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**Behavior models for software architecture**

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ABSTRACT

Monterey Phoenix (MP) is an approach to formal software system architecture specification based on behavior models. Architecture modeling focuses not only on the activities and interactions within the system, but also on the interactions between the system and its environment, providing an abstraction for interaction specification. The behavior of the system is defined as a set of events (event trace) with two basic relations: precedence and inclusion. The structure of possible event traces is specified using event grammars and other constraints organized into schemas. The separation of the interaction description from the components behavior is an essential MP feature. The schema framework is amenable to stepwise architecture refinement, reuse, composition, visualization, and multiple view extraction. The approach yields a basis for executable architecture specification supporting early testing and verification, systematic use case generation, and performance estimates with automated tools.
1. INTRODUCTION

The software system development process involves several layers of models, starting with the abstractions capturing the requirements, and proceeding to the detailed design represented by models expressed in some programming language notation, refining the original requirements into a form that is executable on the target computational platform.

In the last decades the concept of architecture has emerged as one such abstraction layer. Architecture plays a role as a bridge between requirements and implementation of a system, and represents a stepwise refinement in the design process with specific objectives and stakeholders. The following principles have emerged as characteristic for software architecture descriptions [Perry, Wolf 1992], [Shaw, Garlan 1996], [Bass et al. 2003].

- An architecture description belongs to a high level of abstraction, ignoring many of the implementation details, such as algorithms and data structures.
- There should be composition operators for the hierarchical design involving components and subsystems.
- The architecture specification should support the reuse of well-known architectural styles and patterns. Practice has provided several architectural styles and referential architectures, as well established, reusable architectural solutions.
- An architecture of a system should be considered in the context of the environment in which it operates, as suggested in the international standard ISO/IEC 42010 “Systems and Software Engineering – Architecture Description” [ISO 2011]
- The software architect needs a number of different views of the software architecture for various uses and stakeholders [Kruchten 1995], including visual representations, like diagrams.
- Errors in early system design are the most expensive to fix when detected later in the development lifecycle. Software architecture descriptions may be used for the early assessment of design, and for stakeholder communication [Bosch 2000].
- The use of scenarios for evaluating software architectures is recommended as one of the best industrial practices [Abowd et al., 1997], [Dobrica, Niemela 2002]. Scenario-Based Architecture Analysis Method (SAAM) [Bass, Clements, Kazman 2003] is one of the most mature and commonly used architecture analysis methods.

A conclusion in [Rozanski and Woods 2012] states: “Every system has an architecture, whether or not it is documented and understood.”

Software architecture is concerned with the selection of architectural elements, their interactions, and the constraints on those elements and their interactions that are necessary to satisfy the requirements and serve as a basis for the design [Perry, Wolf 1992]. The practice of architecture description has converged on the concepts of architectural elements, such as component, connector, and the relationships between them.

[Oreizy et al. 1998], [Taylor et al. 2010] have emphasized the role of connectors in the architecture description as first-class entities. From this point of view a connector becomes yet another behavior interacting with the behaviors of components.

Software design starts with finding an algorithm and mapping it on the appropriate computational platform. An algorithm commonly is specified as a behavior applying a step-by-step procedure to solve the problem at hand. The design process usually proceeds from the high level behavior and involves several layers of refinement. This rationale is behinds the use of pseudo-code for software design.
One of the central tenets in architecture is the principle of reuse. This requires common abstractions on which the reuse framework can be based. For both system and software architectures one of the basic commonalities is the concept of behavior. When designing a system the main concern is to ensure the proper behavior in the context of environment in which the system is supposed to operate.

These considerations imply the importance of behavior models and executable architecture models, and the need to test and verify the system architecture early in the design phase.

We suggest a framework for software architecture modeling called Monterey Phoenix (or MP). Behavior modeling is at the core of this approach. In traditional architecture models the main elements are components (representing the functionality), and connectors (representing the information flow between components). In MP the main concepts are activities and coordination between activities, based on the following principles.

- A view of the architecture as a high level description of possible system behaviors, emphasizing the behavior of subsystems and interactions between subsystems. The MP behavior model is based on the concept of an event as an abstraction of activity.
- Separation of the component behavior description from the interaction description provides for a high level of abstraction and supports the reuse of architectural models. Interactions between activities are modeled using event coordination constructs.
- The environment's behavior is an integral part of the system architecture model. MP provides a uniform method for modeling behaviors of the software, hardware, business processes, and other aspects of the system. This facilitates the role of architecture as a bridge between the system requirements and design.
- The event grammar provides a view of the behavior as a set of activities (event trace) with two basic relations, where the PRECEDES relation captures the dependency abstraction, and the IN relation represents the hierarchical relationship. Since the event trace is a set of events, additional constraints can be specified using set-theoretical operations and predicate logic.
- The MP architecture description is amenable to deriving multiple views, and provides a uniform basis for specifying structural and behavioral aspects of a software system.
- MP supports automated and exhaustive (for a given scope) scenario generation for early system architecture verification. The Small Scope Hypothesis [Jackson 2006] states that most flaws in models could be demonstrated on relatively small counterexamples.
- MP framework can assists in unifying UML activity and sequence diagrams, statechart notations, and the recent Executable UML Alf language [OMG 2010] for behavior specification. MP can be used as an addition to the existing tools and methodologies.

The MP framework is intended for the use of lightweight Formal Methods in software and system architecture design and maintenance. It provides an ecosystem for sanity checking tools, reusable architecture patterns, reusable assertions, queries, and tools for extracting architecture views.

2. BRIEF RELATED WORK SURVEY

The following ideas of behavior modeling and formalization have provided inspiration and insights for this work.

Literate programming introduced by D.Knuth set the directions for hierarchical refinement of structure mapped into behavior, with the concept of pseudo-code and tools to support the refinement process [Knuth 1984].

[Campbell, Habermann 1974] and [Bruegge, Hibbard 1983] have demonstrated the application of path expressions as appropriate abstraction for program monitoring and debugging. In [Perry, Wolf 1992] path expressions have been used (semi-formally) as a part of software architecture description.
CSP (Communicating Sequential Processes) and other process algebras [Hoare 1985], [Milner 1989], [Roscoe 1997] provided a framework for process behavior modeling and formal reasoning about those models, including the ideas of individual events, composite events, and event sharing. This behavior modeling approach has been applied to software architecture descriptions for connector protocol specification [Allen 1997], [Allen, Garlan 1997], [Pelliccione et al. 2009].

Rapide [Luckham et al. 1995a, 1995b] uses events and partially ordered sets of events (posets) to characterize component interaction.

“The backbone of the system model should be a hierarchy of activities, … that capture the functional capabilities of the system - suitably decomposed to a level with which the designer is happy.“ [Harel 1992]. Statecharts [Harel 1987] is an example of labeled transition system approach to the behavior modeling. It became one of the most common behavior modeling frameworks, integrated in the broader modeling and specification systems UML [Booch et al. 2000], and AADL [Feiler et al. 2006].

Coordination models and languages advocate separation of the interactional and the computational aspects of software components. Configuration and architectural description languages share these principles with coordination languages [Papadopolous, Arbab 1998], [Carriero, Gelernter 1992]. Separation of the component behavior from the coordination between behaviors in MP follows this principle and extends on it.

