+1)
                                                                            RCM05830
200 CONTINUE
                                                                            RCM05840
                                                                            RCM05850
    DO 300 I=1,4
    CALL PHYSOR(XORG(I), YORG(I))
                                                                            RCM05860
    CALL AREA2D(3.5,3.5)
                                                                            RCM05870
    CALL XNAME('X',1)
                                                                            RCM05880
    CALL YNAME(IYNAM(KNT(I)), 100)
                                                                            RCM05890
    CALL GRAF(0., 'SCALE', 1.0, YMIN(I), 'SCALE', YMAX(I))
                                                                            RCM05900
    IF(I.EQ.1) CALL SETCLR('YELLOW')
                                                                            RCM05910
    IF(I.EQ.2) CALL SETCLR('CYAN')
                                                                            RCM05920
    IF(I.EQ.3) CALL SETCLR('RED')
IF(I.EQ.4) CALL SETCLR('MAGENTA')
                                                                            RCM05930
                                                                            RCM05940
    IF(N.EQ.K) CALL SETCLR('WHITE')
                                                                            RCM05950
    IF(I.EQ.1) CALL CURVE (XARRAY, PARRAY, 100,0)
                                                                            RCM05960
```

IF(I.EQ.2) CALL CURVE (XARRAY, RARRAY, 100,0) RCM(IF(I.EQ.3) CALL CURVE (XARRAY, UARRAY, 100,0) RCM(IF(I.EQ.4) CALL CURVE (XARRAY, SARRAY, 100,0) RCM(CALL ENDGR(0)RCM(300 CONTINUE RCM(RETURN RCM(END RCM(SUBROUTINE GE(SWL, SWR, N, TTOTAL, TIME, UEXMAX, PTOTIN, PREF) RCM(INTEGER SWL, SWR RCM(DIMENSION P(203), R(203), U(203), A(203), S(203), X(203) RCM(COMMON/SUBS/P,R,U,A,S,X RCM(C**CALCULATION STARTS AT EXHAUST PORT OPENING. SUBROUTINE STRUCTURED RCM(C**ACCORDINGLY. RCM(IF((SWL.EQ.1).AND.(SWR.EQ.2)) GO TO 10 RCM(IF((SWL.EQ.4).AND.(SWR.EQ.2)) GO TO 30 RCM(IF((SWL.EQ.4).AND.(SWR.EQ.1)) GO TO 50 RCM(IF((SWL.EQ.1).AND.(SWR.EQ.1)) RETURN RCM(10 PWALL=P(2)RCM(IF(PWALL.LE.(PTOTIN/PREF)) GO TO 20 RCM(RETURN RCM(20 SWL=4 RCM(WRITE(6,74)RCM(WRITE(6,75) N, TTOTAL, TIME RCM(RETURN RCM(30 UEXIT=U(202) RCM(IF(UEXMAX.LT.UEXIT) UEXMAX=UEXIT RCM(IF(UEXIT.LT.UEXMAX/2.) GO TO 40 RCM(RETURN RCM(40 SWR=1 RCM(RCM(WRITE(6,76)WRITE(6,75) N,TTOTAL,TIME RCM(RCM(RETURN 50 PlSHOK=P(2)RCM(RCM(IF(P1SHOK.GT.PTOTIN/PREF) GO TO 60 RCM(RETURN 60 SWL=1 RCM(WRITE(6,77) RCM(WRITE(6,75) N,TTOTAL,TIME RCM(74 FORMAT (5X, 'INLET PORT OPENS AT: ') RCM(75 FORMAT(5X,14,5X,2F14.7) RCM(76 FORMAT(5X, 'EXHAUST PORT CLOSES AT:') RCM() 77 FORMAT (5X, 'INLET PORT CLOSES AT: ') RCM() RETURN RCM() END RCM() SUBROUTINE SPCTRA(N, SWL, SWR, TIME, UEXMAX, PSEXIT, PSOUT1, PSOUT2, PSOUTRCM(*3, JCOUNT, QPRINT, TTOTAL, KCOUNT) RCM() INTEGER SWL, SWR, QPRINT RCM() DIMENSION P(203), R(203), U(203), A(203), S(203), X(203) RCM() COMMON/SUBS/P,R,U,A,S,X RCM() C*CALCULATION STARTS AT HP GAS IN PORT. JCOUNT IS NUMBERED ACCORDINGLY**RCM IF((SWL.EQ.1).AND.(SWR.EQ.3)) GO TO 10 RCM() IF((SWL.EQ.2).AND.(SWR.EQ.3)) GO TO 20 RCM(IF((SWL.EQ.2).AND.(SWR.EQ.1)) GO TO 30 RCM(IF((SWL.EQ.5).AND.(SWR.EQ.1)) GO TO 40 RCM()

0

IF((SWL.EQ.2).AND.(SWR.EO.5)) GO TO 50 RCM06510 IF((SWL.EQ.2).AND.(SWR.EO.4)) GO TO 60 RCM06520 IF((SWL.EQ.1).AND.(SWR.EQ.4)) GO TO 70 RCM06530 10 IF(U(3).LT.0.0) GO TO 11 RCM06540 RETURN RCM06550 11 JCOUNT=JCOUNT+1 RCM06560 PSEXIT=PSOUT1 RCM06570 SWL=2RCM06580 WRITE(6.12)RCM06590 WRITE(6,13)N, TIME, SWL, SWR, JCOUNT RCM06600 12 FORMAT(5X, 'H.P. AIR OUT PORT OPENS AT') RCM06610 **13** FORMAT(5X, I4, 5X, F9.7, 5X, 3I3) RCM06620 RETURN RCM06630 20 DO 26 I=5,199,2 RCM06640 IF((R(I)-R(I+2)).GT.0.1) GO TO 22 RCM06650 GO TO 26 RCM06660 $22 \times CNTCT = X(I)$ RCM06670 UCNTCT=U(I) RCM06680 TCNTCT=XCNTCT/ABS(UCNTCT) RCM06690 AHEAD=A(199)RCM06700 THEAD = 1.0 / A(199)RCM06710 IF(TCNTCT.LE.THEAD) GO TO 23 RCM06720 RETURN RCM06730 23 JCOUNT=JCOUNT+1 RCM06740 SWR = 1RCM06750 RCM06760 WRITE(6, 24)WRITE(6,25)N, TIME, SWL, SWR, JCOUNT RCM06770 24 FORMAT(5X, 'H.P. GAS IN PORT CLOSES AT') RCM06780 **25** FORMAT(5X, 14, 5X, F9.7, 5X, 313) RCM06790 RETURN RCM06800 **26 CONTINUE** RCM06810 30 IF(JCOUNT.EQ.4) GO TO 80 RCM06820 IF(JCOUNT.EQ.6) GO TO 90 RCM06830 RCM06840 IF(JCOUNT.EO.8) GO TO 100 IF((R(2)-R(4)).GT.0.1) GO TO 31 RCM06850 RETURN RCM06860 31 JCOUNT=JCOUNT+1 RCM06870 RCM06880 SWL=5 WRITE(6, 32)RCM06890 WRITE(6,33)N, TIME, SWL, SWR, JCOUNT RCM06900 32 FORMAT (5X, 'HP AIR OUT PORT CLOSES AND TUNING PORT L1 OPENS AT') RCM06910 **33** FORMAT(5X,14,5X,F9.7,5X,313) RCM06920 RCM06930 RETURN 40 IF(JCOUNT.EQ.7) GO TO 110 RCM06940 IF(U(3).GE.0.0) GO TO 41 RCM06950 RETURN RCM06960 41 JCOUNT=JCOUNT+1 RCM06970 RCM06980 PSEXIT=PSOUT2 RCM06990 SWL=2 RCM07000 WRITE(6, 42)WRITE(6,43)N, TIME, SWL, SWR, JCOUNT RCM07010 42 FORMAT (5X, 'TUNING PORT L1 CLOSES AND EXHAUST PORT E1 OPENS AT') RCM07020 43 FORMAT(5X,14,5X,F9.7,5X,313) RCM07030 RCM07040 RETURN

- at

