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Decision-Based Metrics for Test and Evaluation Experiments

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Decision-Based Metrics for Test and Evaluation Experiments

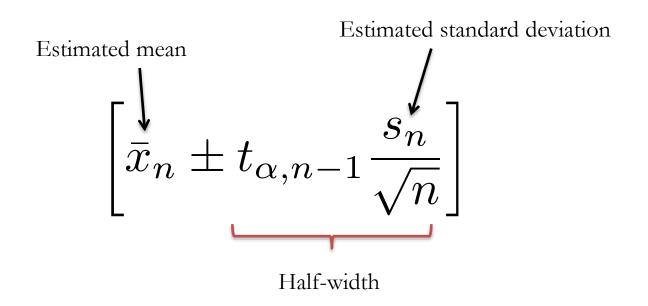
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Research Question

- Sequential sampling rules can be used to decide the number of experimental replications
- These rules are often made independently of the desired outcome or decision.
- Let D be the decision threshold for making a decision about a system.

How can we use decision criteria to inform sequential sampling rules?

Confidence Intervals



- Confidence intervals represent the uncertainty in the mean performance of a system based on *n* samples
- Often assume normality in the data
- The half-width should be small enough to ensure that the variation in the mean estimate is acceptable

Fixed Sampling Rules – Choosing the sample size

Can use standard deviation estimate $n \geq \left(\frac{z_{\alpha}\sigma}{\delta}\right)^2$ Desired half-width of confidence interval

- If a variance estimate is available, can calculate ahead of time how many samples should be taken to obtain a confidence interval with a half-width smaller than δ .
- Challenges:
 - hard to choose δ
 - *n* might be large
 - Variance estimate might not be available

Solution: Sequential Sampling Rules

Absolute precision rules: fix a value of δ and collect samples until the half-width is smaller than δ .

$$n^* = \text{smallest } n \text{ s.t. } t_{\alpha, n-1} \frac{s_n}{\sqrt{n}} \le \delta$$

Relative precision rules: fix a percentage δ and collect samples until the half-width is within some percent of the sample mean.

$$n^* = \text{smallest } n \text{ s.t. } t_{\alpha, n-1} \frac{s_n}{\sqrt{n}} \le \delta \bar{x}_n$$

Pros: can stop earlier when desired precision is reached, do not need variance estimate ahead of time

Cons: statistical bias (confidence interval coverage $<1-\alpha$), could still require a large number of samples

Example from Small Arms Testing

Table reproduced from TOP 3-2-045

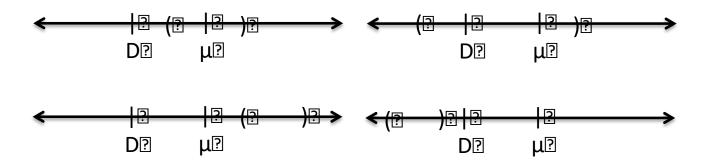
MAXIMUM PERMISSIBLE <u>ERROR OF MEASUREMENT*</u>
±0.5% full-scale reading.
$\pm 1\%$ at rates up to 6000 spm and burst lengths of 100 rounds.
<u>+</u> 0.025 mm.
<u>+</u> 0.6 °C (1 °F).
0.1% or 0.5 m/s (whichever is highest) for bursts to 6000 spm.

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^{*}Values can be assumed to represent ±2 standard deviations.

Four Types of Confidence Interval (CI) Results

- Let μ be the true mean system performance.
- Let D be the decision threshold
 - If CI>D, then "Accept" the system as meeting the requirement
 - If CI<D, or includes D, then "Reject" the system as failing to meet the requirement
- Confidence intervals can either
 - correctly include (cover) μ or not
 - correctly determine whether μ is greater than D, or not.



Cover & Correct	Cover & Incorrect
Fail to cover & Correct	Fail to cover & Incorrect

Decision-Based Procedures

- Traditional sequential rules do not incorporate D
- New rules directly incorporate D in the stopping criterion

$$n^* = \text{smallest } n \text{ s.t. } t_{\alpha, n-1} \frac{s_n}{\sqrt{n}} \le |\bar{x}_n - D|$$

- Results in confidence intervals that usually do not include D
- Will require more samples if the true performance is close to D
 - Ensures precise confidence interval if decision is a close call
- Will end early if true performance is far from D
 - Saves time/replications if the decision is obvious

Conclusions and Implementation

- The expected number of samples required by the procedure depends on how far the unknown μ is from the known requirement D.
- $\sigma=1$, $1-\alpha=90\%$

$ \mu - D $	Expected no. samples
1.0	5.0
0.5	10.9
0.3	28.6
0.1	263.9
0.05	1095.9
0.0	∞

Confidence interval coverage can be poor for small sample sizes. Solution: aim for high confidence (99%) known actual confidence may be closer to 95% or 90%.

Conclusions and Future Work

- Developed a new sequential stopping rule that incorporates the decision requirement D.
 - Potentially more efficient in making a decision.
- There may be significant bias associated with sequential rules, along with our proposed modifications. Simulation testing can be used to estimate the bias.
- Looking for ongoing/real test data to estimate the impact of sequential rules.