[Wang, Parnas 1994] proposed to use trace assertions to formalize the externally observable behavior of a software module and presented a trace simulator to symbolically interpret the trace assertions and simulate the externally observable behavior. The approach is based on algebraic specifications and term rewriting.

The Alloy modeling framework [Jackson 2006] has strongly influenced MP through ideas of integration of sets and first order predicate logic within the relational logic framework, inheritance structure, emphasis on lightweight Formal Methods as opposed to the full-scale theorem proving, with the fundamental concept of Small Scope Hypothesis, and the principles of immediate feedback and visualization during model design.

The concept of software behavior models based on event grammars and event traces was also introduced in [Auguston 1991, 1995], [Auguston, Jeffery, Underwood 2002], [Auguston, Michael, Shing 2006] as an approach to software debugging and testing automation. The early draft of Monterey Phoenix has appeared in [Auguston 2009 a, 2009 b]. This paper is a substantial extension of a conference paper [Auguston, Whitcomb 2012].

3. BEHAVIOR MODELS

In a certain sense, the source code of a program is a compact description for a set of required behaviors. The source code in any programming language – a finite object by itself – specifies a potentially infinite number of execution paths. The behavior of the system is usually the main concern for the developer, and the presence of unintended behaviors manifests errors in the design. A system is operating in a certain environment, which has its own behavior and interacts with the system. The objective of the MP approach is to provide a framework for specifying behaviors of the system, its parts and its environment, and interactions between them.

3.1 Event concept

An implemented software system usually represents an algorithm, i.e. a step-by-step description of activities tailored towards achieving a certain goal. The MP behavior model is based on the concept of an event as an abstraction of activity. The event has a beginning and an end, and may have duration (a time interval during which the action is accomplished).

The behavior of a system is modeled as a set of events with two binary relations defined for them: precedence (PRECEDES) and inclusion (IN) – the event trace. One action is required to precede another if there is a dependency between them, e.g. the Send event should precede the Receive event. Events may be nested, when a complex activity contains a set of other activities. Imposing one of these basic relations on a
pair of activities represents an important design decision. Usually system behavior does not require a total ordering of events. Both PRECEDES and IN are partial ordering relations. If two events are not ordered, they may occur concurrently. Appendix 1 provides axioms specifying the properties of basic relations.

3.2 Event grammar

The structure of possible event traces is described by an event grammar. A grammar rule specifies structure for a particular event type (in terms of IN and PRECEDES relations) and has a form

\[ A : \text{pattern\_list}; \]

where A is an event type name and pattern\_list is composed from event patterns. Event types that do not appear in the left hand part of rules are considered atomic and may be refined later by adding corresponding rules.

An instance of an event trace satisfying the grammar rule can be visualized as a directed graph with two types of edges (one for each of the basic relations). Events are visualized as boxes, and basic relations as arrows. Fig. 1 outlines the event patterns for use in the grammar rule’s right hand part. Here B, C, D stand for event type names or event patterns.

Sequence denotes ordering of events under the PRECEDES relation. The rule \( A : B; C; \) means that an event \( a \) of the type A contains ordered events \( b \) and \( c \) matching B and C, correspondingly (\( b \) IN \( a \), \( c \) IN \( a \), and \( b \) PRECEDES \( c \)). A grammar rule may contain a sequence of several events, like \( A : B; C; D; \)

![Fig. 1. Event patterns and examples of event traces.](image)

Pattern \( + B + \) may be used to denote a sequence of one or more events B, and \( \{ + B + \} \) denotes a set of one or more events B. In all cases it is assumed that iterated event instances are unique. Event patterns may use recursion or iteration to describe repeated behavior patterns.

An event grammar is a graph grammar for directed acyclic graphs of vertices (events) with edges representing relations IN and PRECEDES.

Example 1. An event grammar for car race scenarios.

\[
\text{car\_race:} \quad \{ + \text{driving\_a\_car} + \};
\]

\[
\text{driving\_a\_car:} \quad \text{go\_straight} \ ( \{ \text{go\_straight} | \text{turn\_left} | \text{turn\_right} \} \*) \ \text{stop};
\]

\[
\text{go\_straight:} \quad \{ \text{accelerate} | \text{decelerate} | \text{cruise} \};
\]

Similar to context-free grammars, event grammars can be used as production grammars to derive instances of event traces.
Fig. 2. An instance of event trace derived from the event grammar in Example 1.

4. BEHAVIOR COMPOSITION AND ARCHITECTURE VIEWS

The behavior of a particular system is specified as a set of possible event traces using a schema. The concept of the MP schema is inspired by the Z schema [Spivey 1992]. The purpose is to define the structure of event traces (in terms of IN and PRECEDES relations) using event grammar rules and other constraints. A schema usually contains a collection of events called roots representing the behaviors of parts of the system (components and connectors in common architecture descriptions), composition operations specifying interactions between these behaviors, and additional constraints on behaviors.

There is precisely one instance of each root event in a trace. A schema can contain auxiliary grammar rules defining composite event types used in other rules, and may be reused by including it in another schema. A schema may define both finite and infinite traces, but most analysis tools for reasoning about a system’s behavior assume that a trace is finite.

The schema represents instances of behavior (event traces) in the same sense as Java source code represents instances of program execution. Just as a particular execution path can be extracted from a Java program’s source code by running it on a JVM, a particular event trace specified by a MP schema can be derived from the event grammar rules by applying behavior composition operations and constraints.

Example 2. Simple pipe/filter architecture pattern.

SCHEMA simple_message_flow
ROOT Task_A: (* send *);
ROOT Task_B: (* receive *);
COORDINATE $x: send FROM Task_A,
               $y: receive FROM Task_B
       DO
           ADD $x PRECEDES $y
       OD;

The composition operation COORDINATE coordinates behaviors of two root events sending and receiving messages. This trace transformation operation takes two root event traces and produces a modified event trace (merging behaviors of Task_A and Task_B) by adding the PRECEDES relation for the selected send and receive pairs. Essentially it is a loop performed over the structure of coordinated events, hence the DO - OD notation for the loop body.
This synchronized COORDINATE composition uses event selection patterns to specify subsets of root traces that should be coordinated. The send pattern identifies the set of events selected from Task_A. Synchronized composition requires that events selected in each coordinated root trace are totally ordered (with respect to the transitive closure of PRECEDES), both selected event sets should have the same number of elements (send events from the first trace and receive events from the second), and the pair coordination follows this ordering (synchronous coordination), i.e. first send is paired with first receive, second with the second, and so on. Labels $x$ and $y$ provide access to the pair of events matching the selection pattern within each iteration. The ADD composition completes the behavior adjustment, specifying additional PRECEDES relation for each pair of selected events. Behavior specified by this schema is a set of matching event traces for Task_A and Task_B with the modifications imposed by the composition. If any of selected event sets is not totally ordered, the synchronized coordination operation fails to produce a resulting trace.

The selection pattern may be either an event type name (atomic or composite), or an alternative pattern composed of event type names (Example 3). Sometimes it is desirable to coordinate groups of events. This can be done with the selection pattern (+ Pattern +) with optional iteration scope (Example 8).