80	IF(ABS(U(201)).GT0001) GO TO 81		RCM07(
0 1	RETURN		RCM07(
0 L	SWR=5		RCM070
	WRITE(6.82)		RCM07(
	WRITE(6,83)N,TIME,SWL,SWR,JCOUNT		RCM07
82	FORMAT(5X, 'TUNING PORT R1 OPENS AT')		RCM07
83	FORMAT(5X,14,5X,F9.7,5X,313)		RCM07
50	RETURN TE(ICOUNT EO A) CO TO 120		RCMU7.
20	IF(JCOUNT.EQ.7) GO IO 120IF(ABS(U(201)-U(3)) LF 0 001) GO TO 51		RCM07
	RETURN		RCM07
51	JCOUNT=JCOUNT+1		RCM07
	SWR=1		RCM07
	WRITE(6,52)		RCM07
E 2	WRITE(6,53)N, TIME, SWL, SWR, JCOUNT		RCM07:
53	FORMAT(5X, TONING FORT RI CLOSES RI) FORMAT(5X T4 5X F9 7 5X 3T3)		RCM07
55	RETURN		RCM07:
90	THEAD1=X(201)/(ABS(U(3))+A(3))		RCM07:
	KCOUNT=KCOUNT+1		RCM07:
	IF(KCOUNT.EQ.1) TTOT1=TTOTAL		RCM07:
	DETUDN		RCMU7.
91	ICOUNT=ICOUNT+1		RCM07
<i></i>	SWL=5		RCM07
	WRITE(6,92)		RCM07
	WRITE(6,93)N,TIME,SWL,SWR,JCOUNT		RCM07
92	FORMAT(5X, 'EXHAUST PORT E1 CLOSES AND TUNING PORT L2 OPENS AT	')	RCM07
93	FORMAT (5X, 14, 5X, F9.7, 5X, 313)		RCM07
110	TF(U(3) GE(0, 0) GO(TO(11))		RCM07
	RETURN		RCM07
111	JCOUNT=JCOUNT+1		RCM07
	PSEXIT=PSOUT3		RCM07
	SWL=2		RCM07
	WRITE(6,112)		RCM07
112	WKIIL(6,113)N, TIME, SWL, SWK, JOUUNI FORMAT(5% 'TUNING DORT 12 CLOSES AND EXHAUST DORT 52 ODENS AT	11	RCM07
113	FORMAT(5X, TOWING FORT L2 CLOSES AND EXHAUST FORT E2 OPENS AT)	RCM07
115	RETURN		RCM07
100	IF(ABS(U(201)).GT0001) GO TO 101		RCM07
	RETURN		RCM07
101	JCOUNT=JCOUNT+1		RCM07
	SWR=5		RCM07
	WKIIL(6,102) WRITE(6,103)N TIME SUD ICOUNT		RCM07
102	FORMAT(5X 'THINING PORT R2 OPENS AT')		RCM07
103	FORMAT(5X, 14, 5X, F9, 7, 5X, 313)		RCM07
	RETURN		RCM07
120	IF(ABS(U(201)-U(3)).LE.0.0001) GO TO 121		RCM07
101	RETURN		RCM07
171			RCM07
	SWK-4		KCM07

122 123	WRITE(6,122) WRITE(6,123)N,TIME,SWL,SWR,JCOUNT FORMAT(5X,'TUNING PORT R2 CLOSES AND L.P. AIR INLET OPENS AT') FORMAT(5X,14,5X,F9.7,5X,3I3) RETURN	RCM07590 RCM07600 RCM07610 RCM07620 RCM07630
60	IF((R(4)-R(2)).GT.0.1) GO TO 61	RCM07640
61	JCOUNT=JCOUNT+1 SWL=1	RCM07650 RCM07660 RCM07670
	WRITE(6,62)	RCM07680
	WRITE (6,63)N, TIME, SWL, SWR, JCOUNT	RCM07690
62	FORMAT(5X, 'EXHAUST PORT E2 CLOSES AT')	RCM07700
63	FORMAT(5X,14,5X,F9.7,5X,313)	RCM07710
	RETURN	RCM07720
70	IF(U(201).GE.0.0) GO TO /I	RCM07730
7 1	RETURN LCOUNT-O	RCM07740
11		
	SWK-1	RCM07770
	WRITE $(0, 72)$ WRITE $(6, 73)$ N TIME SWI SWR ICOUNT	RCM07780
72	FORMAT(5X, 'CYCLE, COMPLETED, ')	RCM07790
73	FORMAT(5X, 14, 5X, F9, 7, 5X, 313)	RCM07800
	RETURN -	RCM07810
	END	RCM07820

 $\frac{1}{2} = \frac{1}{2} + \frac{1}{2}$

APPENDIX B

PROGRAM RCM

B.1. Program Description

B.l.l. Computational Grid

The computational region is divided into 100 cells; the solution grid points are odd numbered, e.g., 3, 5, 7 ..., 201 with 1 and 203 being the points where the boundary conditions are specified. The even numbered points, 2, 4, 6 ..., 202 are intermediate locations where solutions are stored before being assigned to the solution grid points. See Fig. (2).

B.1.2. Data Input

Data for various ports (exhaust, inlet, etc.) is specified in dimensional form in S.I. units (Pascal (N/m^2) for pressure, kg/m³ for density, m/s for velocity etc.). Reference values are also specified in like manner. See lines RCM00210 through 00250.

Initial data is specified through a call to an appropriate subroutine, depending on where the calculation is started for a particular wave diagram. For the example given in section II on the Spectra Technology wave diagram, the computation is started at the point when the high pressure gas inlet port just opens. The call for initial data is made to subroutine INIT3R, which prescribes data consistent with a solid wall boundary at the left and a 'piston' inflow boundary at the right.

B.1.3. Non-dimensionalization

Non-dimensionalization is carried out in lines 00540 through 00610 with entropy defined as

 $S = ln \left(\frac{p}{\mu Y}\right)$

Note that velocities are all referred to a reference sonic velocity defined by

$$a_{ref} = \frac{Pref}{Pref}$$

B.l.4. Structure

The main program loop starts at line 00630, for the number of time steps specified. The time step is computed according to the appropriate CFL condition for the method, and a random number for the time step is generated by a call to the function subroutine WDP.

A secondary loop to define the sequence of local Riemann problems for the time step is set up at line 00750. For each Riemann problem defined, a call is made to subroutine GLIMM which i) solves the Riemann problem, and ii) samples the solution using the random number generated. The subroutine then returns the sampled solution as the parameters PGLIM, RGLIM, UGLIM for the pressure, density and velocity respectively. These solutions are initially stored in the even numbered intermediate locations on the grid, and are then assigned to either the left or the right solution grid point depending on whether the random number was in the negative or the positive half of the interval respectively.

A call is then made to one of the modular subroutines structured for particular types of wave diagrams, lines 01050-01080, and the others are commented out.

Boundary conditions are invoked after the call to the modular subroutines which return the proper values of the switches SWL and SWR. The structure of the boundary condition subroutines is described in section II. This sequence completes one pass through the main loop and the process is repeated for the number of time steps specified.

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B.2. Example Use of Program RCM

The program is set up in the following steps:

- i) Line 00150 output device designation. See B.3.
- ii) Line 00190 specify the number of time steps, k , and the switches SWL and SWR consistent with where the computation is to be started.
- iii) Lines 00210 prescribe flow data for various ports in through 00250 dimensional form. See list of variables for explanation of variable names.
- iv) Lines 00490 invoke the proper initial data subroutine and through 00530 comment out the rest. See list of subroutines for explanation of subroutine, function subprogram names.
- v) Line 00660 set the interval for number of time steps at which a plot of the flow parameters is required.
- vi) Lines 01050 user supplied modular subroutine for particular through 01080 wave diagram to be computed. Comment out the rest.
- vii) Line 01190 call to plotting routine should be consistent with interval specified in line 0660.
- viii) Lines 02650 identify proper subroutine to prescribe initial through 03700 data (consistent with iv), and specify the data in the subroutine in dimensional form.
- ix) Lines 05470 specify plotting parameters, viz., origins of through 05990 plots, scales, number of points to be plotted, color of plots, etc. Facility dependent.

The subroutines PLOT1 and PLOT2 given in the listing are structured for DISSPLA software installed in the facility at NPGS.

x) Lines 06040 - user supplied modular subroutine for wave diagram through 07820 to be computed.

B.3. Execution

The program is run in an interactive mode and is invoked through a call to DISSPLA, available on most mainframes. After compiling the program (FORTRAN H Extended compiler), the following command executes it:

DISSPLA filename

If working at stations equipped with dual screens, the command on line 150 can be of the type

CALL TEK618 + Tektronix screen

If working on a non-graphics terminal, or a single screen station, this should be changed to

CALL COMPRS

which generates a 'DISSPLA METAFILE' to be routed later to either a screen or a plotter, e.g., VRSTEC, IBM79, TEK618, etc. Once generated, the metafile can be accessed and routed by the command

DISSPOP device designation

These are facility dependent commands and should be modified accordingly.

B.4. List of Important Variables (In Alphabetical Order)

A	-	sonic velocity
AHEAD	-	sonic speed of head wave of rarefaction fan
АМАСН	-	Mach number
AL	-	left side sonic speed value for RP
AR	-	right side sonic speed value for RP
AREF	-	reference speed of sound
ASTAR	-	<pre>speed of sound in 'starred' state of RP solution (see Fig. 3)</pre>
CFLNUM	-	CFL number for time step determination
DT	-	time step
DX	-	grid cell width
EPS	-	small number for pressure iteration in RP solver
G	-	ratio of specific heats, Y
IDIGT	-	see WNORM
II	-	argument used in function subprogram PHI equal to either 0 or l $$
JCOUNT	-	counter
K	-	number of time steps
KCOUNT	-	counter
N	-	counter for time steps
N1	-	counter

 PA - flow parameter describing 'a' state in transition functions PGLIM - pressure value returned by subroutine GLIMM PR I eff side pressure value for RP PREF reference pressure PSEXT - static pressure for incoming 'piston' flow on left side PSINL - static pressure for incoming 'piston' flow on right side PSINL - static pressure for incoming 'piston' flow on right side PSINT - static pressure for incoming 'piston' flow on right side PSINT - static pressure for incoming 'piston' flow on right side PSINT - static pressure for incoming 'piston' flow on right side PSOUTN - total pressure for isentropic inflow PREF pressure in 'starred' state of RP solution (see Fig. 3) PTOTIN - total pressure for isentropic inflow PROME - maximum number of iterations for solution of Riemann problem, (RP) R - density RA, RB - flow parameters describing 'a' and 'b' states in transition functions RGLIM - density returned by subroutine GLIMM RINR - static density for incoming 'piston' flow on left side RL - left side density for RP RMU - function of Y RR - right side density for RP RREF - reference density RTOTIN - total density for isentropic inflow S - entropy SWL - switch for left boundary SWL - switch for right boundary SWL - switch for right boundary SWR - time taken by contact surface to travel a certain distance THEAE - reference time TOTAL - cumulative non-dimensional time for number of time steps U - velocity Flow parameter for 'a' state in transition functions UCCITT - velocity of contact surface UEXMAX - maximum velocity for RP USTAR - velocity for RP USTAR - veloci	Р	-	pressure
PGLIM = pressure value returned by subroutine GLIMM PL = left side pressure value for RP PRF = right side pressure at exit or outlet port PSEXIT = static pressure at exit or outlet port PSINL = static pressure for incoming 'piston' flow on right side PSINT = static pressure for incoming 'piston' flow on right side PSINT = static pressure for incoming 'piston' flow on right side PSINT = static pressure for isentropic inflow OPTOTIN = n = 1,2,3 - exit static pressure for output QSTOP = maximum number of iterations for solution of Riemann problem, (RP) R = density RA,RB = flow parameters describing 'a' and 'b' states in transition functions RCLIM = density for incoming 'piston' flow on right side RINL = static density for incoming 'piston' flow on right side RINL = static density for RP RMU = function of γ RRF = reference density ROTIN = total density for isentropic inflow S = entropy SWL = switch for right boundary SWR = switch for right boundary SWR = switc	PA	-	flow parameter describing 'a' state in transition functions