Fig. 3 (a) gives a sample of event trace satisfying the schema simple_message_flow. It resembles a UML sequence diagram’s “swim lanes”.

Different views for different stakeholders can be extracted from MP schemas. For example, each root may be visualized as a box. If there is a composition operation specifying an interaction (or coordination) between root behaviors, the boxes are connected by an arrow marked by the interaction type as illustrated in Fig. 3 (b). The root behavior by itself may be visualized with UML Activity Diagram [Booch et al. 2000]. The environment for MP development may have a library of predefined views providing different visualizations for schemas.

Fig. 3. a) Example of a composed event trace for the simple_message_flow schema. b) An architecture view for the simple_message_flow schema.

Another case of selecting event pairs is called asynchronous coordination. In this case the coordination operation should be marked with a symbol <!>. For example,

\[
\text{COORDINATE <!> } \quad \text{Sx: E1 FROM A,} \\
\quad \quad \quad \text{Sy: E2 FROM B} \\
\quad \text{DO } \quad \text{ADD Sx PRECEDES Sy } \quad \text{OD;}
\]
Matching event sets from $A$ and $B$ should contain an equal number of selected events $E_1$ and $E_2$, correspondingly. Selected sets of $E_1$ and $E_2$ may be totally ordered or not. But now the resulting merged traces will include all permutations of events $E_2$ from $B$ paired with events $E_1$ from $A$, with the \textbf{PRECEDES} relation imposed on each selected pair. This assumes that other constraints, like the partial ordering axioms from Appendix 1, are satisfied. Each permutation yields one potential instance of a resulting trace for the schema deploying this composition. Use of $<!>$ may significantly increase the number of composed traces. In order to reduce the exponential explosion, optimizations similar to symmetry reduction in model checking tools may be considered for trace generation.

The composition operation may be considered as an abstract interaction (interface) description for root behaviors. The separation of the interaction description from the components behavior is an essential MP feature. The same component behavior may be reused with different interaction descriptions – a useful composition/reuse aspect (see Sec. 7).

The \textbf{COORDINATE} operation supports a “cause-effect” refinement for the behavior of two components and it bears a certain similarity to Aspect-Oriented Programming (AOP) paradigm [Kiczales et al. 1997]. For example, the following AOP behavior could be modeled by MP schema where event coordination implements AOP join point and advice coordination.

Suppose that the main stream of execution contains calls to methods $M_1$ and $M_2$ as join points, and the aspect behavior requires a call to $\text{Prolog}$ before, and to $\text{Epilog}$ after each method call as an advice. The corresponding MP model may look like the following.

\begin{verbatim}
Example 3.
ROOT Main:   (* ( M1 | M2 ) *);
ROOT PreAdvice:  (* Prolog *);
ROOT PostAdvice:  (* Epilog *);
COORDINATE  $jp: ( M1 | M2 )  FROM  Main,
$sa1: Prolog  FROM  PreAdvice,
$sa2: Epilog   FROM  PostAdvice
DO  ADD  $sa1  PRECEDES  $jp,  $jp  PRECEDES  $sa2  OD;
\end{verbatim}

\textbf{4.1 DATA ITEMS AS BEHAVIORS}

Data items in MP are represented by actions (events) that may be performed on that data. This principle follows the Abstract Data Type (ADT) concept introduced in [Liskov, Zilles 1974].

\begin{verbatim}
Example 4. Data flow.
SCHEMA Data_flow
ROOT Process_1:  (* work write *);
ROOT Process_2:  (* ( read | work ) *);
ROOT File:  (+ write +)  (* read *);
Process_1, File  SHARE ALL  write;
Process_2, File  SHARE ALL  read;
\end{verbatim}

The behavior of the $\text{File}$ requires $\text{write}$ events to be completed before any $\text{read}$ events, and there should be at least one $\text{write}$ event. The $\text{SHARE ALL}$ composition operation ensures that the schema admits only event traces where corresponding event sharing is implemented. It is defined as following (here $X$, $Y$ are root events, $Z$ is an event type, and $\text{IN}^*$ is a transitive closure of $\text{IN}$).
Event sharing is yet another way of behavior coordination. It is assumed that shared events may appear in the root event at any level of nesting.

The architecture view of this schema in Fig.4 (b) renders root interaction with a line where the shared event name is attached as a label. At the architectural level data items are inputs or outputs of activities and are modeled as operations that may be performed on them. This is a simple and uniform concept. If bringing particular data values in the architecture model is needed, for instance in the assertions describing some constraints on even traces, this can be accomplished by using event attributes.

4.2 BEHAVIOR CONSTRAINTS

A set of behaviors (event traces) is defined by the root event rules, composition operations, and some additional constraints.

**Example 5. Stack behavior.**

SCHEMA Stack  
ROOT Stack_operation: (* ( push | pop ) *);  

ENSURE FOREACH $x: pop$ FROM Stack_operation  
( Number_of (pop) before ($x$) < Number_of (push) before ($x$) );

This schema specifies the behavior of a stack in terms of stack primitive operations. Let IN* denote the transitive closure of the IN relation (similarly, PRECEDES* is a transitive closure for PRECEDES). The ENSURE Boolean expression provides a condition that each acceptable trace should satisfy. The domain of the universal quantifier is the set of all events e, such that (e IN* Stack_operation). The function Number_of (pop) before ($x$) yields the number of pop events e such that (e PRECEDES* $x$). The set of event traces specified by this schema contains only traces that satisfy the constraint. This example presents a filtering operation as yet another kind of behavior composition, and demonstrates an example of combining imperative (event grammar) and declarative (Boolean expressions) features for behavior specification.
4.3 COMPONENTS AND CONNECTORS

Connectors and components, which are the core elements in traditional architecture descriptions, can be uniformly modeled in MP as behaviors. The idea that connectors should be elevated to first-class-citizen status on par with components is often discussed in the literature, for example, in [Taylor et al. 2010].

Suppose that the communication between components is implemented via a buffer of size \( \text{max\_buffer\_size} \), and not necessarily all sent messages are consumed, i.e. some of them could stay in the buffer indefinitely. Each message may be consumed no more than once, and the order of receiving does not necessarily correspond to the order of sending. The root \text{Buffered\_channel} simulates the behavior of a connector between \text{Task\_A} and \text{Task\_B}.

**Example 6.**

SCHEMA Buffered\_transaction
ROOT Task\_A: (* Send *);
ROOT Task\_B: (* Receive *);
ROOT Buffered\_channel: \{* (Send [ Receive ] ) *\} (Overflow | Normal);

\( \text{Task\_A, Buffered\_channel} \; \text{SHARE ALL} \; \text{Send}; \)
\( \text{Task\_B, Buffered\_channel} \; \text{SHARE ALL} \; \text{Receive}; \)

ENSURE FOREACH \( \$x \): Receive FROM Buffered\_channel
\( ( \text{Number\_of (Send) before (} \$x \text{)} - \text{Number\_of (Receive) before (} \$x \text{)}) \leq \text{max\_buffer\_size}; \)
ENSURE FOREACH \( \$x \): Overflow FROM Buffered\_channel
\( ( \text{Number\_of (Send) before (} \$x \text{)} - \text{Number\_of (Receive) before (} \$x \text{)} ) > \text{max\_buffer\_size}; \)
ENSURE FOREACH \( \$x \): Normal FROM Buffered\_channel
\( ( \text{Number\_of (Send) before (} \$x \text{)} - \text{Number\_of (Receive) before (} \$x \text{)}) \leq \text{max\_buffer\_size}; \)

Fig. 5. a) An example of event trace without overflow for the Buffered\_transaction schema with \( \text{max\_buffer\_size} = 3 \).

b) An architecture view for the Buffered\_transaction schema

The view of both components and connectors as coordinated behaviors provides flexibility to define hierarchical protocols for interactions between parts of the system.
5. ENVIRONMENT’S BEHAVIOR

The following example demonstrates how to integrate the behavior model of an environment with the behavior model of a system. The `ATM_withdrawal` schema specifies a set of possible interactions between the Customer, ATM_system, and Data_Base.