 PL - left side pressure value for RP PREF - reference pressure PSEXT - static pressure for incoming 'piston' flow on left side PSINL - static pressure for incoming 'piston' flow on left side PSINR - static pressure for incoming 'piston' flow on right side PSUNT - n = 1,2,3 - exit static pressures for cycles with more than one exhaust port PSTAR - pressure in 'starred' state of RP solution (see Fig. 3) PTOTIN - total pressure for incoming 'piston' flow on Riemann problem, (RP) R - density RA,RB - flow parameters describing 'a' and 'b' states in transition functions RGLIM - density for incoming 'piston' flow on right side RLNL - static density for incoming 'piston' flow on right side RLNL - static density for incoming 'piston' flow on right side RLNL - static density for RP RMU - function of Y RRF - reference density RTOTIN - total density for SP RKEF - reference density RTOTIN - total density for isentropic inflow S - entropy SWL - switch for left boundary SWR - switch for right boundary SWR - switch for right boundary SWR - switch for right boundary SUR - real time in seconds TIMEREF - reference time TTOTAL - cumulative non-dimensional time for number of time steps U - velocity U - velocity - velocity for RP WKM - flow parameter for 'a' state in transition functions UCCITT - velocity occurring at an outflow boundary UKMAX - maximu velocity occurring at an outflow boundary UKMAX - walce tot ravel sufface UKMAX - walce tot ravel sufface UKMAX - maximu velocity occurring at an outflow boundary UCLIM - left side velocity for RP UN - flow parameter for 'a' state of RP solution (see Fig. 3) WDP - value returned by random number generator subprogram X NDP - value r	PGLIM	-	pressure value returned by subroutine GLIMM
 PR - right side pressure value for RP PREF - reference pressure PSEXIT - static pressure at exit or outlet port PSINI - static pressure for incoming 'piston' flow on left side PSINR - static pressure for incoming 'piston' flow on right side PSINR - static pressure for incoming 'piston' flow on right side PSOUTN - static pressure for isentropic inflow QRENT - specification of interval size for output QSTOP - maximum number of iterations for solution of Riemann problem, (RP) R - density R, RB - flow parameters describing 'a' and 'b' states in transition functions RCLIM - density for incoming 'piston' flow on left side RINL - static density for incoming 'piston' flow on right side RINR - static density for incoming 'piston' flow on right side RINR - static density for RP RMU - function of γ RRF - right side density for RP RKF - right side density for RP RKF - right side density for Sequence S - entropy SW - switch for left boundary SW - switch for left surface to travel a certain distance TIMEREF - reference time TTOTAL - cumulative non-dimensional time for number of time steps U - velocity UA - flow parameter for 'a' state in transition functions UCNTCT - velocity of contact surface UEXMAX - maximu velocity for RP UR - fight side velocity for RP UR - fight side velocity for RP UR - fight side velocity for RP UR - flow parameter for 'a' state in transition functions UCNTCT - velocity of contact surface UX - flow parameter for 'a' state of number of time steps UNTAR - velocity for RP 	PL	-	left side pressure value for RP
 PREF - reference pressure PSEXIT - static pressure at exit or outlet port PSINL - static pressure for incoming 'piston' flow on left side PSINR - static pressure for incoming 'piston' flow on right side PSOUTn - n = 1,2,3 - exit static pressures for cycles with more than one exhaust port PSTAR - pressure in 'starred' state of RP solution (see Fig. 3) PTOTIN - total pressure for incoming 'piston' flow on right side QSTOP - maximum number of iterations for solution of Riemann problem, (RP) R - density RA,RB - flow parameters describing 'a' and 'b' states in transition functions RCLIM - density returned by subroutine GLIMM RINR - static density for incoming 'piston' flow on left side RL - left side density for RP RW - function of γ RR - right side density for RP RREF - reference density RTOTIN - total density for isentropic inflow S entropy SWR - switch for left boundary SWR - switch for left boundary SWR - switch for right boundary SWR - time taken by contact surface to travel a certain distance TIME - real time in seconds TIMEREF - reference time TOTAL - cumulative non-dimensional time for number of time steps U velocity UA - flow parameter for 'a' state in transition functions UCMTCT - velocity of contact surface UEXMAX - maximum velocity occurring at an outflow boundary UCMTCT - velocity for RP WR - right side velocity for RP WR - right shock wave velocity WR	PR	-	right side pressure value for RP
<pre>PSEXIT - static pressure at exit or outlet port PSINL - static pressure for incoming 'piston' flow on left side PSINR - static pressure for incoming 'piston' flow on right side PSINR - n = 1,2,3 - exit static pressures for cycles with more than one exhaust port - pressure in 'starred' state of RP solution (see Fig. 3) PTOTIN - total pressure for isentropic inflow QSTOP - maximum number of iterations for solution of Riemann problem, (RP) R - density RA,RB - flow parameters describing 'a' and 'b' states in transition functions RCLIM - static density for incoming 'piston' flow on left side RINR - static density for incoming 'piston' flow on right side RINR - static density for RP RMU - function f Y RR - right side density for RP RKEF - reference density RTOTIN - total density for isentropic inflow S - entropy SWL - switch for left boundary SWR - switch for left boundary CWTCT - total density for isentropic inflow S - entropy SWL - switch for left boundary TCMTCT - time taken by head wave of expansion to travel a certain distance TIME - reference time TTOTAL - cumulative non-dimensional time for number of time steps U - velocity UA - flow parameter for 'a' state in transition functions UCMTCT - velocity of contact surface UEXMAX - maximum velocity occurring at an outflow boundary UCMTCT - velocity of contact surface UEXMAX - maximum velocity occurring at an outflow boundary UCMTCT - velocity of contact surface UEXMAX - maximum velocity occurring at an outflow boundary UCLIM - velocity in 'starred' state of RP solution (see Fig. 3) WDP - value returned by subroutine GLIMM UL - left side velocity for RP USTAR - velocity in 'starred' state of RP solution (see Fig. 3) WDP - value returned by random number generator subprogram X - space dimension XCNTCT - location of contact surface XL,XII - random numbers generator subprogram X - space dimension XCNTCT - location of contact surface</pre>	PREF	-	reference pressure