Example 7. Withdraw money from ATM.

SCHEMA ATM_withdrawal

ROOT Customer: (* insert_card
request_withdrawal (get_money | not_sufficient_funds) | identification_fails *) *);

ROOT ATM_system: (* read_card validate_id
id_successful check_balance (sufficient_balance dispense_money) | unsufficient_balance | id_failed *) *);

ROOT Data_Base: (* (validate_id | check_balance) *);

Data_Base, ATM_system SHARE ALL validate_id, check_balance ;

COORDINATE $x: insert_card FROM Customer,
$y: read_card FROM ATM_system
DO ADD $x PRECEDES $y OD;
COORDINATE $x: request_withdrawal FROM Customer,
$y: check_balance FROM ATM_system
DO ADD $x PRECEDES $y OD;
COORDINATE $x: identification_succeeds FROM Customer,
$y: id_successful FROM ATM_system
DO ADD $y PRECEDES $x OD;
COORDINATE $x: get_money FROM Customer,
$y: dispense_money FROM ATM_system
DO ADD $y PRECEDES $x OD;
COORDINATE $x: not_sufficient_funds FROM Customer,
$y: unsufficient_balance FROM ATM_system
DO ADD $y PRECEDES $x OD;
COORDINATE $x: identification_fails FROM Customer,
$y: id_failed FROM ATM_system
DO ADD $y PRECEDES $x OD;
If the view of the whole system’s behavior emphasizing the interaction between the parts (components) can be visualized as in Fig. 6, (b), then the view of the root’s standalone behavior can be rendered as a UML Activity Diagram. Since event aggregate patterns (iterations, alternatives, sets) in MP are well structured, it is possible to use Nassi–Shneiderman diagrams [Nassi, Shneiderman 1973] as yet another kind of view.

An event trace generated from the schema can be considered as a use case example. The event trace on Fig. 6, (a) can be viewed also as an analog of UML sequence diagram’s “swim lanes” for Customer and ATM_system interactions. MP models can be integrated into the standard frameworks, like UML, SysML, DoDAF, providing the level of abstraction convenient for architecture models, where MP focuses on the interaction aspects.

The concept of environment in an architecture model includes behavior of other systems, hardware, business processes, and any other behaviors, which are not part of the system under consideration, but may interact with it. In particular, this approach may be of use for analyzing emergent behaviors of System of Systems, when the architecture model of SoS is composed from the models of its components.

6. MULTI-TIER ARCHITECTURE MODELING

Choices of platform, operating system, middleware, database, and such are major architectural choices [Kruchten 2001]. The following example outlines an approach to multilayer architecture modeling. An event in the Top_layer deploys several events in Bottom_layer. This may involve 1..n multiplicity for event coordination.

Example 8.

SCHEMA two-tier-architecture
ROOT Top_layer: (* top_event anything_else *);
ROOT Bottom_layer: (* bottom_event anything_else *);
COORDINATE $x$: top_event FROM Top_layer,
    $y$: (+ bottom_event +) FROM Bottom_layer
DO    ADD $y$ IN $x$ OD;

The coordination is based on IN relation. It models the case when one top_event contains one or more bottom_event. To limit the number of bottom_event repetitions, iteration multiplicity can be used, like:
    $y$: (* <1..3> bottom_event *)

7. COMPONENT REUSE WITH THE JOIN OPERATION

The following compiler’s front-end architecture model is inspired by [Perry, Wolf 1992], [Shaw, Garlan 1996] and the unforgettable picture of compiler architecture from the “Dragon Book” [Aho, Sethi, Ullman 1986](page 13). The following examples demonstrate component reuse with different interaction patterns and emphasize the advantages of separation between the specification of component behavior and the specification of interactions between components.

7.1 COMPILER FRONT END IN BATCH PROCESSING MODE

The Lexer schema models the behavior of a typical LEX machine.

SCHEMA Lexer
ROOT Text_Input:  (* ( String | Unget_char ) *);
    String:  (+ Get_char +);
ROOT Token_processing:  (* Token_recognition *);
    Token_recognition:  {+ RegExpr_Match +}
                      (+ Unget_char +) Fire_rule;
    RegExpr_Match:  (+ Get_char +);
    Fire_rule:  [ Put_token ];
Text_Input, Token_processing SHARE ALL Unget_char;

COORDINATE $t$: Token_recognition FROM Token_processing,
    $s$: String FROM Text_Input
DO
    COORDINATE <!> $r$: RegExpr_Match FROM $t$
    DO $r$, $s$ SHARE ALL Get_char OD
OD;

The Token_recognition event defines Lexer’s behavior according to the semantics when a regular expression in each LEX rule is applied independently, and hence no ordering on RegExpr_Match events is imposed. Each RegExpr_Match performs one or more Get_char until all finite automata involved in the token recognition enter the Error state. Then the winner is selected and look-ahead characters beyond the recognized lexeme are returned into the input stream by Unget_char. The String event contains all Get_char events involved in this cycle of recognizing a token, including characters returned back into the input stream. Some recognized tokens, like spaces or comments, don’t trigger Put_token.

The second COORDINATE composition operation provides for a traversal of each instance of RegExpr_Match within the given Token_recognition (which are unordered, hence the use of <!>). This ensures that all instances of RegExpr_Match share all Get_char with the String coordinated with the Token_recognition.

The following ENSURE constraint requires that at least one input character will be consumed by Token_recognition.
ENSURE FOREACH $t: Token_recognition FROM Token_processing
    (Number_of(Get_char) in ($t) > Number_of(Unget_char) in ($t));

The join operation for schemas looks like:

SCHEMA A
INCLUDE B;
NEW B;

Roots for A
Additional constraints and composition operations involving roots from both A and B

The INCLUDE brings schema B into scope, and NEW B creates a new instance of schema B. The resulting schema A contains roots defined in A and roots defined in B, merges within its scope constraints and composition operations defined in B, and may have additional constraints and composition operations involving all roots.

Appendix 1 contains Base schema specifying properties for the basic relations IN* and PRECEDES*. It is assumed that any MP schema joins Base. This operation on schemas is inspired by the Z schema expressions concept [Spivey 1992]. A typical use of such schema composition may be for assembling the architecture of a System-of-Systems from the architectures of its constituent systems.

The following schema provides a model for bottom-up parsing and reuses stack behavior (represented by push and pop events) defined in Example 5.