<pre>PSINL - static pressure for incoming 'piston' flow on left side PSINR - static pressure for incoming 'piston' flow on right side PSOUTn - n = 1,2,3 - exit static pressures for cycles with more than one exhaust port PTAR = pressure in 'starred' state of RP solution (see Fig. 3) PTOTIN - total pressure for isentropic inflow QRINT - specification of interval size for output QSTOP - maximum number of iterations for solution of Riemann problem, (RP) R - density RA,RB - flow parameters describing 'a' and 'b' states in transition functions RCLIM - density returned by subroutine GLIMM RINL - static density for incoming 'piston' flow on left side RINR - static density for RP RMU - function of Y RR - right side density for RP RREF - reference density RTOTIN - total density for isentropic inflow S - entropy SWL - switch for left boundary TCNTCT - time taken by contact surface to travel a certain distance TIME - reference time TIME - reference time U - velocity U - velocity of contact surface UEXMAX - maximum velocity occurring at an outflow boundary UCHTCT - velocity for RP UR - right side velocity for RP UR - right shock wave velocity WP - value returned by random number generator subprogram VL - left shock wave velocity WR - right of contact surface XL,XII - random numbers generator subprogram X Space dimension XCNTCT - location of</pre>	PSEXIT	-	static pressure at exit or outlet port
 PSINR - static pressure for incoming 'piston' flow on right side PSOUTA - n = 1,2,3 - exit static pressures for cycles with more than one exhaust port PSTAR - pressure in 'starred' state of RP solution (see Fig. 3) PTOTIN - total pressure for isentropic inflow QFNINT - specification of interval size for output QSTOP - maximum number of iterations for solution of Riemann problem, (RP) R - density RA,RB - flow parameters describing 'a' and 'b' states in transition functions RGLIM - density returned by subroutine GLIMM RINL - static density for incoming 'piston' flow on left side RINR - static density for RP RMU - function of Y RRF - right side density for RP RRFF reference density RTOTIN - total density for isentropic inflow S - entropy SWL - switch for left boundary SWR - switch for right boundary SWR - switch for right boundary SWR - reference time TIMEAP TIMEAP TIME - real time in seconds TIMERFF reference time TIMERFF - reference time TIMEAP TIMEAP TOTAL - cumulative non-dimensional time for number of time steps U - velocity UA - flow parameter for 'a' state in transition functions UCNTCT - velocity of contact surface UEMAX - maximum velocity occurring at an outflow boundary UGLIM - velocity for RP UR - right side velocity for RP UR - right side velocity for RP UR - velocity in 'starte' state of RP solution (see Fig. 3) WDP - value returned by subroutine GLIMM UL - left shock wave velocity WR - right side velocity for RP UR - right side velocity for RP UR - right side velocity for RP UR - right side velocity for RP WDP - value returned by random number generator subprogram MA - left shock wave velocity WR - righ	PSINL	-	static pressure for incoming 'piston' flow on left side
 PSOUTN - n = 1,2,3 - exit static pressures for cycles with more than one exhaust port PSTAR - pressure in 'starred' state of RP solution (see Fig. 3) PTOTIN - total pressure for isentropic inflow QRNIT - specification of interval size for output QSTOP - maximum number of iterations for solution of Riemann problem, (RP) R - density RA,RB - flow parameters describing 'a' and 'b' states in transition functions RCLIM - density for incoming 'piston' flow on left side RINL - static density for fncoming 'piston' flow on right side RL - left side density for RP RKEF - reference density RTOTIN - total density for isentropic inflow S - entropy SWL - switch for left boundary SWR - switch for left boundary SWR - switch for right boundary TCNTCT - time taken by contact surface to travel a certain distance TIMEREF - reference time TTOTAL - cumulative non-dimensional time for number of time steps U - velocity UA - flow parameter for 'a' state in transition functions UCSTCT - velocity occurring at an outflow boundary UCMTCT - velocity for RP UREFF - reference time TUTOAL - cumulative non-dimensional time for number of time steps U - velocity UA - flow parameter for 'a' state in transition functions UCSTAC - velocity of contact surface UEXMAX - maximum velocity occurring at an outflow boundary UCA - flow parameter for RP UR - right side velocity for RP UR - right shock wave velocity WR - right shock wave velocity WR - right shock wave velocity<td>PSINR</td><td>-</td><td>static pressure for incoming 'piston' flow on right side</td>	PSINR	-	static pressure for incoming 'piston' flow on right side
PSTAR - pressure in 'starred' state of RP solution (see Fig. 3) PTOTIN - total pressure for isentropic inflow QPRINT - specification of interval size for output OSTOP - maximum number of iterations for solution of Riemann problem, (RP) R - density RA,RB - flow parameters describing 'a' and 'b' states in transition functions RGLIM - density returned by subroutine GLIMM RINL - static density for incoming 'piston' flow on left side RINR - static density for removing 'piston' flow on right side RL - left side density for RP RMU - function of Y RR - right side density for RP RREF - reference density RTOTIN - total density for isentropic inflow S - entropy SWL - switch for left boundary SWR - switch for left boundary CCNTCT - time taken by contact surface to travel a certain distance THEAD - time taken by head wave of expansion to travel a certain distance TIME - reference time TTOTAL - cumulative non-dimensional time for number of time steps U - velocity U - velocity of contact surface UEXMAX - maximum velocity occurring at an outflow boundary UCLIM - velocity for RP UR - right side velocity for RP UR - right shock wave velocity WR - right shock wave v	PSOUTn	-	<pre>n = 1,2,3 - exit static pressures for cycles with more than one exhaust port</pre>
<pre>PTOTIN = total pressure for isentropic inflow QPRINT = specification of interval size for output QSTOP = maximum number of iterations for solution of Riemann problem, (RP) R = density RA,RB = flow parameters describing 'a' and 'b' states in transition functions RGLIM = density returned by subroutine GLIMM RINL = static density for incoming 'piston' flow on left side RL = left side density for RP RMU = function of Y RR = right side density for RP RREF = reference density RTOTIN = total density for isentropic inflow S = entropy SWL = switch for left boundary SWR = switch for right boundary TCNTCT = time taken by contact surface to travel a certain distance TIME = real time in seconds TIMEREF = reference time TTOTAL = cumulative non-dimensional time for number of time steps U = velocity UA = flow parameter for 'a' state in transition functions UCNTCT = velocity of contact surface UEMAX = maximum velocity occurring at an outflow boundary UL = left side velocity for RP UL = left side velocity for RP UR = right shock wave velocity WR = right shock wave velocity VRORM = variable used in random number generator subprogram X = space dimension XCNTCT = location of contact surface XL,XII = random number scaled to grid cell</pre>	PSTAR	_	pressure in 'starred' state of RP solution (see Fig. 3)
QPRINT-specification of interval size for outputQSTOP-maximum number of iterations for solution of Riemann problem, (RP)R-densityRA,RB-flow parameters describing 'a' and 'b' states in transition functionsRGLIM-density returned by subroutine GLIMMRINL-static density for incoming 'piston' flow on left sideRINL-static density for incoming 'piston' flow on right sideRL-left side density for RPRMU-function of YRR-right side density for RPRREF-reference densityRTOTIN-total density for isentropic inflowS-entropySWL-switch for right boundarySWR-switch for right boundarySWR-switch for right boundarySWR-real time in secondsTIMEREF-reference timeTTOTAL-cumulative non-dimensional time for number of time stepsU-velocityUA-flow parameter for 'a' state in transition functionsUCHTCT-velocity of contact surfaceUEXMAX-maximum velocity occurring at an outflow boundaryUGLIM-velocity for RPUR-right side velocity for RP <tr< td=""><td>PTOTIN</td><td>_</td><td>total pressure for isentropic inflow</td></tr<>	PTOTIN	_	total pressure for isentropic inflow