SCHEMA Parser
INCLUDE Stack;
NEW Stack;

ROOT Parsing: push
    -- push the start symbol on the stack
    (* Get_token (* Reduce *) Shift *) [Syntax_error];
    Shift: push;
    Reduce: (+ pop +) push Put_node;

ROOT Parse_Tree: (* Put_node *);
    -- Put_node event represents the construction of a parse tree.

Parsing, Stack SHARE ALL pop, push;
Parsing, Parse_Tree SHARE ALL Put_node;

To merge Lexer and Parser schemas into a single schema we need to tell how those components interact. The following schema specifies batch processing.

Example 9.
SCHEMA Batch_processing
INCLUDE Lexer, Parser;
NEW Lexer;
NEW Parser;

ROOT Batch: Produce_tokens Consume_tokens;
    Produce_tokens: (* Put_token *);
    Consume_tokens: (* Get_token *);

Batch, Lexer SHARE ALL Put_token;
Batch, Parser SHARE ALL Get_token;

ENSURE Number_of(Put_token) in (Batch) >= Number_of(Get_token) in (Batch);
The ordering of Produce_tokens and Consume_tokens events ensures that production of the whole set of tokens will precede the consumption. The following diagram represents a view of the Batch_processing architecture. Black arrows stand for the IN relation, wider lines represent abstract interaction defined by the composition operation SHARE ALL, hexagons represent schemas, and rectangles represent root events.

Fig. 7. An architecture view on the Compiler’s front end in batch mode.

7.2 COMPILED'S FRONT END IN INCREMENTAL MODE

Yet another possible interaction is a case in which Parser requests the next token and triggers an event inside Lexer, delivering a token (the usual LEX/YACC operation pattern). The schema Incremental_processing represents such operation mode. The IN relation imposed between Put_token and Get_token events reflects the dependency or synchronization between Lexer and Parser behaviors involved in the token request/delivery. In fact, the Get_token event is now refined with the Put_token event. Incremental_processing schema reuses Lexer and Parser schemas, but defines different interaction pattern.

Example 10.

SCHEMA Incremental_processing
INCUDE Lexer, Parser;
NEW Lexer;
NEW Parser;

COORDINATE $x: Token_recognition FROM Token_processing,
Sy: Get_token FROM Parsing
DO ADD $x IN $y OD;

The merged architecture defines a set of event traces with structure inherited from Lexer and Parser, into Incremental_processing schema with the additional constraints for sharing the token processing events. The following diagram represents a view of the Incremental_processing architecture.

Fig. 8. An architecture view on the Compiler’s front end in incremental mode.
8. SCHEMA REUSE WITH THE MAP COMPOSITION OPERATION

Reuse of a behavior defined by a schema may require mapping of some activities in one schema onto activities in another, thus defining a composite behavior. The MAP operation establishes event aliases (event mapping) between two instances of behaviors. Example 11 provides an architecture model for a user’s login in order to receive access to a system’s services. This solution is reused as another architecture’s component in Example 12.

Example 11
The User requests access to a System’s services by providing his general Id. The System requests that specific credentials be provided. If the supplied credentials are valid, the System authorizes the User to access the services, otherwise the System notifies the User that the received credentials are invalid and the User may re-attempt access up to two more times. At any time the User may decide to abandon the access request.

SCHEMA Authentication_Scenario
ROOT User: request_access
   (* creds_invalid request_access *)
   ( creds_valid (run_services | abandon_access_request) |
     creds_invalid (attempt_exhausted| abandon_access_request) );
request_access: provide_general_ID provide_unique_ID;

The alternative for abandon_access_request always includes an interaction with the System. Absence of the interaction triggers long_wait_for_User in the System.

ROOT System: request_unique_ID
   [ creds_invalid request_unique_ID
     [ creds_invalid request_unique_ID
       [ creds_invalid attempt_exhausted
         invalid_creds_notice cancel_access_request ] ]
     [ ( creds_valid ( authorize_access run_services |
         long_wait_for_User cancel_access_request ) |
       creds_invalid long_wait_for_User cancel_access_request ) ]
   ];
User, System SHARE ALL creds_valid, creds_invalid,
   attempt_exhausted, run_services;

COORDINATE $x: provide_general_ID FROM User,
   $y: request_unique_ID FROM System
   DO ADD $x PRECEDES $y OD;

COORDINATE $x: request_unique_ID FROM System,
   $y: provide_unique_ID FROM User
   DO ADD $x PRECEDES $y OD;

Example 12
The task is to reuse the behavior from the Authentication_Scenario schema. The INCLUDE statement brings Authentication_Scenario schema into the context of Processing schema. This means that all constraints specified in the Authentication_Scenario also will be included.

SCHEMA Processing
INCLUDE Authentication_Scenario;
ROOT Customer: (* work_session *);
work_session: (+ log_in +) (login_succeeds work | login_fails);
work: (* (read | write) *);

ROOT Login_service: (* credentials_check *);
credentials_check: (authorize_access | refuse_access);

ROOT DataBase: (* (read | write) *);

Customer, DataBase SHARE ALL read, write;

COORDINATE $a: authorize_access FROM Login_service,
            $b: login_succeeds FROM Customer
DO ADD $a PRECEDES $b OD;

COORDINATE $a: refuse_access FROM Login_service,
            $b: login_fails FROM Customer
DO ADD $a PRECEDES $b OD;

The following COORDINATE specifies the reuse of the Authentication_Scenario schema and imposes a coordination between each (synchronized) pair of events work_session and credentials_check from Processing schema and a new instance of the Authentication_Scenario behavior. Synchronized COORDINATE composition requires the number of work_session and credentials_check events in the trace to be the same, and each of them has to be totally ordered within the corresponding root.

Since NEW Authentication_Scenario appears in the COORDINATE loop body, a new instance of a complete schema’s Authentication_Scenario trace is created at each COORDINATE iteration to match events selected for coordination. The nested COORDINATE operation follows the nesting of coordinated source and target events. The MAP is yet another event composition performed within the COORDINATE operation. Each A AS B pair establishes A and B as aliases for the same event instance.

COORDINATE $w: work_session FROM Customer,
            $ch: credentials_check FROM Login_service,
            $a: NEW Authentication_Scenario;
MAP $w AS User FROM $a,
    $ch AS System FROM $a,
    work FROM $w AS run_services FROM $a,
    authorize_access FROM Login_service AS authorize_access FROM $a,
    refuse_access FROM Login_service AS cancel_access_request FROM $a;
COORDINATE $log: log_in FROM $w,
            $req: request_access FROM (User FROM $a)
DO MAP $log AS $req
OD;

OD;

Fig. 9 gives an example of event trace generated from the Processing schema. Only IN and PRECEDES relations directly specified in the grammar rules or in composition operations are shown. For instance, the PRECEDES* relation between provide_unique_ID and corresponding creds_valid or creds_invalid is implied by Axiom 9 (Appendix 1).
MAP AS can be considered a generalization of the SHARE ALL composition. For atomic events it is equivalent to SHARE ALL. For example,

\[ A, B \text{ SHARE ALL } c; \]

is equivalent to

\[
\text{COORDINATE }<!> \quad \text{DO MAP} \quad \text{MAP} \quad A \text{ AS } B \quad \text{OD;}
\]

For composite events MAP AS means merging the behaviors as independent threads, which can be coordinated further if needed. If original event structures are

\[ A: \text{pattern1}; \]
\[ B: \text{pattern2}; \]

then MAP A AS B establishes an event AB (for which both A and B are aliases).
\[ AB: \{ \text{pattern1, pattern2 } \}; \]
9. EVENT PARTITIONING AND COORDINATION

Event partitioning may be needed to specify activities like competitive resource sharing at a high level of abstraction, without going into the implementation details. The following example demonstrates event partitioning rendered in the \texttt{SHARE ALL} composition.