<pre>QSTOP - maximum number of iterations for solution of Riemann problem, (RP) R - density RA,RB - flow parameters describing 'a' and 'b' states in transition functions RCLIM - density returned by subroutine GLINM RINL - static density for incoming 'piston' flow on left side RINR - static density for incoming 'piston' flow on right side RL - left side density for RP RMU - function of Y RR - right side density for RP RREF - reference density RTOTIN - total density for isentropic inflow S - entropy SWL - switch for left boundary SWR - switch for right boundary TCNTCT - time taken by head wave of expansion to travel a certain distance TIME - real time in seconds TIMEREF - reference time TIMEREF - reference time TOTAL - cumulative non-dimensional time for number of time steps U - velocity UA - flow parameter for 'a' state in transition functions UCNTCT - velocity of contact surface UEXMAX - maximum velocity courring at an outflow boundary UEXIMA - maximum velocity for RP UR - right side velocity for RP UR - right shock wave velocity WNORM - variable used in random number generator subprogram X - space dimension XCNTCT - location of contact surface XI,XII - random numbers scaled to grid cell</pre>	OPRINT	_	specification of interval size for output
<pre>R = density RA,RB = flow parameters describing 'a' and 'b' states in transition functions RGLIM = density returned by subroutine GLIMM RINL = static density for incoming 'piston' flow on left side RINR = static density for incoming 'piston' flow on right side RL = left side density for RP RMU = function of γ RR = right side density for Sentropic inflow S = entropy SWL = switch for left boundary SWR = switch for left boundary CCNTCT = time taken by head wave of expansion to travel a certain distance TIME = reference time TTOTAL = cumulative non-dimensional time for number of time steps U = velocity UA = flow parameter for 'a' state in transition functions UCNTCT = velocity of contact surface UEXMAX = maximum velocity occurring at an outflow boundary UGLIM = velocity in 'starred' state of RP solution (see Fig. 3) WDP = value returned by random number generator subprogram XL = left shok wave velocity WNORM = variable used in random number generator subprogram XL = location of contact surface XL,XI = random numbers scaled to grid cell </pre>	QSTOP	-	maximum number of iterations for solution of Riemann problem, (RP)
<pre>RA,RB - flow parameters describing 'a' and 'b' states in transition functions RGLIM - density returned by subroutine GLIMM RINL - static density for incoming 'piston' flow on left side RINT - static density for incoming 'piston' flow on right side RL - left side density for RP RMU - function of Y RR - right side density for RP RREF - reference density RTOTIN - total density for isentropic inflow S - entropy SWL - switch for left boundary SWR - switch for right boundary TCNTCT - time taken by contact surface to travel a certain distance THEAD - time taken by contact surface to travel a certain distance TIME - real time in seconds TIMEREF - reference time TTOTAL - cumulative non-dimensional time for number of time steps U - velocity UA - flow parameter for 'a' state in transition functions UCNTCT - velocity of contact surface UEXMAX - maximum velocity occurring at an outflow boundary UGLIM - velocity for RP UR - right side velocity WR - value returned by random number generator subprogram WL - left shock wave velocity WNORM - variable used in random number generator subprogram X - space dimension XCNTCT - location of contact surface XL,XII - random numbers scaled to grid cell</pre>	R	-	density
<pre>functions RGLIM - density returned by subroutine GLIMM RINL - static density for incoming 'piston' flow on left side RINR - static density for incoming 'piston' flow on right side RL - left side density for RP RMU - function of Y RR - right side density for RP RREF - reference density RTOTIN - total density for isentropic inflow S - entropy SWL - switch for left boundary TCNTCT - time taken by contact surface to travel a certain distance TIME - reference time TTOTAL - cumulative non-dimensional time for number of time steps U - velocity UA - flow parameter for 'a' state in transition functions UCNTCT - velocity of contact surface UEXMAX - maximum velocity occurring at an outflow boundary UGLIM - velocity in 'starred' state of RP solution (see Fig. 3) WDP - value returned by random number generator subprogram WL - left shock wave velocity WNORM - variable used in random number generator subprogram X - space dimension XCNTCT - location of contact surface XI,XII - random numbers scaled to grid cell </pre>	RA,RB	-	flow parameters describing 'a' and 'b' states in transition
<pre>RGLIM - density returned by subroutine GLIMM RINL - static density for incoming 'piston' flow on left side RINR - static density for incoming 'piston' flow on right side RL - left side density for RP RMU - function of Y RR - right side density for RP RREF - reference density RTOTIN - total density for isentropic inflow S - entropy SWL - switch for left boundary SWR - switch for right boundary TCNTCT - time taken by contact surface to travel a certain distance TIME - real time in seconds TIMEREF - reference time TTOTAL - cumulative non-dimensional time for number of time steps U - velocity UA - flow parameter for 'a' state in transition functions UCNTCT - velocity of contact surface UEXMAX - maximum velocity for RP UR - right side velocity for RP USTAR - velocity in 'started' state of RP solution (see Fig. 3) WDP - value returned by random number generator subprogram WL - left shock wave velocity WNORM - variable used in random number generator subprogram X - space dimension XCNTCT - location of contact surface XI,XII - random numbers scaled to grid cell</pre>			functions
<pre>RINL = static density for incoming 'piston' flow on left side RINR = static density for incoming 'piston' flow on right side RL = left side density for RP RMU = function of Y RR = right side density for RP RREF = reference density RTOTIN = total density for isentropic inflow S = entropy SWL = switch for left boundary SWR = switch for right boundary TCNTCT = time taken by contact surface to travel a certain distance THEAD = time taken by contact surface to travel a certain distance THEAD = time taken by contact surface to travel a certain distance TIME = real time in seconds TIME = real time in seconds TIMEREF = reference time TTOTAL = cumulative non-dimensional time for number of time steps U = velocity UA = flow parameter for 'a' state in transition functions UCNTCT = velocity of contact surface UEXMAX = maximum velocity occurring at an outflow boundary UGLIM = velocity for RP UR = right side velocity for RP USTAR = velocity in 'starred' state of RP solution (see Fig. 3) WDP = value returned by random number generator subprogram WL = left shock wave velocity WNORM = variable used in random number generator subprogram X = space dimension XCNTCT = location of contact surface XI,XII = random numbers scaled to grid cell</pre>	RGLIM	-	density returned by subroutine GLIMM