\textit{Example 13. Communicating via unreliable channel.}

\texttt{SCHEMA AtoB}
\texttt{ROOT TaskA: (* A\_sends\_request\_to\_B} 
\texttt{(*) A\_receives\_data\_from\_B | A\_timeout\_waiting\_from\_B *)};
\texttt{-- it is assumed that A is the leading actor}

\texttt{ROOT TaskB: (* (B\_working | request\_bounces\_back) *)};
\texttt{B\_working: B\_receives\_request\_from\_A B\_sends\_data\_to\_A;}
\texttt{-- request\_bounces\_back event simulates the connector's unsuccessful attempt to connect to B.}

\texttt{ROOT Connector\_A\_to\_B: (* A\_sends\_request\_to\_B}
\texttt{(*) B\_receives\_request\_from\_A | request\_bounces\_back}
\texttt{A\_timeout\_waiting\_from\_B *)};
\texttt{-- A\_timeout\_waiting\_from\_B may happen either because Connector\_A\_to\_B just fails or because TaskB is not working.}
\texttt{ROOT Connector\_B\_to\_A: (* B\_sends\_data\_to\_A}
\texttt{(*) A\_receives\_data\_from\_B | A\_timeout\_waiting\_from\_B *)};

\texttt{TaskA, Connector\_A\_to\_B SHARE ALL A\_sends\_request\_to\_B;}
\texttt{TaskB, Connector\_A\_to\_B SHARE ALL B\_receives\_request\_from\_A, request\_bounces\_back;}
\texttt{TaskB, Connector\_B\_to\_A SHARE ALL B\_sends\_data\_to\_A;}
\texttt{TaskA, Connector\_B\_to\_A SHARE ALL A\_receives\_data\_from\_B;}

\texttt{Operator [+|] is used in the context of SHARE ALL as an exclusive union (a partitioning of events, XOR-like operation) with respect to the sharing of a specific event. The event A\_timeout\_waiting\_from\_B cannot belong to both Connector\_A\_to\_B and Connector\_B\_to\_A, although sharing of other events between them may be permitted.}

10. REACTIVE EVENT INTEGRATION

Reactive component integration, or implicit invocation [Shaw, Garlan 1996] has been introduced in architecture techniques to capture situations when an activity is triggered by an event arriving from the environment or from another component. The exception handling mechanism in programming languages and the interrupt operator in CSP [Roscoe 1997] provide examples of such control flow.

In MP, the behavior model event stream defined by the event grammar rule may be interrupted at any place by another event that triggers continuation of the event flow using another event pattern. This behavior pattern may be modeled with the WHEN clause. The < and > delimiters determine the scope of events, which could be interrupted.

\texttt{<| event\_pattern 'WHEN' when\_unit, when\_unit, ... |>}

The \texttt{when\_unit} contains the triggering event’s name followed by the event pattern for continuation.\texttt{event\_name => pattern\_list}

\texttt{When\_unit} can be interrupted by another WHEN event. This option may be computationally expensive for event trace generation and should be used with care, to specify for instance an event that may occur in the
environment at any unpredictable moment.

The meaning of the WHEN event pattern for trace generation can be defined with the concept of $\text{CUT}(E)$ as a pattern specifying possible initial segments of an event trace for the event pattern $E$, when $E$ has been interrupted while generating its event trace.

1) $\text{CUT}(A) = \{ A \}$ if $A$ is atomic event pattern
2) $\text{CUT}(A) = \{ A: \text{CUT}(\text{Body}) \}$ if $A$ is a composite event $A: \text{Body}$
3) $\text{CUT}(A \mid B) = \{ \text{CUT}(A) \mid \text{A} \mid \text{CUT}(B) \}$
4) $\text{CUT}(\{A \mid B\}) = \{ \text{CUT}(A), \text{CUT}(B) \}$
5) $\text{CUT}(\{* <n..m> E *\}) = \{* <n..m-1> E *\} \text{CUT}(E)$
6) $\text{CUT}(\{A, B\}) = \{ \text{CUT}(A), \text{CUT}(B) \}$
7) $\text{CUT}(\{* <n..m> E *\}) = \{* <n..m> \text{CUT}(E) *\}$
8) $\text{CUT}(\{+ E +\}) = \{* E *\} \text{CUT}(E)$
9) $\text{CUT}(\{+ E +\}) = \{+ \text{CUT}(E) +\}$

The $\text{CUT}()$ is an abbreviation for an otherwise cumbersome composition of alternative event patterns inserting the triggering event in all possible positions. The WHEN clause event pattern can be defined as:

$$\langle| P \text{ WHEN } A1 ==> A2, B1 ==> B2, \ldots |\rangle =$$

$$\langle| (P \text{ CUT}(P)) \langle* (A1 \text{ CUT}(A2) | B1 \text{ CUT}(B2) | \ldots ) *\rangle (A1 A2 | B1 B2 | \ldots ) \rangle$$

**Example 14. A process that launches and terminates another process.**

Process_A launches a single instance of Process_B, which proceeds concurrently and may either terminate normally, or be terminated by Process_A as an emergency. In both cases Process_B may be launched later again by Process_A.

**SCHEMA Invoke_and_terminate**

**ROOT Process_A:** (* Launch_B do_something [ Abort_B ] *);

**ROOT Process_B:** (* (| Idle \text{ WHEN } Abort_B ==> |) \text{ Launch_B} (| (| b1 b2 b3 |) \text{ WHEN } Abort_B ==> \text{wrap_up}\rangle |)*)

**Process_A, Process_B** SHARE ALL Launch_B, Abort_B ;

When Process_B is Idle, there is no response to Abort_B. The whole WHEN clause around Idle can be omitted, since MP model defines only acceptable event traces.

**11. EVENT ATTRIBUTES**

Event attributes are immutable values associated with event instances. Timing attributes, like time of beginning, time of end, and duration may be associated with any event instance, with obvious constraints on their values implied by PRECEDES and IN relations. If event duration attributes are provided in the model, it becomes possible to perform different timing estimates for event traces, to search for critical paths (similar to the PERT charts [Fazar 1959]), and to obtain average timing estimates for the sets of event traces.

Assertions involving event attributes may impose additional constraints on a system’s behavior. For example, events used as other event attributes may be useful to specify a system’s topology, like networks and other graphs.

**Example 15. Events used as event attributes.**

Dining Philosophers problem ([http://en.wikipedia.org/wiki/Dining_philosophers_problem](http://en.wikipedia.org/wiki/Dining_philosophers_problem)) is often used to illustrate synchronization issues and the techniques for resolving them. The following MP model provides abstract specification of all correct behaviors, but does not provide implementation details.
The example demonstrates the use of events as attributes of other events. Attribute names are binary relations, and syntax and semantics of Alloy relational logic notation [Jackson 2006] are used in this example to describe constraints involving the attribute relations.