<pre>RINR = static density for incoming 'piston' flow on right side RL = left side density for RP RMU = function of Y RR = right side density for RP RREF = reference density RTOTIN = total density for isentropic inflow S = entropy SWL = switch for left boundary TCNTCT = time taken by contact surface to travel a certain distance THEAD = time taken by head wave of expansion to travel a certain distance TIME = real time in seconds TIMEREF = reference time TTOTAL = cumulative non-dimensional time for number of time steps U = velocity UA = flow parameter for 'a' state in transition functions UCNTCT = velocity of contact surface UEXMAX = maximum velocity for RP UR = right side velocity for RP UR = right side velocity for RP UR = right side velocity for RP USTAR = velocity in 'starred' state of RP solution (see Fig. 3) WDP = value returned by random number generator subprogram WL = left shock wave velocity WR = right shock wave velocity WR = right shock wave velocity WNORM = variable used in random number generator subprogram X = space dimension XCNTCT = location of contact surface XI,XII = random numbers scaled to grid cell</pre>	RINL	-	static density for incoming 'piston' flow on left side
 RL - left side density for RP RMU - function of γ RR - right side density for RP RREF - reference density RREF - reference density RTOTIN - total density for isentropic inflow S - entropy SWL - switch for left boundary SWR - switch for right boundary TCNTCT - time taken by contact surface to travel a certain distance TIME - real time in seconds TIME F - reference time TTOTAL - cumulative non-dimensional time for number of time steps U - velocity UA - flow parameter for 'a' state in transition functions UCNTCT - velocity of contact surface UEXMAX - maximum velocity occurring at an outflow boundary UGLIM - velocity for RP UR - right side velocity for RP USTAR - velocity in 'starred' state of RP solution (see Fig. 3) WDP - value returned by random number generator subprogram WL - left shock wave velocity WRR - right shock wave velocity WRM - space dimension XA - space dimension XA - space dimension 	RINR	_	static density for incoming 'piston' flow on right side
 RMU - function of γ RR - right side density for RP RREF - reference density RTOTIN - total density for isentropic inflow S - entropy SWL - switch for left boundary SWR - switch for right boundary TCNTCT - time taken by contact surface to travel a certain distance THEAD - time taken by head wave of expansion to travel a certain distance TIME - real time in seconds TIMEREF - reference time TTOTAL - cumulative non-dimensional time for number of time steps U - velocity UA - flow parameter for 'a' state in transition functions UCNTCT - velocity of contact surface UEXMAX - maximum velocity occurring at an outflow boundary UGLIM - velocity for RP UR - right side velocity for RP USTAR - velocity in 'started' state of RP solution (see Fig. 3) WDP - value returned by random number generator subprogram WL - left shock wave velocity WR - right shock wave velocity WR - right shock wave velocity WNORM - variable used in random number generator subprogram X - space dimension XCNTCT - location of contact surface 	RL	-	left side density for RP
<pre>RR - right side density for RP RREF - reference density RTOTIN - total density for isentropic inflow S - entropy SWL - switch for left boundary SWR - switch for right boundary TCNTCT - time taken by contact surface to travel a certain distance THEAD - time taken by head wave of expansion to travel a certain</pre>	RMU	-	function of Y
<pre>RREF - reference density RTOTIN - total density for isentropic inflow S - entropy SWL - switch for left boundary SWR - switch for right boundary TCNTCT - time taken by contact surface to travel a certain distance TIME - time taken by head wave of expansion to travel a certain</pre>	RR -	_	right side density for RP
<pre>RTOTIN - total density for isentropic inflow S - entropy SWL - switch for left boundary SWR - switch for right boundary TCNTCT - time taken by contact surface to travel a certain distance THEAD - time taken by head wave of expansion to travel a certain</pre>	RREF	-	reference density
<pre>S = entropy SWL = switch for left boundary SWR = switch for right boundary TCNTCT = time taken by contact surface to travel a certain distance THEAD = time taken by head wave of expansion to travel a certain distance TIME = real time in seconds TIMEREF = reference time TTOTAL = cumulative non-dimensional time for number of time steps U = velocity UA = flow parameter for 'a' state in transition functions UCNTCT = velocity of contact surface UEXMAX = maximum velocity occurring at an outflow boundary UGLIM = velocity returned by subroutine GLIMM UL = left side velocity for RP UR = right side velocity for RP UR = right side velocity for RP USTAR = velocity in 'starred' state of RP solution (see Fig. 3) WDP = value returned by random number generator subprogram WL = left shock wave velocity WR = right shock wave velocity WR = right shock wave velocity WNORM = variable used in random number generator subprogram X = space dimension XCNTCT = location of contact surface XI,XII = random numbers scaled to grid cell</pre>	RTOTIN	-	total density for isentropic inflow
 SWL - switch for left boundary SWR - switch for right boundary TCNTCT - time taken by contact surface to travel a certain distance THEAD - time taken by head wave of expansion to travel a certain distance TIME - real time in seconds TIMEREF - reference time TTOTAL - cumulative non-dimensional time for number of time steps U - velocity UA - flow parameter for 'a' state in transition functions UCNTCT - velocity of contact surface UEXMAX - maximum velocity occurring at an outflow boundary UGLIM - velocity for RP UR - right side velocity for RP USTAR - velocity in 'starred' state of RP solution (see Fig. 3) WDP - value returned by random number generator subprogram WL - left shock wave velocity WR - right shock wave velocity 	S	-	entropy
 SWR - switch for right boundary TCNTCT - time taken by contact surface to travel a certain distance TIME - time taken by head wave of expansion to travel a certain distance TIME - real time in seconds TIMEREF - reference time TTOTAL - cumulative non-dimensional time for number of time steps U - velocity UA - flow parameter for 'a' state in transition functions UCNTCT - velocity of contact surface UEXMAX - maximum velocity occurring at an outflow boundary UGLIM - velocity for RP UR - right side velocity for RP USTAR - velocity in 'started' state of RP solution (see Fig. 3) WDP - value returned by random number generator subprogram WL - left shock wave velocity WR - right shock wave velocity WNORM - variable used in random number generator subprogram X - space dimension XCNTCT - location of contact surface XI,XII - random numbers scaled to grid cell 	SWL	-	switch for left boundary
<pre>TCNTCT - time taken by contact surface to travel a certain distance THEAD - time taken by head wave of expansion to travel a certain distance TIME - real time in seconds TIMEREF - reference time TTOTAL - cumulative non-dimensional time for number of time steps U - velocity UA - flow parameter for 'a' state in transition functions UCNTCT - velocity of contact surface UEXMAX - maximum velocity occurring at an outflow boundary UGLIM - velocity returned by subroutine GLIMM UL - left side velocity for RP UR - right side velocity for RP USTAR - velocity in 'starred' state of RP solution (see Fig. 3) WDP - value returned by random number generator subprogram WL - left shock wave velocity WR - right shock wave velocity WNORM - variable used in random number generator subprogram X - space dimension XCNTCT - location of contact surface XI,XII - random numbers scaled to grid cell</pre>	SWR	-	switch for right boundary