Some Alloy-specific syntax:

- the disj keyword implies that the attribute values (events in this example) are disjoint;
- \(~r\) is a transposition of binary relation \(r\);
- \(^r\) stands for the transitive closure of binary relation \(r\);
- the dot, like in \(\text{left}_\text{user}.right\) stands for the left-associative join operator in Alloy;
- \&\& denotes the set intersection operation in Alloy.

SCHEMA Dining_Philosophers
ROOT Philosophers: {<5> Philosopher *};
  Philosopher: {<5> think eat *}
    ATTRIBUTES { -- attributes of the Philosopher event
      disj left, right: Philosopher;
      disj left_fork, right_fork: Fork; }

Using events as attributes of other events extends the standard relations PRECEDES and IN, for instance, to model interacting components' topology and other dependencies between events.

Event grammar rules appear to be yet another event attribute with a specific syntax and without attribute name. By assigning attribute names to the behavior rules, it may be possible to define several different behaviors as attributes and to make the selection of a behavior attribute dependent on other attributes. This may be used to specify dynamic and product line architectures.

```alloy
  eat: { use_left_fork, use_right_fork };
  use_left_fork: use_fork;
  use_right_fork: use_fork;
```

No ordering is required for \(\text{use}_\text{left_fork}, \text{use}_\text{right_fork}\) activities.

ROOT Forks: {<5> Fork *};
Fork: {<5> ( idle | use_fork ) *}
  ATTRIBUTES {
    disj left_user, right_user: Philosopher; }

The following constraints provide topology specification as filters for trace generation.

Several attributes are mutually symmetric relations.

```alloy
  ENSURE ( left = ~right and left_fork = ~right_user and right_fork = ~left_user );
```

Philosophers form a cycle. Standalone \(\text{Philosopher}\) event name stands here for the set of all events of this type in the event trace (following Alloy conventions).

```alloy
  ENSURE FOREACH $p: Philosopher FROM Philosophers ($p.^left = Philosopher );
```

Neighbors share the same \(\text{Fork}\).

```alloy
  ENSURE FOREACH $f: Fork FROM Forks ( $f.left_user.right.left_fork = $f );
```

Philosophers behavior is synchronized via event sharing. \(\text{A} \mid+\mid \text{B}\) is an exclusive union of events w.r.t. SHARE ALL, which prevents \(\text{A}\) and \(\text{B}\) from sharing the same instance of the event \(E\) (partition for sharing) in \(\text{(A} \mid+\mid \text{B)}, \text{C} \text{ SHARE ALL } E\).

```alloy
  COORDINATE <!> $p: Philosopher FROM Philosophers
```
DO
  ( use_left_fork && ^IN.$p) |+| ( use_right_fork && ^IN.(p.left) ),
  $p.left_fork
  SHARE ALL  use_fork
OD;

12. A FEW WORDS ON ASSERTIONS AND QUERIES

An event trace represents an example of particular execution of the system or a use case, especially if the behavior of the environment is included. Event traces can be effectively derived from the event grammar rules and then adjusted and filtered according to the composition operations and constraints in the schema. This justifies the term executable architecture model. For a given MP schema it is possible to obtain all valid event traces up to a certain limit. Usually such a limit (scope) may be set by the maximum total number of events within the trace, or by the upper limit on the number of iterations in grammar rules (recursion can be limited in a similar way). For many purposes a modest limit of 3 iterations will be sufficient. This process of generating and inspecting event traces for the schema is similar to the traditional software testing process.

In the case of MP models it is possible to automatically generate all event traces within the given scope (exhaustive testing). Careful inspection of generated traces (scenarios/use cases) may help developers identify undesired behaviors. Usually it is easier to evaluate an example of behavior (particular event trace) than the generic description of all behaviors (the schema). The Small Scope Hypothesis [Jackson 2006] states that most errors can be demonstrated on relatively small counterexamples.

The assertion language for MP requires a rigorous and precise discussion, and the use of assertion checking for MP model testing and debugging is not subject of this paper. Here are some considerations outlining the possible approach.

The event trace is a set of events and the assertion formalism can embrace the traditional predicate calculus notation. Properties of behavior can be formalized as assertions about traces (similar to the ENSURE constraint), and verified exhaustively for all event traces within the scope, yielding the counterexamples when the assertion is violated. For example, hazard states can be specified as a result of certain interactions between the system and its environment, and the traces within scope can be searched for a trace that matches the hazard scenario. Since assertion checking is performed on a complete event trace, it becomes possible to refer to events following a given event to specify fairness conditions. This brings the expressiveness of MP assertions closer to temporal logic [Pnueli 1981]. For instance, simple_message_flow schema (Example 2) can be annotated with the assertion

\[
\text{ASSERT FOREACH } x: \text{send FROM Task_A Has_following(receive)} (x);
\]

where Has_following(receive) predicate is based on the PRECEDES* relation.

In a similar fashion queries can be performed on the traces, providing different kinds of statistics. For example, collecting a representative amount of event traces and calculating durations for event sequences of interest can provide system performance estimates.

Another example of an add-on in MP model may be the probability of an event in alternatives, like \([0.3] \text{ A} \mid [0.7] \text{ B}\) establishing that A happens with the probability 0.3 and B with probability 0.7. Now it becomes possible to estimate probabilities of certain event traces within a given scope, e.g. probability for the system to get into a hazard state. This opens a direction for system simulation and statistical experiments based on executable systems.
architecture models and their environment models. [Songzheng Song et al. 2014] has an example of such experiment with MP model using PAT model checker [Jun Sun et al. 2009].

Assertions and queries may be generic for a class of architecture models and could be reused, as Appendix 1 suggests.

13. IMPLEMENTATION
An online demo of the early MP version Eagle6 (on-line editor, event trace generation and visualization, simple query processor, and rudimentary event trace probability estimation) is available at [http://eagle6modeling.riverainc.com/]. This web site also provides several complete examples.

The MP prototype [Auguston, Whitcomb 2010] has been implemented as a compiler generating an Alloy model [Jackson 2006] from the MP schema and then running the Alloy Analyzer to obtain event traces and to perform assertion checks. It has benefited from Alloy’s relational logic formalism and visualization tools. Performance depends on the performance of SAT solver used by Alloy Analyzer.

Direct trace generation from the event grammar can be accomplished quite efficiently, and the process of generating all traces for the given schema within a given scope can be roughly described by the following procedure.

1. For each root in the schema derive a collection of all possible event traces within a given scope.
2. Select one trace from each root’s collection, assembling the resulting trace from root traces with matching numbers of shared/coordinated events.
3. Apply schema’s composition operations and filters. If the resulting composed trace is consistent with the schema’s filters (including Axioms from Appendix 1) and composition operations, it is included into the schema’s trace collection. Otherwise, proceed with the next selection (step 2).

This process has potential for optimization by applying early pruning whenever possible. The main optimization ideas stem from the considerations that composition operations (COORDINATE, SHARE ALL, and MAP) usually require an equal number of selected events in the matching traces. Root traces can be sorted according to the number of matching events to avoid selection of inconsistent root traces in Step 2. Rearrangement of composition operations and filters may also provide a significant speed up in the trace assembly.

A prototype trace generator has been built by converting MP schemas into a C++ code and then compiling and running the generated C++ code to obtain all event traces within a given scope. This architecture solution is similar to the one implemented in the SPIN/PROMELA model checker (using C as a target language) [Holzmann 2004].

Several optimizations mentioned above have been implemented. A sample run on an iMac with 2.8 GHz/4 GB yields the following performance for a schema example with approximately 60 lines of MP source text, including 9 roots, 10 composite event types, 12 atomic event types, 12 SHARE ALL compositions, and for a maximum scope of 3 for iterations. Actually, it is an architecture model for the MP -> C++ prototype itself, the complete MP code for this model is available as Example 9 in the MP Crash Course on [http://wiki.nps.edu/display/MP](http://wiki.nps.edu/display/MP) and can be executed on Eagle6 prototype as well.

- Total 1328 traces generated, with total 79836 events, average 60.1175 events/trace, max trace length 69;
• Initial search space (number of all root traces before filtering) 35100;
• Selection ratio 3.78348%, generation speed 18021.8 events/sec;
• Elapsed time (including compilation of the generated C++ code) 4.42997 sec.

14. CONCLUSIONS

MP executable architecture models provide a high level of abstraction for testing, verifying, and documenting system architecture early in the design phase. The main advantages may be summarized as follows.

• MP focuses a developer’s attention on the behavior of the system early in the process.
• The ability to separate behavior models of components from the models of interactions between them simplifies the modeling process and facilitates the reuse of architecture models.
• The schema framework is amenable to stepwise architecture refinement, reuse, composition, visualization, and application of automated tools for sanity checks.
• Executable system architecture models integrated with environment behavior models can be helpful for identifying emergent behaviors.
• The ability to generate an exhaustive set of use cases (within a given scope) for requirements specification and for testing the system’s implementation. This emphasizes the role of architecture models as a bridge between the requirements and design.
• The pseudo-code style of use cases (event traces) derived from MP schema provides a uniform communication vehicle for different stakeholders. It may be easier for humans, especially not skilled in formal specification notation, to understand and inspect examples of system behavior, neither to deal with the complete and formal MP schema, from which these use cases have been derived. Assertion checking can automatize search for counterexamples violating expected behavior properties.
• The ability to extract different architecture views from the same MP architecture model.
• The ability to develop performance estimates based on statistics obtained from the generated event traces.

14.1 WHAT IS NEXT?

Architecture modeling has substantial consequences for the next phases in software design process. Here are some threads of research stemming from the ideas described above.

• Testing automation. Monitoring the behavior of an implemented system using the MP executable architecture model as an oracle. If the source code of implementation can be instrumented to mark which segments of code start and end corresponding MP events, it becomes possible to log actual execution traces (using [Lamport 1978] timestamps for partial ordering monitoring), and to check the actual traces for consistence with expected behaviors. Test cases could be constructed from the MP event traces using the environment’s behavior as the source for inputs and deriving the oracle from the corresponding MP behavior event trace.
• Developing methods and techniques for static analysis of the architecture model, for example, by verifying MP models with a model checking tool. The first prototypes are presented in [Jiexin Zhang et al. 2012] and [Songzheng Song et al. 2014].
• Introducing metrics for MP models for system cost estimates based on the architecture models. Function Points [Albrecht 1979] can be identified as abstract interactions between components and between the system and its environment in the MP model.
Consequently FP analysis and COCOMO II [Boehm et al. 2000] techniques could be applied for the early system cost estimates.

- **Statistical simulation and analysis of system’s behavior models** [Songzheng Song et al. 2014].
- **Development of reusable architecture patterns and architecture views libraries.**
- **Development of business process models in MP.** Existing process modeling frameworks (BPEL, BPMN [Grosskopf et al. 2009], IDEF) usually follow the “single flowchart” paradigm. MP separates component behaviors from the component interaction, and thus provides a multidimensional picture of concurrent behaviors, with overlapping threads of process phases, participating actors, and other environment behaviors. Exhaustive scenario generation, assertion checking, and queries supported by automated tools (like critical path calculation on PERT charts [Fazar 1959]) could be useful for business process model verification and validation within the MP framework.

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**APPENDIX 1**

**Base** schema specifies a filter for every MP event trace and ensures that it satisfies partial order axioms for IN* and PRECEDES* relations. It uses predefined generic event type Event. The special variable $Trace stands for the whole trace specified by a schema. We use symbols $\neg$, $\wedge$, $\Rightarrow$ for Boolean operations here.

**SCHEMA Base**

There are no root events, this schema is used only to bring the following filter into derived schema.

**ENSURE FOREACH $a$, $b$, $c$: Event FROM $\text{STrace}$**

--- **Mutual Exclusion of Relations**

- $(a \ PRECEDES^{*} b \Rightarrow \neg(a \ IN^{*} b)) \wedge \text{--Axiom 1}$
- $(a \ PRECEDES^{*} b \Rightarrow \neg(b \ IN^{*} a)) \wedge \text{--Axiom 2}$
- $(a \ IN^{*} b \Rightarrow \neg(a \ PRECEDES^{*} b)) \wedge \text{--Axiom 3}$
- $(a \ IN^{*} b \Rightarrow \neg(b \ PRECEDES^{*} a)) \wedge \text{--Axiom 4}$

--- **Non-commutativity**

- $(a \ PRECEDES^{*} b \Rightarrow \neg(b \ PRECEDES^{*} a)) \wedge \text{--Axiom 5}$
- $(a \ IN^{*} b \Rightarrow \neg(b \ IN^{*} a)) \wedge \text{--Axiom 6}$

--- **Irreflexivity for PRECEDES* and IN* follows from non-commutativity.**

--- **Transitivity**

- $(a \ PRECEDES^{*} b) \wedge (b \ PRECEDES^{*} c) \Rightarrow (a \ PRECEDES^{*} c) \wedge \text{--Axiom 7}$
- $(a \ IN^{*} b) \wedge (b \ IN^{*} c) \Rightarrow (a \ IN^{*} c) \wedge \text{--Axiom 8}$

--- **Distributivity**

- $(a \ PRECEDES^{*} b) \wedge (b \ PRECEDES^{*} c) \Rightarrow (a \ PRECEDES^{*} c) \wedge \text{--Axiom 9}$
Each MP schema uses Base as a default extension. As a result, all event traces will be filtered for compliance with the Axioms. For example, the following schema has an empty set of traces, because it violates Axiom 5 for partial ordering.

**SCHEMA Wrong**

**INCLUDE** Base;

**NEW** Base;

**ROOT** A: a b;

**ROOT** B: b a;

A, B **SHARE ALL** a, b;

**REFERENCES**


BOSCH, J., 2000, Design and Use of Software Architectures, ACM Press and Addison-Wesley.


HAREL, D., 1992, Biting the silver bullet: toward a brighter future for system development, IEEE Computer, Vol. 25(1), pp.8-20

HOLZMANN, G., 2004, The SPIN Model Checker, Boston, Addison-Wesley 2004


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