 THEAD - time taken by head wave of expansion to travel a certain distance TIME - real time in seconds TIMEREF - reference time TTOTAL - cumulative non-dimensional time for number of time steps U - velocity UA - flow parameter for 'a' state in transition functions UCNTCT - velocity of contact surface UEXMAX - maximum velocity occurring at an outflow boundary UGLIM - velocity returned by subroutine GLIMM UL - left side velocity for RP UR - right side velocity for RP USTAR - velocity in 'starred' state of RP solution (see Fig. 3) WDP - value returned by random number generator subprogram WL - left shock wave velocity WR - right shock wave velocity WNORM - variable used in random number generator subprogram X - space dimension XCNTCT - location of contact surface XI,XII - random numbers scaled to grid cell 	TCNTCT	_	time taken by contact surface to travel a certain distance
 TIME - real time in seconds TIMEREF - reference time TTOTAL - cumulative non-dimensional time for number of time steps U - velocity UA - flow parameter for 'a' state in transition functions UCNTCT - velocity of contact surface UEXMAX - maximum velocity occurring at an outflow boundary UGLIM - velocity returned by subroutine GLIMM UL - left side velocity for RP UR - right side velocity for RP USTAR - velocity in 'starred' state of RP solution (see Fig. 3) WDP - value returned by random number generator subprogram WL - left shock wave velocity WR - right shock wave velocity WR - space dimension X - space dimension X - space dimension XI,XII - random numbers scaled to grid cell 	THEAD	-	time taken by head wave of expansion to travel a certain distance
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<pre>UCNTCT - velocity of contact surface UEXMAX - maximum velocity occurring at an outflow boundary UGLIM - velocity returned by subroutine GLIMM UL - left side velocity for RP UR - right side velocity for RP USTAR - velocity in 'starred' state of RP solution (see Fig. 3) WDP - value returned by random number generator subprogram WL - left shock wave velocity WR - right shock wave velocity WNORM - variable used in random number generator subprogram X - space dimension XCNTCT - location of contact surface XI,XII - random numbers scaled to grid cell</pre>	UA	-	flow parameter for 'a' state in transition functions
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<pre>UR - right side velocity for RP USTAR - velocity in 'starred' state of RP solution (see Fig. 3) WDP - value returned by random number generator subprogram WL - left shock wave velocity WR - right shock wave velocity WNORM - variable used in random number generator subprogram X - space dimension XCNTCT - location of contact surface XI,XII - random numbers scaled to grid cell</pre>	UL	-	left side velocity for RP
 USTAR - velocity in 'starred' state of RP solution (see Fig. 3) WDP - value returned by random number generator subprogram WL - left shock wave velocity WR - right shock wave velocity WNORM - variable used in random number generator subprogram X - space dimension XCNTCT - location of contact surface XI,XII - random numbers scaled to grid cell 	UR	_	right side velocity for RP
 WDP - value returned by random number generator subprogram WL - left shock wave velocity WR - right shock wave velocity WNORM - variable used in random number generator subprogram X - space dimension XCNTCT - location of contact surface XI,XII - random numbers scaled to grid cell 	USTAR	-	velocity in 'starred' state of RP solution (see Fig. 3)
 WL - left shock wave velocity WR - right shock wave velocity WNORM - variable used in random number generator subprogram X - space dimension XCNTCT - location of contact surface XI,XII - random numbers scaled to grid cell 	WDP	_	value returned by random number generator subprogram
 WR - right shock wave velocity WNORM - variable used in random number generator subprogram X - space dimension XCNTCT - location of contact surface XI,XII - random numbers scaled to grid cell 	WL	_	left shock wave velocity
<pre>WNORM - variable used in random number generator subprogram X - space dimension XCNTCT - location of contact surface XI,XII - random numbers scaled to grid cell</pre>	WR	-	right shock wave velocity
 X - space dimension XCNTCT - location of contact surface XI,XII - random numbers scaled to grid cell 	WNORM	-	variable used in random number generator subprogram
XCNTCT - location of contact surface XI,XII - random numbers scaled to grid cell	Х	-	space dimension
XI,XII - random numbers scaled to grid cell	XCNTCT	-	location of contact surface
	XI,XII	-	random numbers scaled to grid cell

XREF	-	reference length
Y	-	argument used in function subprogram PHI equal to PSTAR
Z	-	argument used in function subprogram PHI equal to either PL or PR
ZETA	-	dummy variable (for initialization purposes in random number generator)

B.5. List of Subroutines, Function Subprograms

B.5.1. Subroutines

INIT1	-	prescribes initial data corresponding to SWL=1, SWR=1; e.g., shock-tube problem
INIT2L	-	prescribes initial data corresponding to SWL=2, SWR=1
INIT2R	-	prescribes initial data corresponding to SWL=1, SWR=2
INIT3L	-	prescribes initial data corresponding to SWL=3, SWR=1
INIT3R	-	prescribes initial data corresponding to SWL=1, SWR=3
PLOT1,2	-	graphics subroutines
GLIMM	-	solves the Riemann problem, samples the solution and returns values for flow parameters
GE	-	modular user supplied subroutine to simulate wave diagram of General Electric Wave Engine
DETON	-	modular user supplied subroutine to simulate evacuation of detonation chamber
SPCTRA	-	modular user supplied subroutine to simulate wave diagram of Spectra Technology's Pressure Exchanger
BCL1	-	prescribes boundary conditions (BC's) corresponding to SWL=1, i.e., solid wall on left side
BCL2	-	prescribes BC's corresponding to SWL=2, i.e., outflow at constant static pressure on left side
BCL3	-	prescribes BC's corresponding to SWL=3, i.e., 'piston' inflow on left side
BCL4	-	prescribes BC's corresponding to SWL=4, i.e., isentropic inflow from reservoir on left side
BCL5	-	prescribes BC's corresponding to SWL=5, i.e., wave 'tuning' on left side

BCR1, BCR2, BCR3, BCR4, BCR5 - prescribe BC's corresponding to SWR=1,2,3,4,5 respectively on right side

B.5.2. Function Subprograms

- PHI(y,z) required in iteration procedure for solution of RP
- PHI1(PB) describes shock transition function, $\psi_a(p_b)$, for two states a and b connected by a shock wave (see Ref. 6, Ch. III)
- PSI(PB) describes rarefaction transition function, $\psi_a(p_b)$, for two states a and b connected by a rarefaction wave (see Ref. 6, Ch. III)
- WDP(II) generates a random number in a van der Corput sequence each time it is invoked. Note that it needs to be called once from outside the main loop by specifying an argument II=1 to initialize IDIGT and WNORM, returning a value of 0 for the dummy variable ZETA, and then a second time from within the main loop with an argument II=0 to return a value which is the random number.

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